

# Radical Diffusion Crossover Phenomenon in Glass-Forming Liquids

Jakov Slade<sup>†</sup>, Dalibor Merunka,<sup>\*,†</sup> and Miroslav Peric<sup>‡</sup>

<sup>†</sup>Division of Physical Chemistry, Ruđer Bošković Institute, Bijenička cesta 54, HR-10000

Zagreb, Croatia

<sup>‡</sup>Department of Physics and Astronomy, California State University, Northridge, Northridge,

California 91330, United States

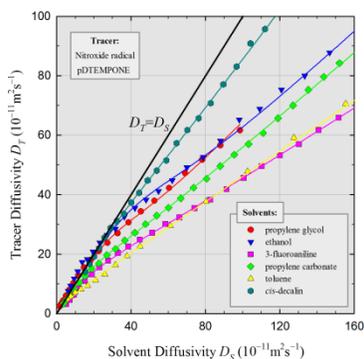
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\*Corresponding author. E-mail: merunka@irb.hr, Tel: +3851-4561-136

## Abstract

We studied the diffusivities of a nitroxide radical at various temperatures in six glass-forming molecular liquids by electron spin resonance. By comparing the radical diffusivities and solvent self-diffusivities, we found that the radical diffusivities are lower than the self-diffusivities at high temperatures and approach them at low temperatures in all liquids. This crossover behavior was considered as evidence that a single-molecule diffusion process transforms into a collective process with temperature lowering. The crossover phenomenon was analyzed by a novel, simple diffusion model, combining collective and single-molecule diffusion processes, and it was compared to the Arrhenius crossover phenomenon. The obtained results suggest that future studies of tracer diffusion could contribute to a better understanding of diffusion mechanisms in glass-forming liquids. The proposed diffusion model could be used to study the crossover phenomena of tracer diffusion measured by other techniques, and it could serve as a base for developing more advanced models.

## TOC graphics



Translational diffusion of host molecules (self-diffusion) and diluted guest molecules (tracer diffusion) in molecular liquids have been studied by a number of experimental and theoretical methods due to theoretical and practical interests.<sup>1-3</sup> If the guest molecule is a free radical, its diffusion can be studied by electron spin resonance (ESR). Since the relative motion of the radical's molecules modulates spin interactions between them, the shape of the ESR spectrum of the radical depends on its diffusion coefficient (diffusivity). By measuring the shape changes of the ESR spectrum with radical concentration, we obtain information about the radical diffusivity.<sup>4-7</sup>

Diffusion in glass-forming liquids shows interesting phenomena whose explanation could help to understand the nature of glass transition. One phenomenon, which is detected in many tracer and self-diffusivity measurements in the supercooled state (below the melting temperature  $T_m$ ), is a great enhancement of diffusivity over that predicted by the Stokes-Einstein (SE) law.<sup>8-</sup>  
<sup>11</sup> The violation of the SE law appears below the crossover temperature  $T_c \approx 1.2T_g$  ( $T_g$  is the glass transition temperature), and it strongly decreases as the tracer molecule exceeds the host molecule's size. This size effect supports the widely accepted view that the SE violation is associated with spatially correlated and heterogeneous dynamics in the supercooled state, but a clear connection between these two phenomena is yet to be established.<sup>8-11</sup>

Another phenomenon detected in diffusivity measurements in glass-forming metallic liquids is the Arrhenius crossover phenomenon at the temperature  $T_A$ , which is much higher than  $T_c$ .<sup>12</sup> This phenomenon denotes a change in the temperature dependence of diffusivity from the Arrhenius dependence above  $T_A$  into a stronger non-Arrhenius one below  $T_A$ . The Arrhenius

crossover phenomenon is believed to reflect the onset of cooperativity in the motion of particles, which move relatively independently above  $T_A$  and begin to move in a more correlated and cooperative fashion below  $T_A$ .<sup>9-13</sup> The relative crossover temperature in metallic liquids  $\theta_A = T_A/T_g \approx 2$  was compared to  $\theta_A$  in molecular and network liquids,<sup>12</sup> which were estimated from relaxation time and viscosity measurements.<sup>13</sup> It was found that  $\theta_A$  is lower for more fragile glass formers, i.e., those with the steeper temperature dependence of transport properties at  $T_g$ .<sup>12</sup> As the most fragile group of glass formers, molecular liquids exhibit  $\theta_A \approx 1.4$ , which means that  $T_A$  is close to  $T_m$ .

Several molecular dynamics simulations confirmed the belief that diffusive motion in a supercooled liquid becomes more cooperative and collective by the temperature decrease.<sup>14-16</sup> One of the scarce experimental pieces of evidence for this belief is a slight difference between the diffusivities of two isotopes of tracer atoms in a supercooled metallic liquid.<sup>17</sup> This very weak isotope effect was explained by the participation of several atoms in the diffusion process. It was argued that in this case, the rate of diffusion processes depends on the average mass of participating atoms, which diminishes the effect of the mass change of one participating atom. Unfortunately, there are not many experimental observations of cooperative diffusion below  $T_A$ . Therefore, more experimental evidence of such cooperative diffusion motion would be desirable.

In this Letter, we report ESR results for the temperature dependences of the tracer diffusivity of a nitroxide radical  $D_T(T)$  in six molecular glass formers. Following indications for coupling between diffusive motion of tracer and host molecules,<sup>7</sup> we determined the temperature

dependences of self-diffusivity  $D_S(T)$  in all liquids from the literature data (Figure S1 and Table S1 in SI1). It was revealed that  $D_T(T)$  is lower than  $D_S(T)$  at high temperatures and approaches  $D_S(T)$  at low temperatures. We considered the crossover behavior of  $D_T(T)$  as evidence that diffusive motion in liquids becomes more collective upon cooling, and we analyzed this phenomenon using a simple diffusion model.

We studied the diffusivity of nitroxide radical pDTEMPONE (perdeuterated 2,2,6,6-tetramethyl-4-oxopiperidine-1-oxyl) in glass-forming liquids: propylene glycol (PG), ethanol (EtOH), 3-fluoroaniline (3-FA), propylene carbonate (PC), toluene (Tol), and *cis*-decalin (*c*-Dec). The chemical structures of the radical and solvents are presented in Figure S2 in SI2. In order to improve the method, we studied radicals labeled with  $^{15}\text{N}$  and  $^{14}\text{N}$  isotopes ( $^{15}\text{N}$ - and  $^{14}\text{N}$ -pDTEMPONE), which have different ESR spectra but practically equal diffusivities.

Here, we give a brief overview of the ESR method for measuring radical diffusivity, which is described in more detail in SI3 and refs 7, 18, and 19. First, we estimated the purities of pDTEMPONE radicals by using solutions of Fremy's salt radicals as standards.<sup>20</sup> Then, we recorded ESR spectra of 12 solutions with different concentrations of  $^{15}\text{N}$ - and  $^{14}\text{N}$ -pDTEMPONE in each solvent at various temperatures. We fitted all ESR spectra (Figure S3 and Table S2) to the theoretical ESR spectral function for solutions of  $^{15}\text{N}$ - and  $^{14}\text{N}$ -labeled radicals with spin interactions.<sup>5,7,18,19</sup> The best-fit values of the spin coherence-transfer rate  $\Lambda$ , which is the best ESR parameter to study radical diffusion, were fitted to a linear function of radical concentration at each temperature (Figure S4). The linear concentration coefficient of  $\Lambda$ , determined as the slope of the linear function, was compared to its theoretical dependence on

radical diffusivity (Figure S5). In theoretical treatment, we modeled dissolved radicals as continuously diffusing hard spheres and applied formalism of the kinetic equations for the spin density matrices of radicals.<sup>4,7,18,19,21</sup> From this comparison, we obtained the diffusivities of <sup>15</sup>N- and <sup>14</sup>N-pDTEMPONE at each temperature, which show similar values (Figure 1). The diffusivity of pDTEMPONE, calculated as the average value of the diffusivities of <sup>15</sup>N- and <sup>14</sup>N-pDTEMPONE, is presented as a function of temperature in all liquids (Figure 1).

From the SE law for the tracer diffusivity  $D_T = k_B T / (6\pi\eta r_T)$ , where  $r_T$  is the radius of the tracer molecule and  $\eta$  is the viscosity of the solution, the expected tracer to self- diffusivity ratio is:

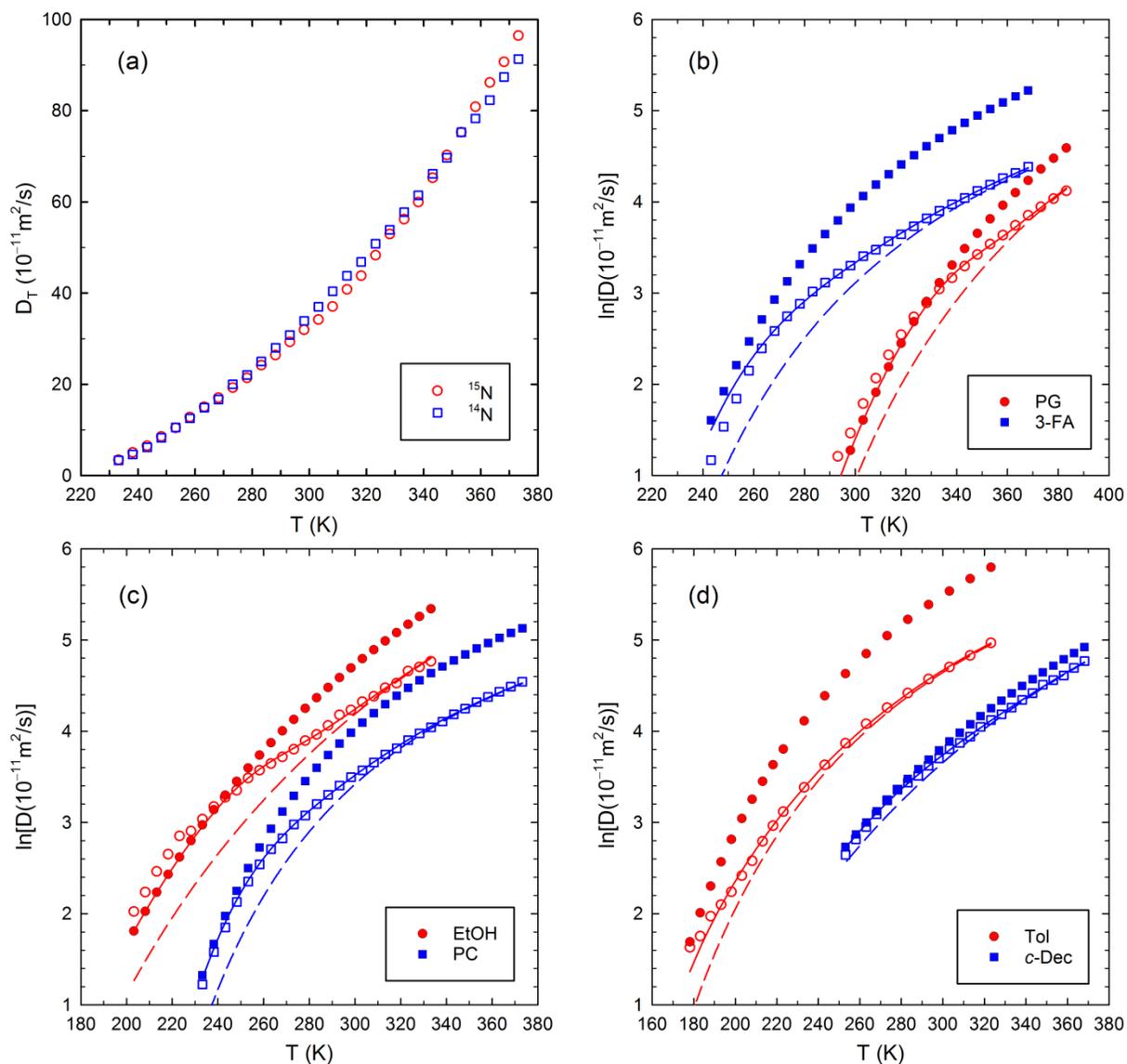
$$R_d \equiv D_T / D_S = r_S / r_T, \quad (1)$$

where  $r_S$  is the radius of the solvent molecule. According to another prediction model for the tracer diffusivity of various solutes in organic solvents and water,<sup>2</sup> this ratio is:

$$R_d = \left( \frac{1 + M_S / M_T}{2} \right)^{1/2} \left( \frac{2}{1 + r_T / r_S} \right)^2, \quad (2)$$

where  $M_T$  and  $M_S$  are the molecular masses of the tracer and solvent molecules, respectively. Both models predict a constant value of  $R_d$ , which depends only on the relative sizes and masses of the tracer and solvent molecules. By using the known masses and calculated radii of the tracer and solvent molecules in our case (Figure S2), the ratios  $R_d$  from eqs 1 and 2 were estimated (Table 1). The radii are calculated from the van der Waals volumes obtained by the fast-calculation method,<sup>22</sup> assuming spherical molecular shapes.

**Figure 1.** (a) Diffusivities versus temperature for  $^{15}\text{N}$ - and  $^{14}\text{N}$ -pDTEMPONE radicals in PC. (b,c,d) Diffusivities of pDTEMPONE (empty symbols) and fitted self-diffusivities (filled symbols) versus temperature in studied liquids. The full and dashed lines denote the radical diffusivity fits to eq 3 and their extrapolated high-temperature dependences, respectively.



**Table 1.** Experimental values of melting temperature  $T_m$ , glass transition temperature  $T_g$ , and fragility index  $m$ . Calculated radical to self-diffusivity ratio  $R_d$  by eqs 1 and 2. The best-fit values of parameters  $R_H$ ,  $\Delta$ , and  $T_{cr}$  of the simple diffusion model (eq 3). The best-fit values of Arrhenius crossover temperatures  $T_A$  from viscosities.

Liquid	$T_m$	$T_g$	$m$	$R_d$	$R_d$	$R_H$	$\Delta$	$T_{cr}$	$T_A$
	(K)	(K)		eq 1	eq 2		(K)	(K)	(K)
PG	211	167	52	0.76	0.63	0.64	18	346	358
EtOH	159	94	55	0.67	0.50	0.58	24	266	199
3-FA	271	173	70	0.82	0.73	0.42	37	269	319
PC	224	160	99	0.80	0.69	0.55	30	267	303
Tol	178	117	103	0.82	0.70	0.43	36	179	236
<i>c</i> -Dec	230	145	149	0.96	0.90	0.84	34	298	337

In order to relate radical and solvent diffusivities, we collected numerical and graphical self-diffusion data and determined the temperature dependence of self-diffusivity  $D_s(T)$  by fitting (Figure S1 and Table S1). Comparing the values of radical diffusivities and the fitted values of self-diffusivities at measured temperatures, we found that the ratio between them  $R_d$  varies with temperature in all liquids (Figure 1). At high temperatures, the radical diffusivities are lower than the self-diffusivities implying that  $R_d < 1$  holds, as predicted by eqs 1 and 2. However, the radical and self-diffusivities have similar values at low temperatures, where  $R_d \approx 1$

holds. Following the explanation of the weak isotope effect on tracer diffusivity in metallic liquids,<sup>14,17</sup> we propose that the crossover behavior of radical diffusivity upon cooling results from the participation of more and more molecules in the diffusion process, which causes the radical and self- diffusivities to differ less and less.

In order to quantify the crossover phenomenon, we constructed a simple diffusion model where one molecule can diffuse via either a single-molecule process or a collective process in which several molecules participate. Consequently, the self-diffusivity can be expressed as  $D_S(T) = D_{S1}(T) + D_{Sc}(T)$ , where  $D_{S1}(T)$  and  $D_{Sc}(T)$  are the single-molecule and collective contributions, respectively, while  $D_T(T) = D_{T1}(T) + D_{Tc}(T)$  is an analogous expression for tracer diffusivity. According to eqs 1 and 2, the ratio between the tracer and solvent single-particle diffusivities  $R_H = D_{T1}(T)/D_{S1}(T)$  is taken as a temperature-independent constant. Based on the explanation of the weak isotope effect on tracer diffusivity in supercooled metallic liquids,<sup>14,17</sup> we expect that the collective diffusivities of tracer and solvent molecules differ much less than their single-particle diffusivities, and, thus we make a simple assumption  $D_{Tc}(T) = D_{Sc}(T)$ . By defining the quantity  $p_1(T) = D_{S1}(T)/D_S(T)$ , the tracer diffusivity can be written as  $D_T(T) = D_S(T)R_d(T)$ , where the diffusivity ratio is  $R_d(T) = R_H p_1(T) + 1 - p_1(T)$ . The diffusivity of the solvent molecule in this model depends on the molecule's displacement during the diffusion process and the rate at which this process occurs. If one assumes similar displacements during the single-molecule and collective diffusion processes, the quantity  $p_1(T)$  becomes the ratio between the rates of single-molecule and any diffusion processes. Thus, the probabilities that the molecule participates in a given diffusion process as a single entity or part

of collective rearrangements are given by  $p_1$  and  $p_c = 1 - p_1$ , respectively. Supposing a simple two-state behavior of the probabilities, we get  $p_1/p_c = \exp[-(E_{TS} - TS_{TS})/(k_B T)]$ . By the general considerations of theory for collective diffusion,<sup>23</sup> the energy difference  $E_{TS} > 0$  can be understood as an extra energy cost for the solitary diffusing molecule compared to the molecule that participates in the collective diffusion process. On the other hand, the collective diffusion process demands coherent movements of participating molecules, which gives the extra entropy cost  $S_{TS} > 0$  for the molecule that participates in the collective process compared to the solitary diffusing molecule. We can now redefine the two-state parameters by introducing  $T_{cr} = E_{TS} / S_{TS}$  as the crossover temperature at which  $p_1 = p_c = 1/2$  and  $\Delta = 2k_B T_{cr}^2 / E_{TS}$  as half of the temperature width of crossover behavior. Thus, the fitting function for radical diffusivity takes the form:

$$D_T(T) = D_S(T)[R_H p_1(T) + 1 - p_1(T)]; p_1(T) = \left[ 1 + \exp\left(\frac{2T_{cr}}{\Delta} \frac{T_{cr} - T}{T}\right) \right]^{-1} \quad (3)$$

where  $D_S(T)$  is the fitted temperature dependence of self-diffusivity. We listed the best-fit parameters of the fitting function in eq 3 for all liquids (Table 1) and presented the fitted temperature dependences of radical diffusivities (Figure 1). The high-temperature dependences of fitted radical diffusivities  $R_H D_S(T)$  are extrapolated to low temperatures to illustrate the crossover effect on radical diffusion (Figure 1), which is indicated by the difference between the experimental data and dashed lines.

By comparing the values of  $R_d$  calculated by eqs 1 and 2 with the fitted values of  $R_H$  (Table 1), we can see a good agreement for PG, EtOH, and *c*-Dec, while the calculated values are higher than the fitted ones for 3-FA, PC, and Tol. A possible cause of the disagreement for the latter three liquids could be their molecules' non-spherical and disk-like shapes. In order to compare the radical diffusion and Arrhenius crossover phenomena, we estimated the Arrhenius crossover temperatures  $T_A$  (Table 1) by fitting the experimental viscosity data available for all liquids (see SI4). We obtained the temperature dependences of viscosities (Figure S6) by using the fitting formula with the parabolic non-Arrhenius term, which was previously applied to analyze metallic liquids' diffusivities.<sup>12</sup> The estimated values of  $T_A$  from the viscosities are checked against the literature values of  $T_A$ , which were determined mainly from relaxation time measurements (see SI4). The estimated values of  $T_A$  were found to be within or a little higher than the ranges of literature values (Table S3). The estimated temperatures  $T_A$  in all studied liquids except EtOH are close to the temperatures  $T_{cr} + \Delta$ , marking the onset of radical diffusion crossover (Table 1).

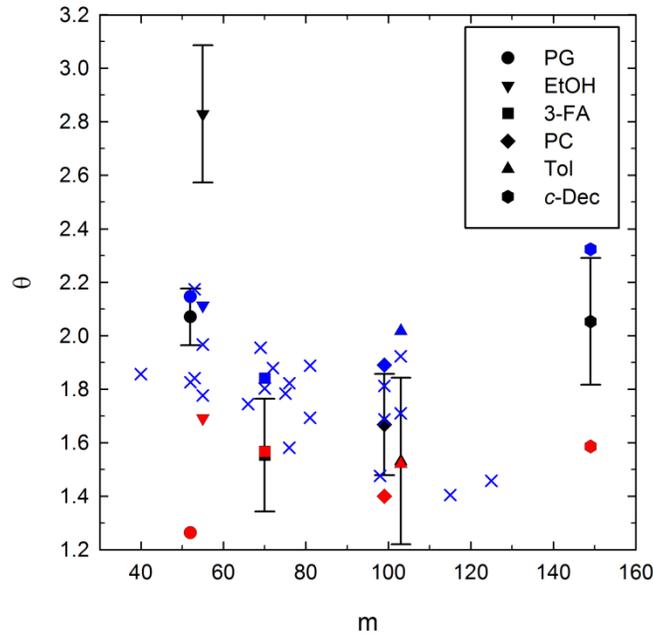
The literature values of  $T_g$  and kinetic fragility index  $m$  for *c*-Dec<sup>24</sup> and other solvents<sup>25</sup> are listed in Table 1, together with the literature values of  $T_m$ . Using these values, we presented the relative characteristic temperatures  $\theta_{cr} = T_{cr}/T_g$ ,  $\theta_A = T_A/T_g$ , and  $\theta_m = T_m/T_g$  as a function of  $m$  (Figure 2). Error bars denote the crossover regions of radical diffusion, which lie between  $\theta_{cr} - \theta_\Delta$  and  $\theta_{cr} + \theta_\Delta$ , where  $\theta_\Delta = \Delta/T_g$  (Figure 2). The fragility index  $m$  increases as we go from the hydrogen-bonded liquids PG and EtOH, through the polar liquids 3-FA and PC to the

non-polar liquids Tol and *c*-Dec (Table 1). The relative melting temperature  $\theta_m$  is not correlated with  $m$ , and its average value is  $\theta_m \approx 1.5$  (Figure 2, red symbols). As we go from the hydrogen-bonded liquids toward 3-FA, PC, and Tol, the relative crossover temperature  $\theta_{cr}$  decreases toward  $\theta_m$ , but it increases again for the most fragile *c*-Dec (Figure 2, black symbols). The initial decrease of  $\theta_{cr}$  agrees with the previous finding<sup>12,13</sup> that some hydrogen-bonded liquids display higher values of  $\theta_A$  than the other molecular liquids, which generally have  $\theta_A \approx 1.4$ . On the other hand, the increase of  $\theta_{cr}$  for *c*-Dec is unexpected and will be discussed below. Another unexpected result is that the relative Arrhenius crossover temperature  $\theta_A$  in our study seems not to be correlated with  $m$  (Figure 2, blue symbols). Therefore, we displayed the data for  $\theta_A$  in molecular liquids from ref 25 (Figure 2, blue crosses). Despite data scattering, we can see that  $\theta_A$  from this study decreases with  $m$  reaching the value  $\theta_A \approx 1.4$  for the highest values of  $m$ . This correlation implies that seemingly uncorrelated behavior of  $\theta_A$  and  $m$  in our study results from the lack of experimental points. It seems that our values of  $\theta_A$  are a little bit higher than expected from the general trend of  $\theta_A$  against  $m$ , which could be the result of our viscosity fitting procedure. However, our values are within the range of data scattering in all studied liquids except in the highly fragile *c*-Dec, where  $\theta_A$  has an unexpectedly high value (Figure 2).

It is interesting to note that *c*-Dec, as one of the most fragile glass former of all, exhibits unexpectedly high values of  $\theta_{cr}$  and  $\theta_A$  (Figure 2). The results of neutron scattering measurements and molecular dynamics simulations indicate that molecular neighbor shells in *c*-Dec are much better defined than in a typical molecular glass former Cumene with a lower

fragility of  $m \approx 90$ .<sup>24</sup> Moreover, the level of definition of neighbor shells in *c*-Dec is as high as in metallic glass formers. Such unexpected short-range ordering in *c*-Dec could be the reason behind its high values of  $\theta_{cr}$  and  $\theta_A$ . Further investigations on this peculiar behavior of *c*-Dec are needed.

**Figure 2.** Relative characteristic temperatures  $\theta$  versus fragility index  $m$  for studied liquids. Symbols mark the crossover temperatures of radical diffusivity  $\theta_{cr} = T_{cr}/T_g$  (black), the Arrhenius crossover temperatures  $\theta_A = T_A/T_g$  from the viscosity fits (blue), and melting temperatures  $\theta_m = T_m/T_g$  (red). Error bars mark the crossover regions of radical diffusivity, which extend from  $\theta_{cr} - \theta_\Delta$  to  $\theta_{cr} + \theta_\Delta$ , where  $\theta_\Delta = \Delta/T_g$ . Blue crosses denote the data for  $\theta_A$  taken from ref 25.



Another interesting point is the already mentioned unusual behavior of EtOH, where  $T_{cr}$  is significantly higher than  $T_A$  (Table 1 and Figure 2). This could relate to the well-known fact that EtOH and other monohydroxy alcohols are inhomogeneous liquids, exhibiting mesoscale structure due to the supramolecular clusters of hydrogen-bonded hydroxyl groups.<sup>26,27</sup> The supramolecular clusters are manifested by the presence of pre-peak in addition to the main peak in diffraction spectra of monohydroxy alcohols. The pre-peak is clearly visible at room temperature in EtOH,<sup>26</sup> indicating that supramolecular clusters exist above  $T_{cr}$  and  $T_A$ . Also, the existence of supramolecular clusters in monohydroxy alcohols results in two relaxation processes in structural dynamics: a structural  $\alpha$ -relaxation, which is attributed to the dynamics of alkyl chains, and a slower Debye relaxation, which is attributed to dynamics of hydrogen-bonded supramolecular clusters.<sup>26,27</sup> Although Debye relaxation peak strongly contributes to dielectric spectra of monohydroxy alcohols and hinders the  $\alpha$ -relaxation peak, the analysis of the true  $\alpha$ -relaxation time in EtOH showed that it exhibits the Arrhenius crossover at 200 K,<sup>28</sup> which is equal to  $T_A$  from our viscosity analysis (Table 1). Because of the short alkyl chains in EtOH, the radical diffusion is possibly coupled to  $\alpha$ -relaxation governed by alkyl-chain dynamics and Debye relaxation governed by dynamics of hydroxyl groups. The effect of the latter coupling could be a shift of the diffusion crossover temperature  $T_{cr}$  to a higher value than  $T_A$ . However, further studies of tracer diffusion in various monohydroxy alcohols are needed to clarify this interesting question.

According to molecular dynamics simulations of glass-forming liquids,<sup>15,16</sup> the molecules that cooperatively participate in the collective diffusion process form string-like clusters

(strings). The string length  $n$ , defined as the number of participating molecules, was found to vary among different strings in very good accordance with the exponential law. This means that the normalized distribution of string lengths has the form  $f_n = (1/n_c)(1-1/n_c)^{n-1}$ , where  $n_c$  is the average string length. The probability that a molecule diffuses as a part of the string with length  $n$  is given by  $p_n = f_n n / n_c$ , which implies that the probability  $p_1$  in eq 3 and  $n_c$  are related as  $p_1 = n_c^{-2}$ . This relationship creates consistency between the observed increase of  $n_c$  upon cooling in simulations<sup>15,16</sup> and the decrease of  $p_1$  upon cooling obtained by fitting radical diffusivities to eq 3.

It was recognized that the nearly exponential distribution of string lengths, whose average length grows upon cooling, resembles the distribution of linear polymers formed by equilibrium polymerization upon cooling.<sup>15,16,29</sup> Therefore, several equilibrium polymerization models were used to reproduce the string forming of mobile particles in supercooled liquid.<sup>16,29,30</sup> In the most simple free polymerization model, the polymer chains of associated monomers are characterized by the growth and scission rate constants  $k_a$  and  $k_d$ , respectively. At the same time, the average chain length is given by  $n_c = 1/2 + (1/4 + \phi K_{eq})^{1/2}$ , where  $K_{eq} = k_a / k_d$  is the equilibrium constant for the polymerization reaction and  $\phi$  is the total concentration of monomers.<sup>30</sup> In the case of weak polymerization  $4\phi K_{eq} \ll 1$ , we get the following relation  $p_1 = n_c^{-2} \approx (1 + 2\phi K_{eq})^{-1}$ . This relation reproduces  $p_1$  from the fitting function in eq 3 under assumptions that  $\phi$  weakly depends on temperature, and  $K_{eq}$  follows the usual Arrhenius law, i.e.,  $K_{eq} \propto \exp[\Delta h / (k_B T)]$ , where  $\Delta h$  is the energy change for chain scission.<sup>16,29,30</sup>

We can conclude that qualitative agreement exists between the assumptions in our simple diffusion model and the behavior of strings in molecular dynamics simulations, which some polymerization models can reproduce. Since polymerization models explain the forming of strings and their behavior only in a phenomenological way without a deeper understanding of underlying mechanisms, we made no attempts to compare our model quantitatively with polymerization models. However, our model offers a link to experimental results for any future diffusion model that will be more physically based. Meanwhile, we expect that our simple diffusion model could be a valuable tool for future studies of tracer diffusion in liquids.

Along with the measurements of the translational diffusivity  $D_{trans}$  of tracer and host molecules, the measurements of their rotational diffusivity  $D_{rot}$  were found helpful in the studies of crossover phenomenon and heterogeneous dynamics below  $T_c \approx 1.2T_g$ .<sup>10,11,31</sup> Studies of molecular rotation revealed that the strong SE violation below  $T_c$  is accompanied by the so-called translation-rotation decoupling. This decoupling denotes a strong violation of the expected relation for  $D_{trans} / D_{rot}$  that combines the SE law for  $D_{trans}$  and the Stokes-Einstein-Debye (SED) law for  $D_{rot}$ . This result raises the question about the existence of similar decoupling for the crossover detected in our study, which could be answered in future studies by using various techniques to measure the translational and rotational diffusion of host and tracer molecules. In this context, we can mention that the NMR results for host water molecules and the ESR results for radical tracer molecules indicate translation-rotation decoupling for both molecules close to  $T_m$  in the water.<sup>18</sup> Also, we expect that the size-dependent experiments of translational and rotational tracer diffusion, which were applied to study crossover phenomenon and

heterogeneous dynamics below  $T_c$ ,<sup>10,11,31</sup> could be applied to study the crossover detected in our study.

In summary, we applied the ESR method to obtain the diffusivity of the pDTEMPONE radical at different temperatures in six glass-forming liquids. By comparing the obtained radical diffusivities with the self-diffusivities in all liquids, we checked the theoretical predictions according to which the radical diffusivities should be lower than the self-diffusivities by a constant factor. We found that the predictions are valid only at the highest measured temperatures, while the values of radical diffusivities reach those of self-diffusivities with lowering the temperature. We propose that this crossover behavior of radical diffusivity evidences an increasing number of participating molecules in the diffusion process with temperature lowering. In the theoretical treatment of the crossover phenomenon, we assumed that the diffusivities of both radical and solvent molecules could be separated into contributions from the single-molecule and collective diffusion processes. We defined a simplified diffusion model, where the single-molecule part of radical diffusivity is lower by a constant factor than that of self-diffusivity, while collective parts of the radical and self-diffusivities are the same. In order to quantify the crossover phenomenon, we additionally assumed that the probabilities for the solvent molecule to diffuse in single-molecule or collective processes are interrelated as in the simple two-state system. Thus, we constructed the fitting function for radical diffusivity with temperature parameters  $T_{cr}$  and  $2\Delta$ , defining the crossover position and its width, respectively. After fitting the experimental radical diffusivities to this function for all liquids, we compared the resulting temperature parameters with the Arrhenius crossover temperatures  $T_A$  obtained by

fitting experimental viscosity data from the literature. The estimated values of  $T_A$  were found to be close to the onset temperatures of the radical diffusion crossover  $T_{cr} + \Delta$  in all studied liquids except ethanol, which suggests that the two crossover phenomena could have the same origin. This origin is very likely the onset of collective behavior of molecular rearrangement upon cooling.

According to the previous studies,<sup>12,13,25</sup> the relative Arrhenius crossover temperature  $\theta_A = T_A/T_g$  in glass-forming liquids decreases toward  $\theta_m = T_m/T_g$  as their fragility index  $m$  increases. Despite a small number of liquids studied here, we found that the relative crossover temperature  $\theta_{cr} = T_{cr}/T_g$  generally follows this trend with the exception of *cis*-decalin. To fully establish a correlation between  $\theta_{cr}$  and  $m$ , further studies of  $\theta_{cr}$  in more glass-forming liquids are needed. We noted that the most fragile *cis*-decalin exhibits relatively high values of  $\theta_{cr}$  and  $\theta_A$ , which was tentatively attributed to its unexpectedly high short-range order of molecular neighbor shells.<sup>24</sup> Finally, we showed a general agreement between our simplified treatment of the radical diffusion crossover and the studies of the string-like clusters of diffusing molecules that were detected in molecular dynamics simulations of glass-forming liquids.<sup>15,16,29,30</sup>

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## Supporting Information

Analysis of self-diffusivity data (SI1), list of molecular properties of materials (SI2), description of ESR method for measuring radical diffusivity (SI3), and estimation of Arrhenius crossover temperatures from viscosities (SI4).

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