

Measurements of π^\pm , K^\pm , p and \bar{p} spectra in proton-proton interactions at 20, 31, 40, 80 and 158 GeV/c with the NA61/SHINE spectrometer at the CERN SPS

NA61/SHINE Collaboration

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Abstract Measurements of inclusive spectra and mean multiplicities of π^\pm , K^\pm , p and \bar{p} produced in inelastic $p + p$ interactions at incident projectile momenta of 20, 31, 40, 80 and 158 GeV/ c ($\sqrt{s} = 6.3, 7.7, 8.8, 12.3$ and 17.3 GeV, respectively) were performed at the CERN Super Proton Synchrotron using the large acceptance NA61/SHINE hadron spectrometer. Spectra are presented as function of rapidity and transverse momentum and are compared to predictions of current models. The measurements serve as the baseline in the NA61/SHINE study of the properties of the onset of deconfinement and search for the critical point of strongly interacting matter.

1 Introduction

This paper presents experimental results on inclusive spectra and mean multiplicities of π^\pm , K^\pm , p and \bar{p} produced in inelastic $p + p$ interactions at 20, 31, 40, 80 and 158 GeV/ c . The measurements were performed by the multi-purpose NA61/SHINE experiment [1,2] at the CERN Super Proton Synchrotron (SPS). The new measurements complement previously published results from the same datasets on π^- production [3] obtained without particle identification as well as on fluctuations of charged particles [4]. These studies form part of the NA61/SHINE strong interaction programme investigating the properties of the onset of deconfinement and searching for the critical point of strongly interacting matter. The programme is mainly motivated by the observation of rapid changes of hadron production properties in central Pb + Pb collisions at about 30A GeV/ c by the NA49 experiment [5,6] which were interpreted as the onset of deconfinement. These findings were recently confirmed by the RHIC beam energy programme [7] and the interpretation is supported by the LHC results (see Ref. [8] and references therein). Clearly, a two dimensional scan in collision energy and size of colliding nuclei is required to explore systematically the phase diagram of strongly interacting matter [9].

Pursuing this programme NA61/SHINE already recorded data on $p + p$, Be + Be, Ar + Sc and $p + pb$ collisions and data taking on Xe + La collisions is scheduled for 2017. Moreover, measurements of Pb + Pb interactions are planned for the coming years [10].

An interpretation of the rich experimental results on nucleus–nucleus collisions relies to a large extent on a comparison to the corresponding data on $p + p$ and $p + A$ interactions. However, the published measurements mainly refer to basic features of unidentified charged hadron production and are sparse. Results on identified hadron spectra, fluctuations and correlations are mostly missing. Detailed measurements of hadron spectra in a large acceptance in the beam momentum range covered by the data in this paper exist only from the NA49 experiment for inelastic $p + p$ interactions at 158 GeV/ c [11–13]. Thus new high precision measurements of hadron production properties in $p + p$ and $p + A$ interactions are essential. They are performed by NA61/SHINE in parallel with the corresponding measurements on nucleus–nucleus collisions using the same detector and thus covering the same acceptance. Precise data on pion, kaon and proton production properties are crucial for constraining basic properties of models of strong interactions.

This publication presents two-dimensional spectra of positively and negatively charged pions, kaons, protons and antiprotons produced in $p + p$ interactions in the SPS momentum range (20, 31, 40, 80, 158 GeV/ c). The paper is organized as follows: after this introduction the experiment is briefly described in Sect. 2. The analysis procedure is discussed in Sect. 3. Section 4 presents the results of the analysis. In Sect. 5 model calculations are compared to the new measurements. A summary in Sect. 6 closes the paper.

The following variables and definitions are used in this paper. The particle rapidity is calculated in the collision center of mass system (cms), $y = a \tanh(\beta_L)$, where $\beta_L = cp_L/E$ is the longitudinal component of the velocity and p_L and E are the longitudinal momentum and energy given in the cms. The transverse component of the momentum is denoted as p_T and the transverse mass m_T is defined as $m_T = \sqrt{m^2 + (cp_T)^2}$, where m is the particle mass in GeV. The momentum in the laboratory frame is denoted p_{lab} and electric charge in units of the electron charge as q . The collision energy per nucleon pair in the center of mass system is denoted as $\sqrt{s_{NN}}$.

2 NA61/SHINE experiment

NA61/SHINE is a fixed target experiment employing a large acceptance hadron spectrometer situated in the North Area

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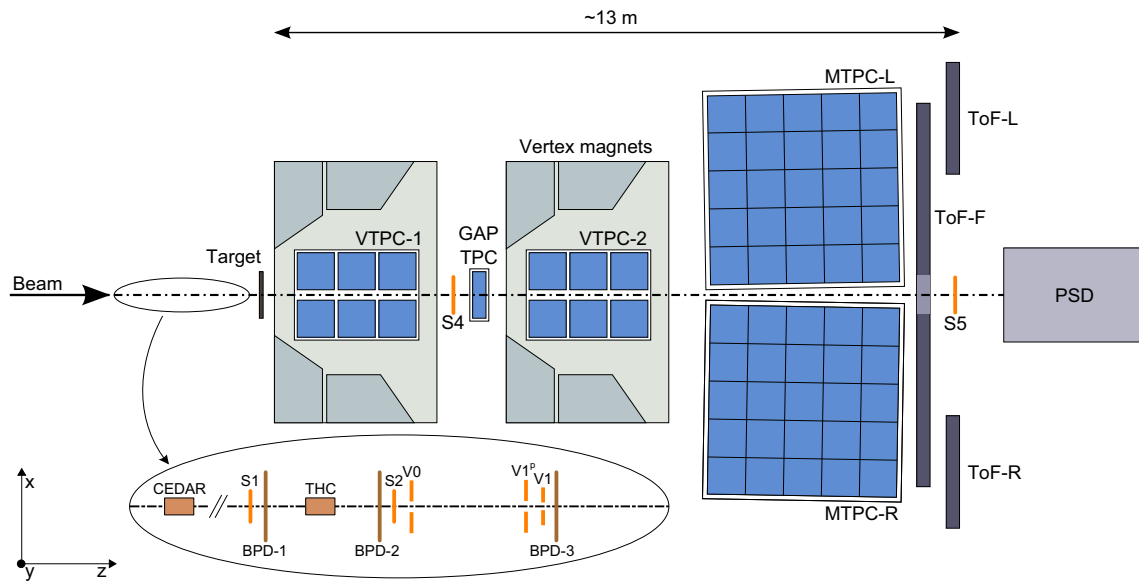


Fig. 1 The schematic layout of the NA61/SHINE experiment at the CERN SPS (horizontal cut, not to scale). Alignment of the NA61/SHINE coordinate system is shown on the plot. The nominal beam

direction is along the z axis. The magnetic field bends charged particle trajectories in the $x-z$ plane. The electron drift direction in the TPCs is along the y (vertical) axis

Table 1 Basic beam properties and number of events recorded for $p + p$ interactions at incident proton momentum of 20, 31, 40, 80 and 158 GeV/c

p_{beam} (GeV/c)	\sqrt{s} (GeV)	Particles per spill $\times 10^3$	Proton fraction (%)	Number of recorded events
20	6.2	1000	12	1.3×10^6
31	7.7	1000	14	3.1×10^6
40	8.8	1200	14	5.2×10^6
80	12.3	460	28	4.3×10^6
158	17.3	250	58	3.5×10^6

H2 beam-line of the CERN SPS [1]. A schematic layout is shown in Fig. 1. The main components of the detection system used in the analysis are four large volume time projection chambers (TPC). Two of them, called vertex TPCs (VTPC), are located downstream of the target inside superconducting magnets with maximum combined bending power of 9 Tm. The TPCs are filled with Ar:CO₂ gas mixtures in proportions 90:10 for the VTPCs and 95:5 for the Main TPCs. The MTPCs and two walls of pixel time-of-flight (ToF-L/R) detectors are placed symmetrically to the beamline downstream of the magnets. A GAP-TPC (GTPC) between VTPC-1 and VTPC-2 improves the acceptance for high-momentum forward-going tracks.

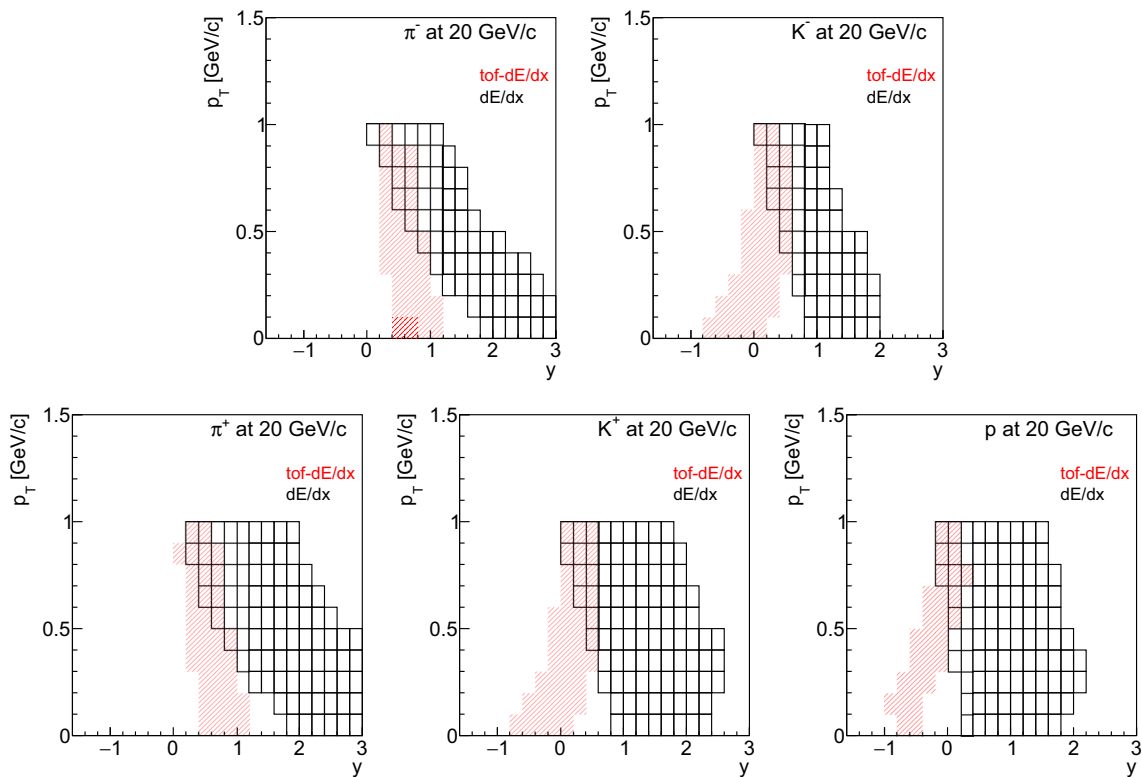
Individual beam particles are identified and precisely measured by a set of scintillation and Cherenkov counters, as well as three beam position detectors (BPDs) placed upstream of the target [1]. Secondary beams of positively charged hadrons at momenta of 20, 31, 40, 80 and 158 GeV/c were used to collect the data for the analysis presented in this paper. These beams were produced from 400 GeV/c pro-

tons extracted from the SPS in a slow extraction mode with a flat-top of 10 seconds. Protons from the secondary hadron beam are identified by two Cherenkov counters, a CEDAR [14] (either CEDAR-W or CEDAR-N) and a threshold counter (THC). A selection based on signals from the Cherenkov counters allowed to identify beam protons with a purity of about 99% [15]. The proton contamination in the secondary beam The beam momentum and intensity was adjusted by proper setting of the H2 beamline magnets and collimators. The precision of the setting of the beam magnet currents is approximately 0.5%. The beam momentum was verified by a direct measurement at 31 GeV/c by bending the incoming beam particles into the TPCs with the maximum magnetic field. The properties of the beams used for obtaining the analysed data are summarized in Table 1.

A liquid hydrogen target (LHT) of 20.29 cm length (2.8% interaction length) and 3 cm diameter was placed 88.4 cm upstream of VTPC-1. Data were taken with full (denoted as target inserted, I) and empty (denoted as target removed, R)

Table 2 Statistics of events and tracks used in dE/dx and $tof-dE/dx$ identification methods for target inserted and removed configurations. Events with removed target were used to evaluate corrections for off-target interactions

Momentum (GeV/c)	Number of events	Number of tracks (dE/dx method)	Number of tracks ($tof-dE/dx$ method)
Target inserted			
20	234,758	244,813	17,023
31	832,608	859,573	44,228
40	1,604,483	1,625,595	199,775
80	1,591,076	1,592,538	214,316
158	1,625,578	4,464,269	158,520
Target removed			
20	3184	2175	402
31	12,618	10,080	691
40	42,115	39,893	4745
80	51,588	38,132	8003
158	26,837	41,234	3373

**Fig. 2** Acceptance of the $tof-dE/dx$ and dE/dx methods for identification of pions, kaons and protons in $p + p$ interactions at 20 GeV/c

LHT. The event statistics collected in the two configurations are summarised in Table 2.

Interactions in the target are selected with the trigger system by requiring an incoming beam proton and no signal from S4, a small 2 cm diameter scintillation counter placed on the beam trajectory between the two vertex magnets. This minimum bias trigger is based on the disappearance of the beam proton downstream of the target.

3 Analysis procedure

This section starts with a brief overview of the data analysis procedure and the applied corrections. It also defines to which class of particles the final results correspond. A description of the calibration and the track and vertex reconstruction procedure can be found in Ref. [3].

The analysis procedure consists of the following steps:

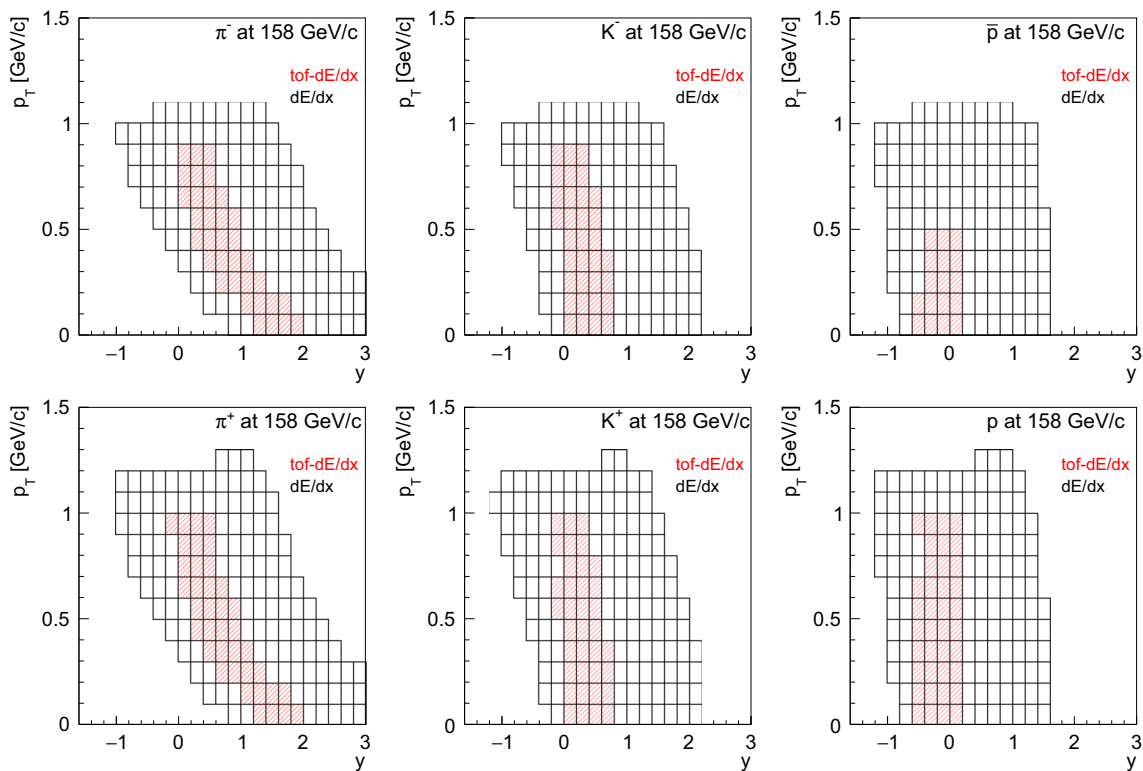
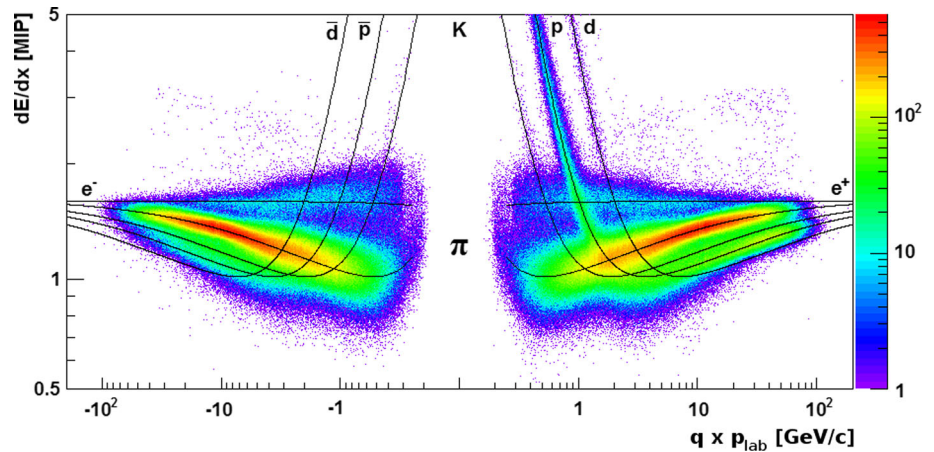


Fig. 3 Acceptance of the *tof-dE/dx* and *dE/dx* methods for identification of pions, kaons and protons in *p + p* interactions at 158 GeV/c

Fig. 4 Distribution of charged particles in the *dE/dx-q × p_{lab}* plane. The energy loss in the TPCs for different charged particles for events and tracks selected for the analysis of *p + p* interactions at 80 GeV/c (the target inserted configuration). Expectations for the dependence of the mean *dE/dx* on *p_{lab}* for the considered particle types are shown by the curves calculated based on the Bethe–Bloch function



- (i) application of event and track selection criteria,
 - (ii) determination of spectra of identified hadrons using the selected events and tracks,
 - (iii) evaluation of corrections to the spectra based on experimental data and simulations,
 - (iv) calculation of the corrected spectra and mean multiplicities,
 - (v) calculation of statistical and systematic uncertainties.
- (ii) contribution from off-target interactions,
 - (iii) contribution of particles other than *primary* (see below) hadrons produced in inelastic *p + p* interactions,
 - (iv) losses of inelastic *p + p* interactions due to the trigger and the event and track selection criteria employed in the analysis as well as losses of produced hadrons in accepted interactions due to their decays and secondary interactions.

Corrections for the following biases were evaluated and applied:

- (i) geometrical acceptance,

The final results refer to identified hadrons produced in inelastic *p + p* interactions by strong interaction processes

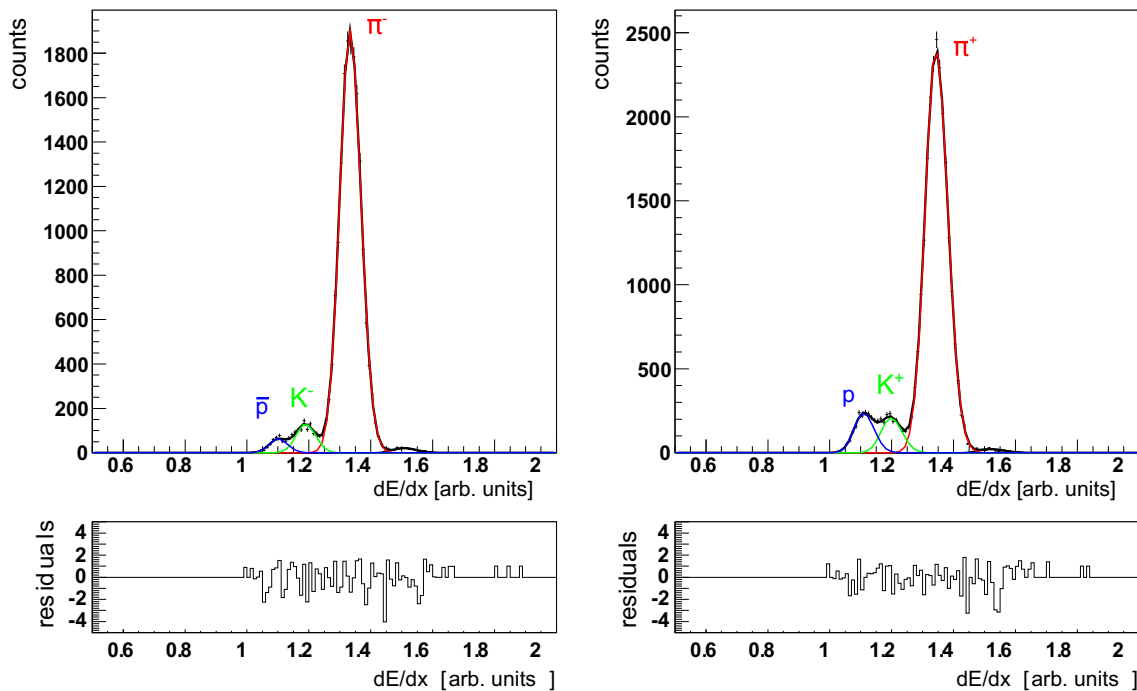


Fig. 5 The dE/dx distributions for negatively (*top-left*) and positively (*top-right*) charged particles in the bin $12.6 < p_{\text{lab}} \leq 15.8$ GeV/c and $0.2 < p_T \leq 0.3$ GeV/c produced in p + p interactions at 158 GeV/c. The fit by a sum of contributions from different particle types is shown

by solid lines. The corresponding residuals (the difference between the data and fit divided by the statistical uncertainty of the data) is shown in the bottom plots

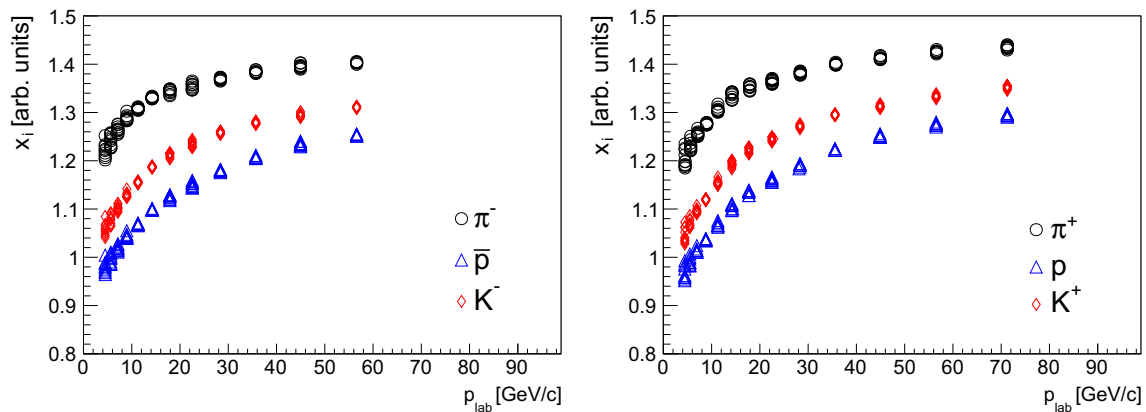


Fig. 6 Fitted peak positions in p + p interactions at 158 GeV/c for different particles as a function of p_{lab} . Different points at the same value of p_{lab} correspond to different transverse momentum bins

and in electromagnetic decays of produced hadrons. Such hadrons are referred to as *primary* hadrons.

The analysis was performed independently in (y, p_T) bins. The bin sizes were selected taking into account the statistical uncertainties and the resolution of the momentum reconstruction [3]. Corrections as well as statistical and systematic uncertainties were calculated for each bin.

3.1 Event and track selection

3.1.1 Event selection

Inelastic p + p events were selected using the following criteria:

- (i) no off-time beam particle detected within a time window of $\pm 2 \mu\text{s}$ around the trigger particle,

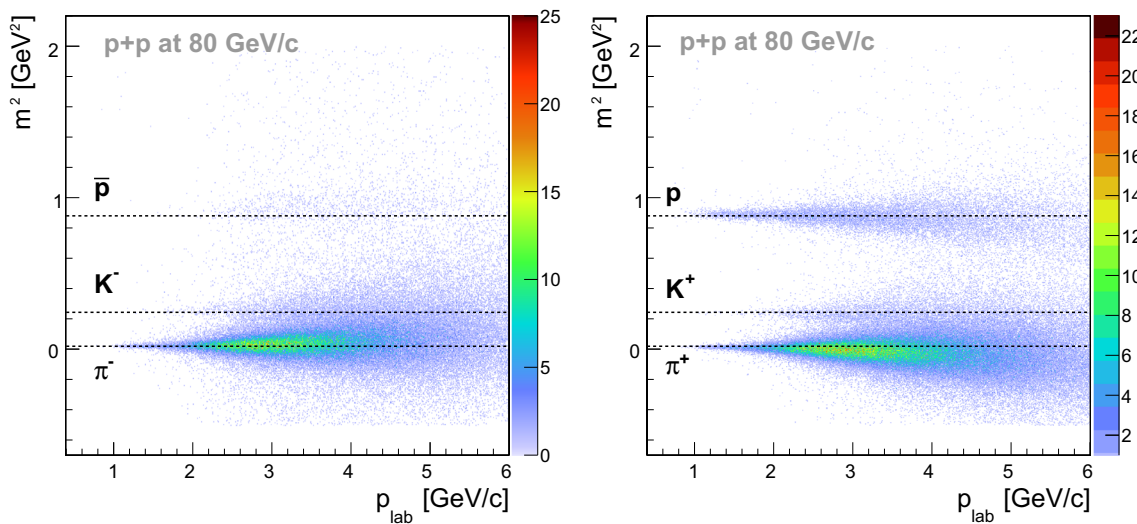
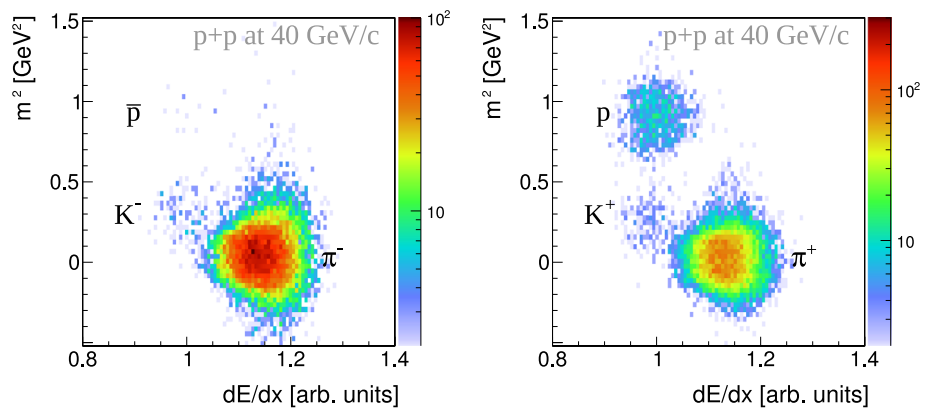


Fig. 7 Mass squared versus momentum measured by ToF-R (*left*) and ToF-L (*right*) detectors for particles produced in $p + p$ interactions at 80 GeV/c. The lines show the expected mass squared values for different hadrons

Fig. 8 Particle number distribution in the m^2 - dE/dx plane for negatively (*left*) and positively (*right*) hadrons with momenta close to 4 GeV/c for $p + p$ interactions at 40 GeV/c. Electrons are not visible since their dE/dx values are beyond the dE/dx plot range



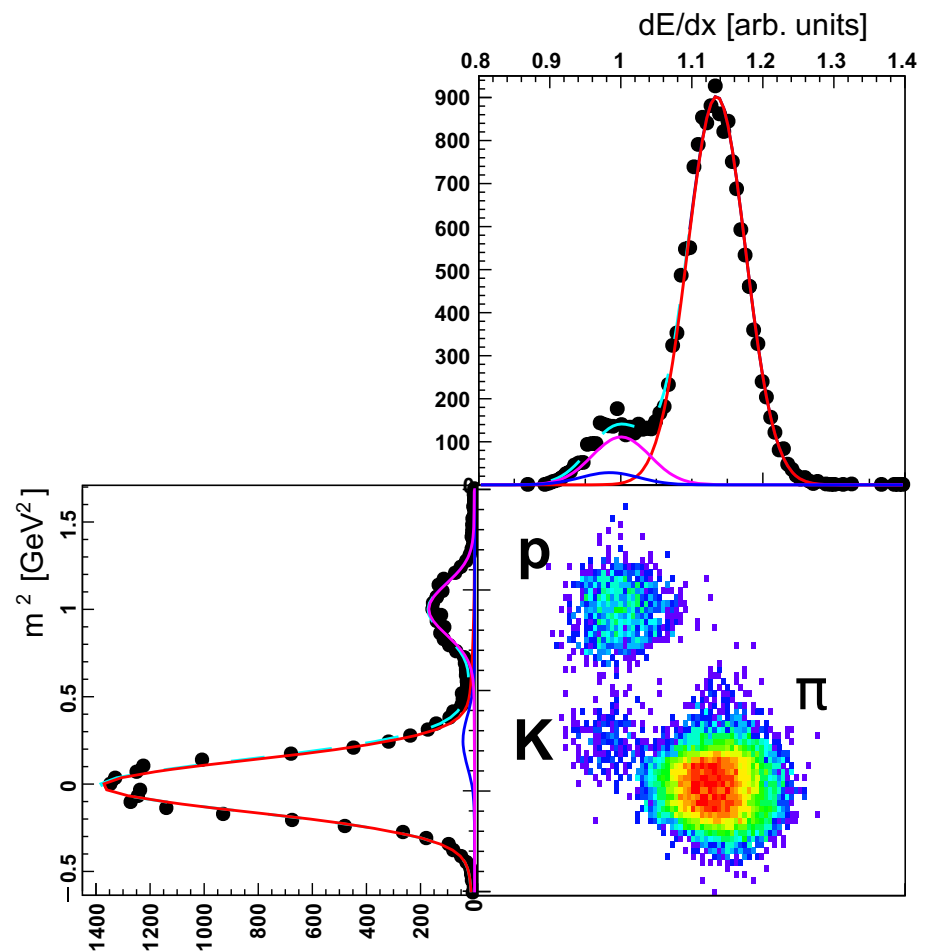
- (ii) beam particle trajectory measured in at least three planes out of four of BPD-1 and BPD-2 and in both planes of BPD-3,
- (iii) at least one track reconstructed in the TPCs and fitted to the interaction vertex,
- (iv) z position of the interaction vertex (fitted using the beam trajectory and TPC tracks) not farther away than 20 cm from the center of the LHT,
- (v) events with a single, positively charged track with absolute momentum close to the beam momentum (see [3]) are removed in order to eliminate elastic scattering reactions.

3.1.2 Track selection

In order to select tracks of primary charged hadrons and to reduce the contamination of tracks from secondary interactions, weak decays and off-time interactions, the following track selection criteria were applied:

- (i) track momentum fit at the interaction vertex should have converged,
- (ii) fitted x component of particle rigidity ($p_{lab,x}/q$) is positive. This selection minimizes the angle between the track trajectory and the TPC pad direction for the chosen magnetic field direction, reducing uncertainties of the reconstructed cluster position, energy deposition and track parameters,
- (iii) total number of reconstructed points on the track should be greater than 30,
- (iv) sum of the number of reconstructed points in VTPC-1 and VTPC-2 should be greater than 15 or the number of reconstructed points in the GAP-TPC should be greater than 4,
- (v) the distance between the track extrapolated to the interaction plane and the interaction point (impact parameter) should be smaller than 4 cm in the horizontal (bending) plane and 2 cm in the vertical (drift) plane,
- (vi) the total number of reconstructed dE/dx points on the track should be greater than 30,

Fig. 9 Example of the tof - dE/dx fit (Eq. (4)) obtained in a single phase-space bin ($3 < p_{lab} < 4$ GeV/ c and $0.2 < p_T < 0.3$ GeV/ c) for positively charged particles in $p + p$ interactions at 158 GeV/ c . Lines show projections of obtained fits for pions (red), kaons (blue) and protons (magenta)



(vii) in case of tof - dE/dx identification, three additional selection criteria were used:

- (i) the hit in the ToF pixel should be matched only with one TPC track,
- (ii) proper measurement of the hit in charge to digital converter (QDC) and time to digital converter (TDC)
- (iii) the last point of the track should be in the last 2 padrows of the MTPC to ensure good matching with the ToF hit.

The event and track statistics after applying the selection criteria are summarized in Table 2.

3.2 Identification techniques

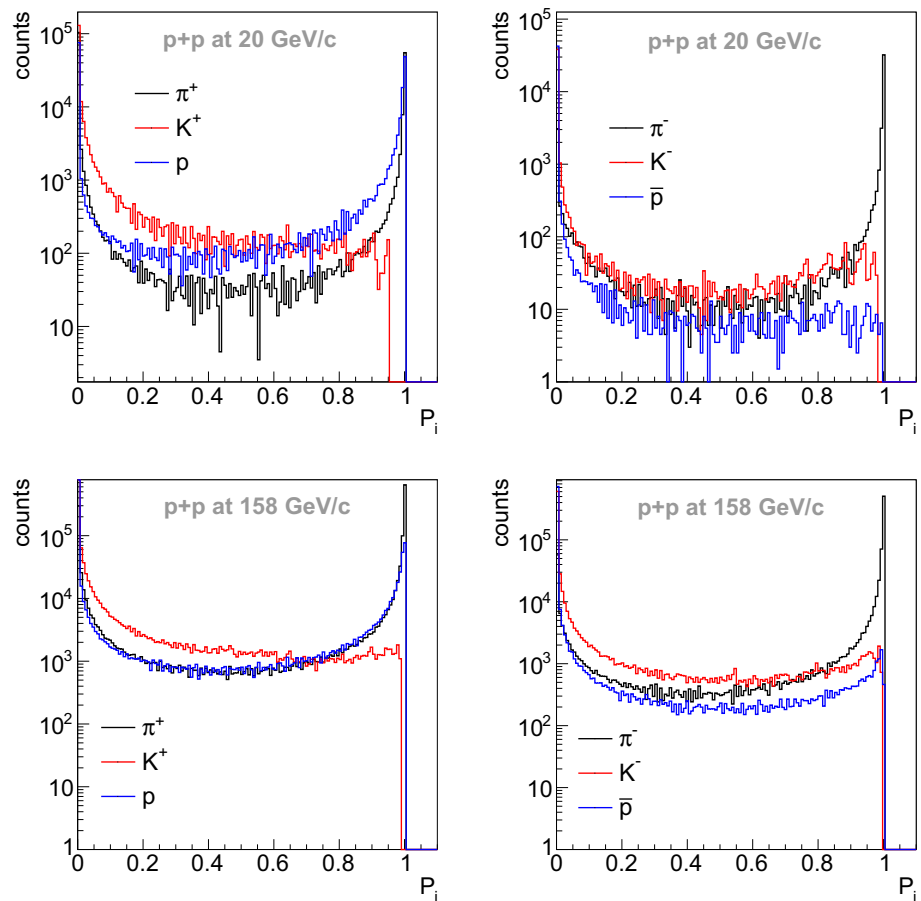
Charged particle identification in the NA61/SHINE experiment is based on the measurement of the ionization energy loss dE/dx in the gas of the TPCs and of the time of flight tof obtained from the ToF-L and ToF-R walls. In the region of the relativistic rise of the ionization at large momenta the measurement of dE/dx alone allows identification. At lower

momenta the dE/dx bands for different particle species overlap and additional measurement of tof is required to remove the ambiguity. These two methods allow to cover most of the phase space in rapidity and transverse momentum which is of interest for the strong interaction program of NA61/SHINE. The acceptance of the two methods is shown in Figs. 2 and 3 for $p + p$ interactions at 20 and 158 GeV/ c , respectively. At low beam energies the tof - dE/dx method extends the identification acceptance, while at top SPS energy it overlaps with the dE/dx method.

3.2.1 Identification based on energy loss measurement (dE/dx)

Time projection chambers can provide measurements of energy loss dE/dx of charged particles in the chamber gas along their trajectories. Simultaneous measurements of dE/dx and p_{lab} allow to extract information on particle mass. Here dE/dx is calculated as the truncated mean (smallest 50%) of cluster charges measured along a track trajectory. As an example, dE/dx measured in $p + p$ interactions at 80 GeV/ c , for positively and negatively charged particles, as a function

Fig. 10 Probability of a track being a pion, kaon, proton for positively (left panels) and negatively (right panels) charged tracks from dE/dx measurements in $p + p$ interactions at 20 and 158 GeV/c



of $q \times p_{lab}$ is presented in Fig. 4. The expected values of dE/dx are shown by the Bethe–Bloch curves.

The contributions of e^+ , e^- , π^+ , π^- , K^+ , K^- , p and \bar{p} are obtained by fitting the dE/dx distributions separately for positively and negatively charged particles in bins of p_{lab} and p_T with a sum of four functions [16, 17] each corresponding to the expected dE/dx distribution for a given particle type.

In order to ensure similar particle multiplicities in each bin, 20 logarithmic bins are chosen in p_{lab} in the range 1–100 GeV/c to cover the full detector acceptance. Furthermore the data are binned in 20 equal p_T intervals in the range 0–2 GeV/c.

The dE/dx fits consider four particle types ($i = p, K, \pi, e$). The signal shape for a given particle type is parametrised as the sum of asymmetric Gaussians with widths $\sigma_{i,l}$ depending on the particle type i and the number of points l measured in the TPCs. Simplifying the notation in the fit formulae, the peak position of the dE/dx distribution for particle type i is denoted as x_i . The contribution of a reconstructed particle track to the fit function reads:

$$\begin{aligned} \rho(x) &= \sum_i \rho_i(x) \\ &= \sum_{i=\pi,p,K,e} A_i \frac{1}{\sum_l n_l} \sum_l \frac{n_l}{\sqrt{2\pi}\sigma_l} \exp \\ &\quad \times \left[-\frac{1}{2} \left(\frac{x - x_i}{(1 \pm \delta)\sigma_l} \right)^2 \right], \end{aligned} \tag{1}$$

where x is the dE/dx of the particle, n_l is the number of tracks with number of points l in the sample and A_i is the amplitude of the contribution of particles of type i . The second sum is the weighted average of the line-shapes from the different numbers of measured points (proportional to track-length) in the sample. The quantity σ_l is written as:

$$\sigma_l = \sigma_0 \left(\frac{x_i}{x_\pi} \right)^{0.625} / \sqrt{n_l}, \tag{2}$$

where the width parameter σ_0 is assumed to be common for all particle types and bins. A $1/\sqrt{l}$ dependence on number

Fig. 11 Probability of a track being a pion, kaon, proton for positively (left panels) and negatively (right panels) charged tracks from *tof-dE/dx* measurements in p + p interactions at 20 and 158 GeV/c

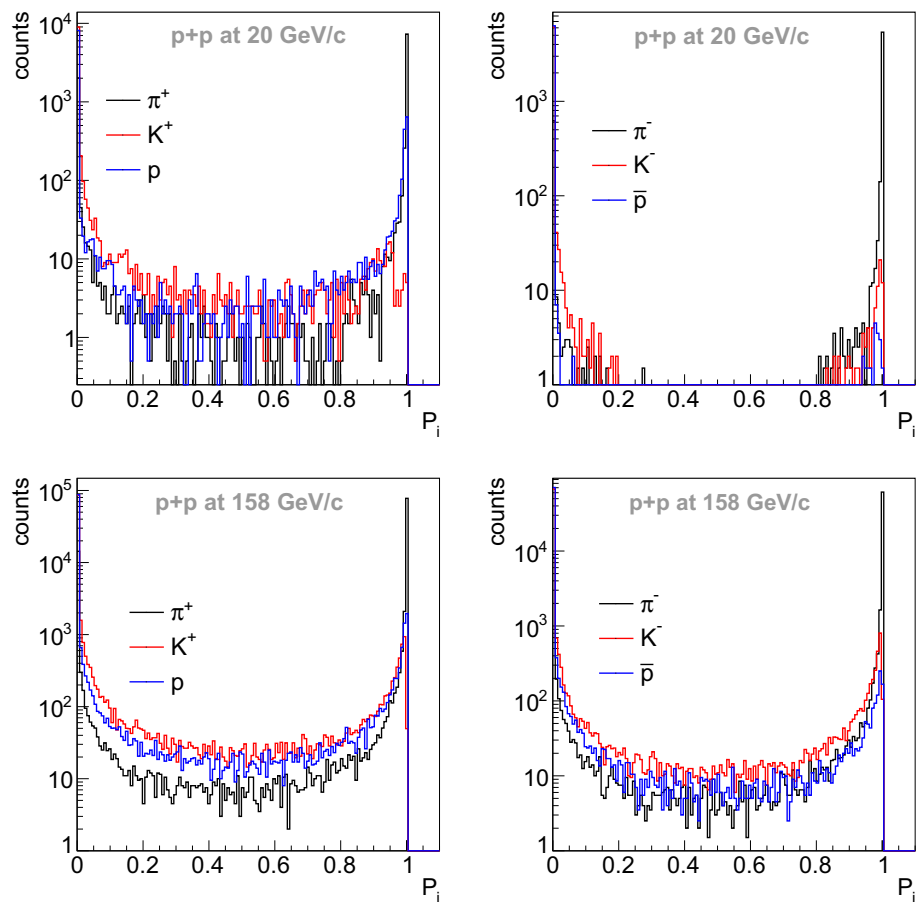


Table 3 Measured fraction of out-of-target events in recorded p + p interactions at SPS energies

Beam momentum (GeV/c)	Fraction of target removed events (%)
20	20.22
31	26.17
40	15.84
80	12.53
158	9.62

of points is assumed. The Gaussian peaks are allowed to be asymmetric (parameter δ added/subtracted above/below the peak x_i) to describe the tail of the Landau distribution which may still be present after truncation.

The fit function has 10 parameters (4 amplitudes, 4 peak positions, width and asymmetry) which are very difficult to fit in each bin independently. Therefore the following simplifications were adopted:

- (i) relative positions of electrons, kaons and protons to pions were assumed to be p_T -independent,

- (ii) in the analysed data, the asymmetry parameter δ is smaller than 0.001 and thus was fixed to zero,
- (iii) the fitted amplitudes were required to be greater than or equal to 0,
- (iv) the electron amplitude was set to zero for total momentum $p_{lab} > 23.4$ GeV/c (i.e. starting from the 13th bin), as the electron contribution vanishes at high p_{lab} ,
- (v) if possible, the relative position of the positive kaon peak was taken to be the same as that of negative kaons determined from the negatively charged particles in the bin of the same p_{lab} and p_T . This procedure helps to overcome the problem of the large overlap between K^+ and protons in the dE/dx distributions.

The simplifications reduce the number of independently fitted parameters in each bin from 10 to 6, i.e. the amplitudes of the four particle types, the pion peak position and the width parameter σ_0 .

Examples of fits are shown in Fig. 5 and the values of the fitted peak positions x_i are plotted in Fig. 6 versus momentum for different particle types i in p + p interactions at 158 GeV/c. As expected, the values of x_i increase with p_{lab} but do not depend on p_T .

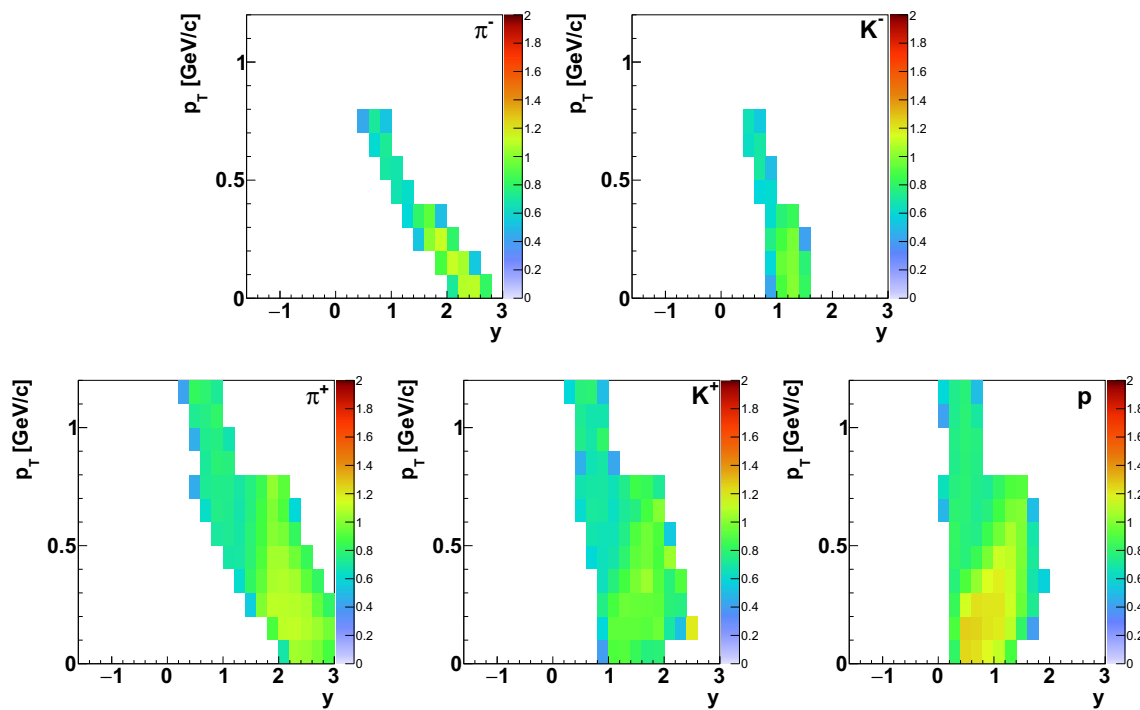


Fig. 12 Correction factors C_i^{-1} for the dE/dx identification method for positively and negatively charged pions, kaons and protons in $p + p$ interactions at 20 GeV/c. The correction factor for antiprotons produced in inelastic $p + p$ interactions is not presented due to insufficient statistics

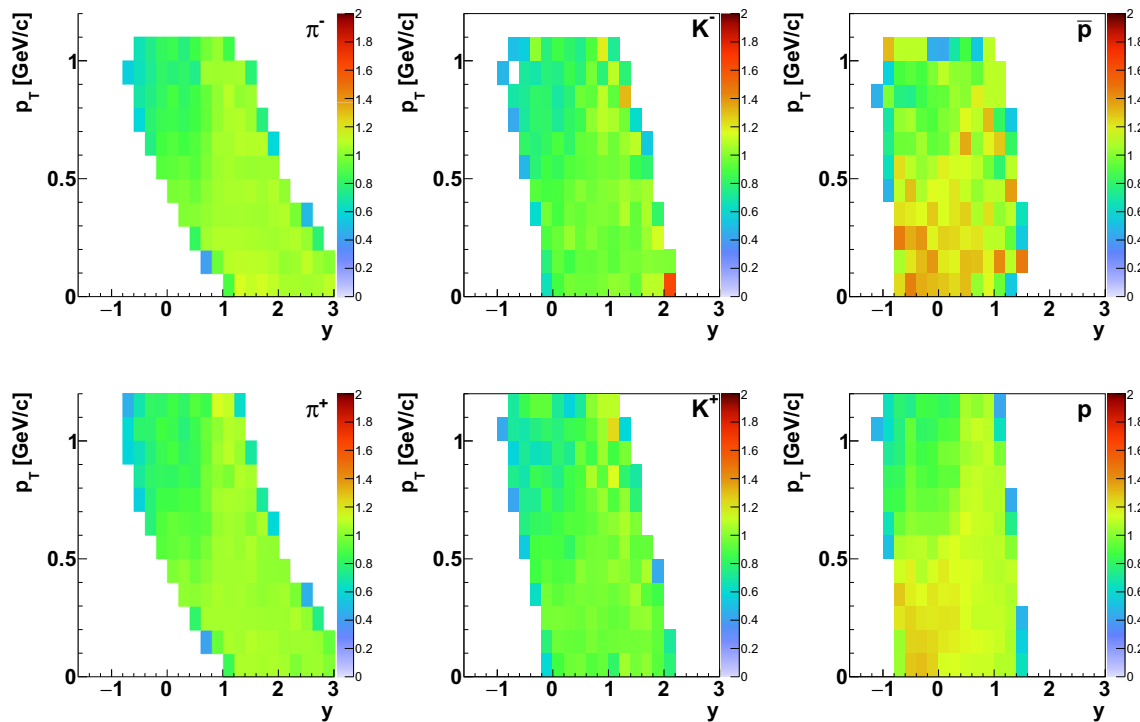


Fig. 13 Correction factors C_i^{-1} for the dE/dx identification method for positively and negatively charged pions, kaons and protons in $p + p$ interactions at 158 GeV/c

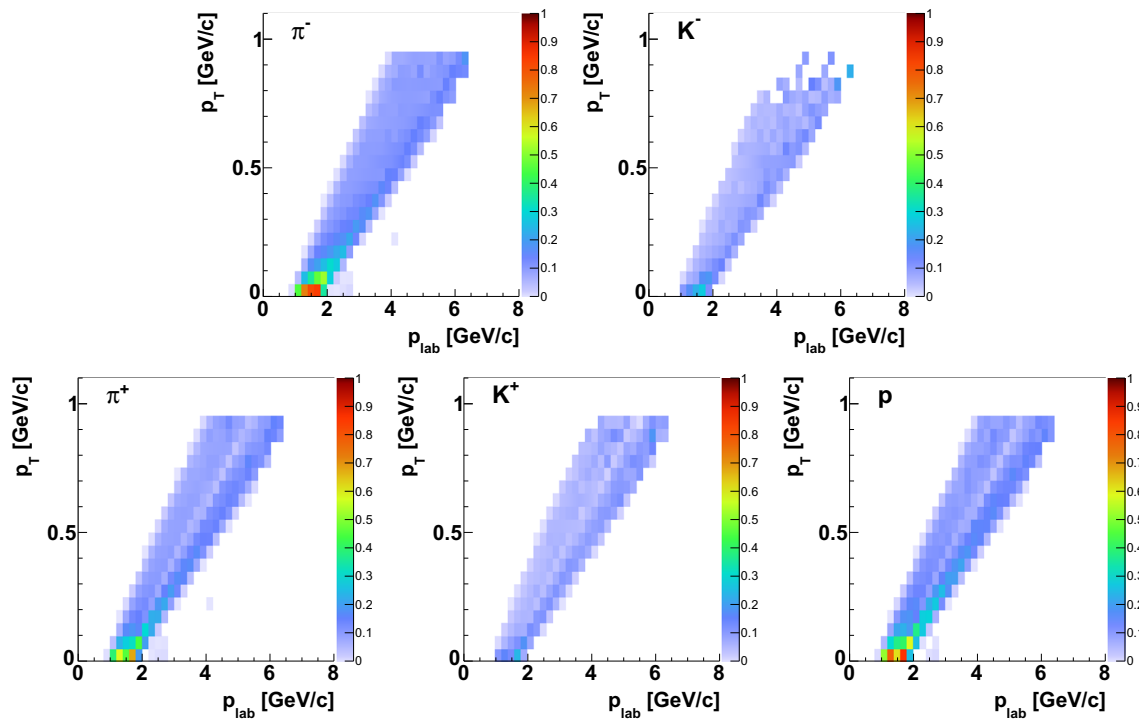


Fig. 14 Efficiencies C_i^{tof} for the $tof-dE/dx$ identification method for positively and negatively charged pions, kaons and protons for $p + p$ interactions at 20 GeV/c

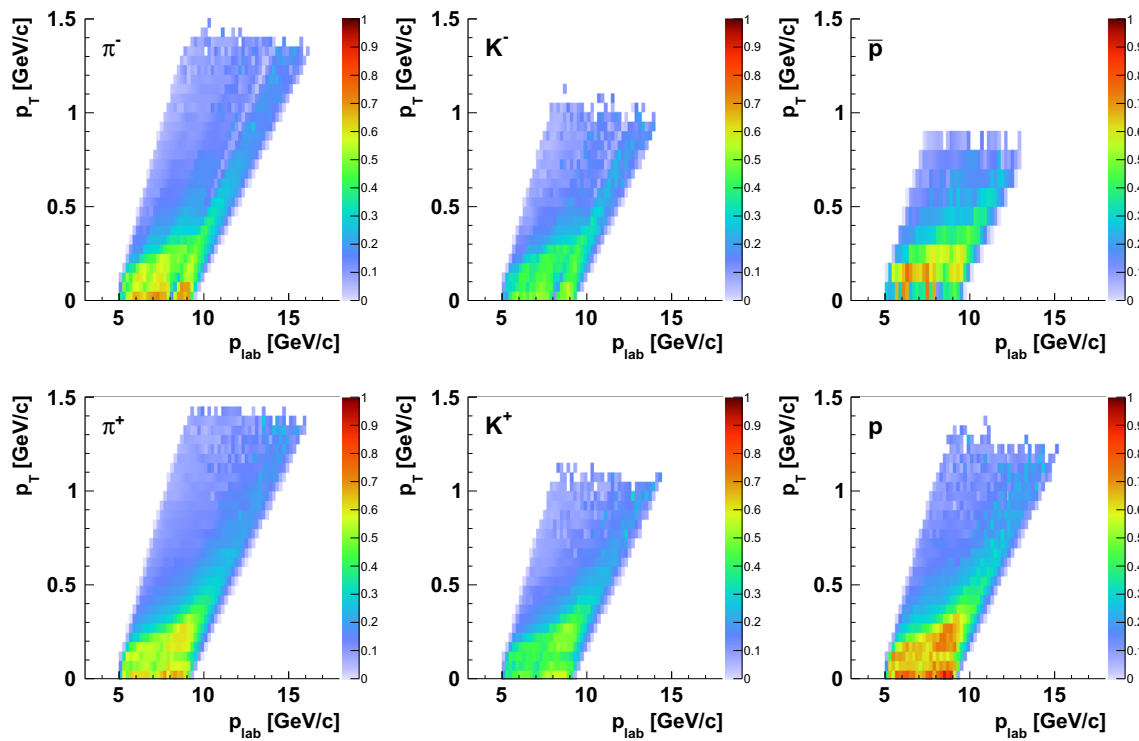
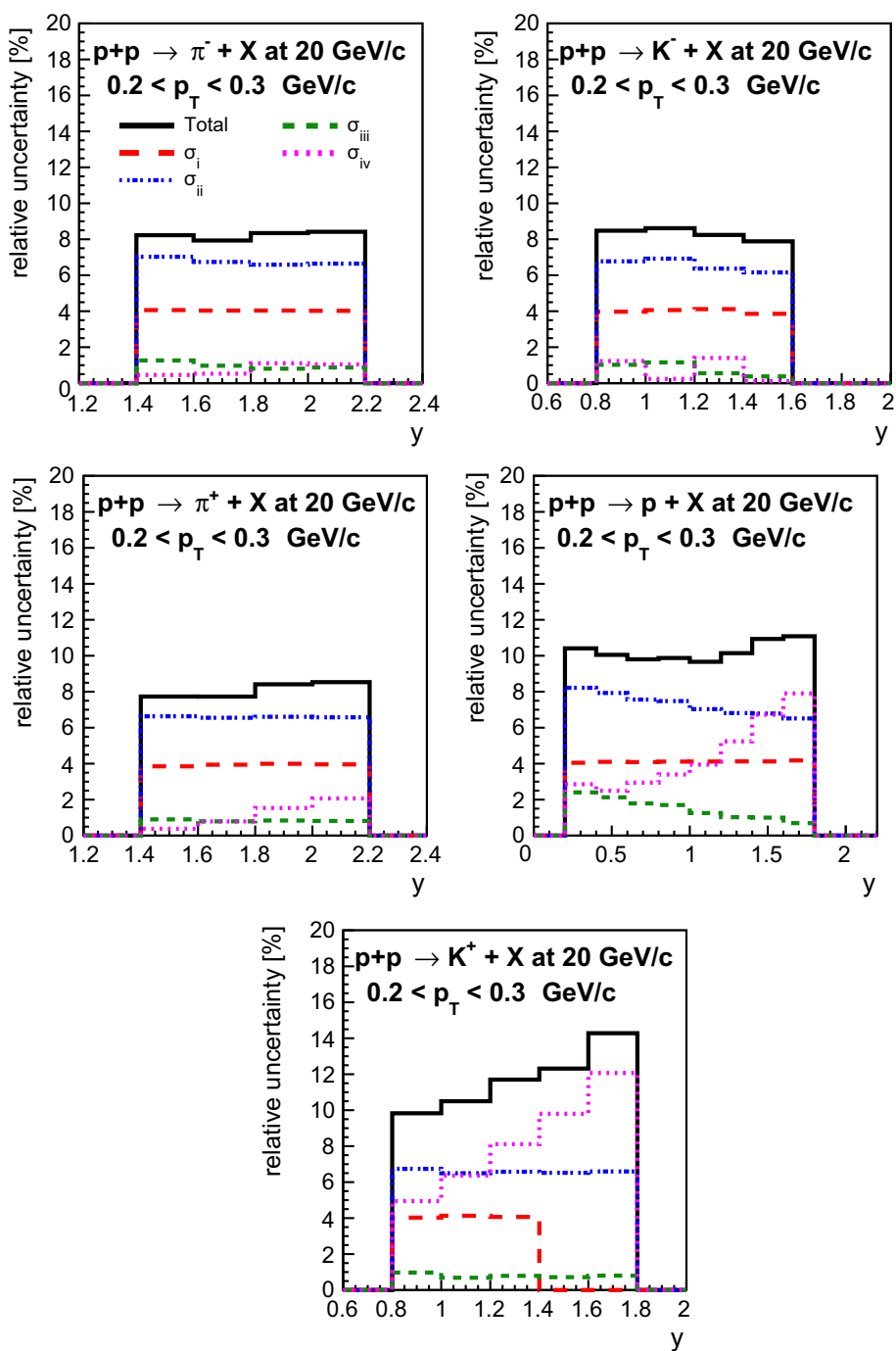


Fig. 15 Efficiencies C_i^{tof} for the $tof-dE/dx$ identification method for positively and negatively charged pions, kaons and protons for $p + p$ interactions at 158 GeV/c

Fig. 16 Components of systematic uncertainty of particle spectra obtained from the dE/dx method in inelastic $p + p$ interaction at 20 GeV/c as function of rapidity for the transverse momentum interval between 0.2–0.3 GeV/c. σ_i refers to acceptance of events with off-time beam tracks, σ_{ii} to possible bias of the S4 trigger, σ_{iii} to event vertex and track selection procedure and σ_{iv} to the identification technique. Black lines (Total) show the total systematic uncertainty calculated as the square root of the sum of squares of the components

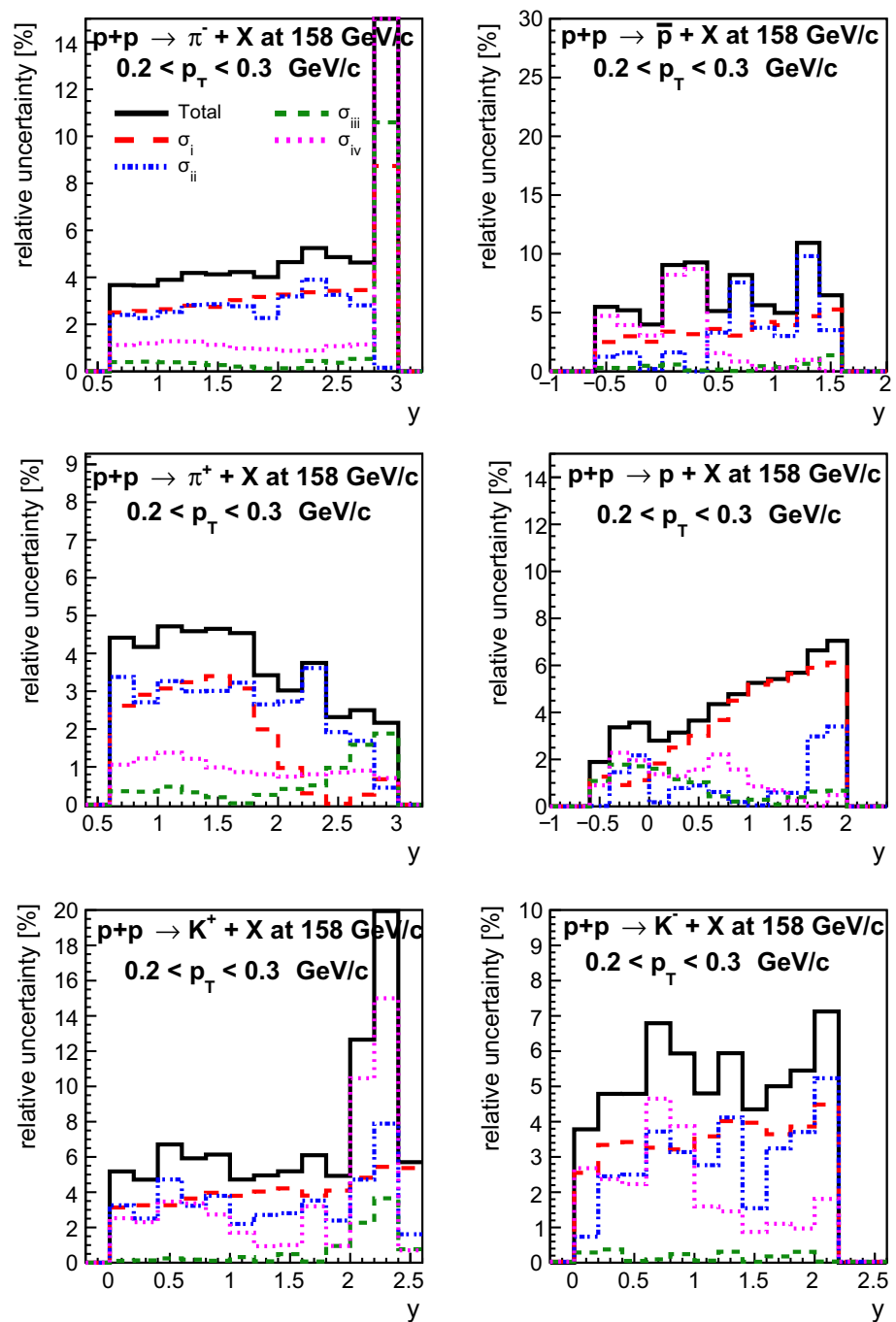


In order to ensure good fit quality, only bins with number of tracks greater than 300 are used for further analysis. The Bethe–Bloch curves for different particle types cross each other at low values of the total momentum. Thus, the proposed technique is not sufficient for particle identification at low p_{lab} and bins with $p_{lab} < 3.98$ GeV/c (bins 1–5) are excluded from the analysis based solely on dE/dx .

3.2.2 Identification based on time of flight and energy loss measurements (tof-dE/dx)

Identification of π^+ , π^- , K^+ , K^- , p and \bar{p} at low momenta (from 2 to 8 GeV/c) is possible when measurement of dE/dx is combined with time of flight (tof) information. Signals from the constant-fraction discriminators TDC and signal amplitude information from ADCs are recorded for each tile of the ToF-L/R walls. Only tof hits which satisfy quality

Fig. 17 Components of systematic uncertainty of particle spectra obtained from the dE/dx method in inelastic $p + p$ interaction at 158 GeV/c as function of rapidity for the transverse momentum interval between 0.2–0.3 GeV/c. σ_i refers to removal of events with off-time beam tracks, σ_{ii} to possible bias of the S4 trigger, σ_{iii} to event vertex and track selection procedure and σ_{iv} to the identification technique. Black lines (Total) show the total systematic uncertainty calculated as the square root of the sum of squares of the components



criteria (see Ref. [18]) are selected for the analysis. Tracks reconstructed in the TPCs are extrapolated to the front face of ToF-L/R where they are matched to the selected hits. The position of the extrapolation point on the scintillator tile is used to correct the measured value of tof for the propagation time of the light signal. The distribution of the difference between the corrected tof measurement and the value predicted from the track momentum and the trajectory length can be well described by a Gaussian with standard deviation of 80 ps for ToF-R and 95 ps for ToF-L. These

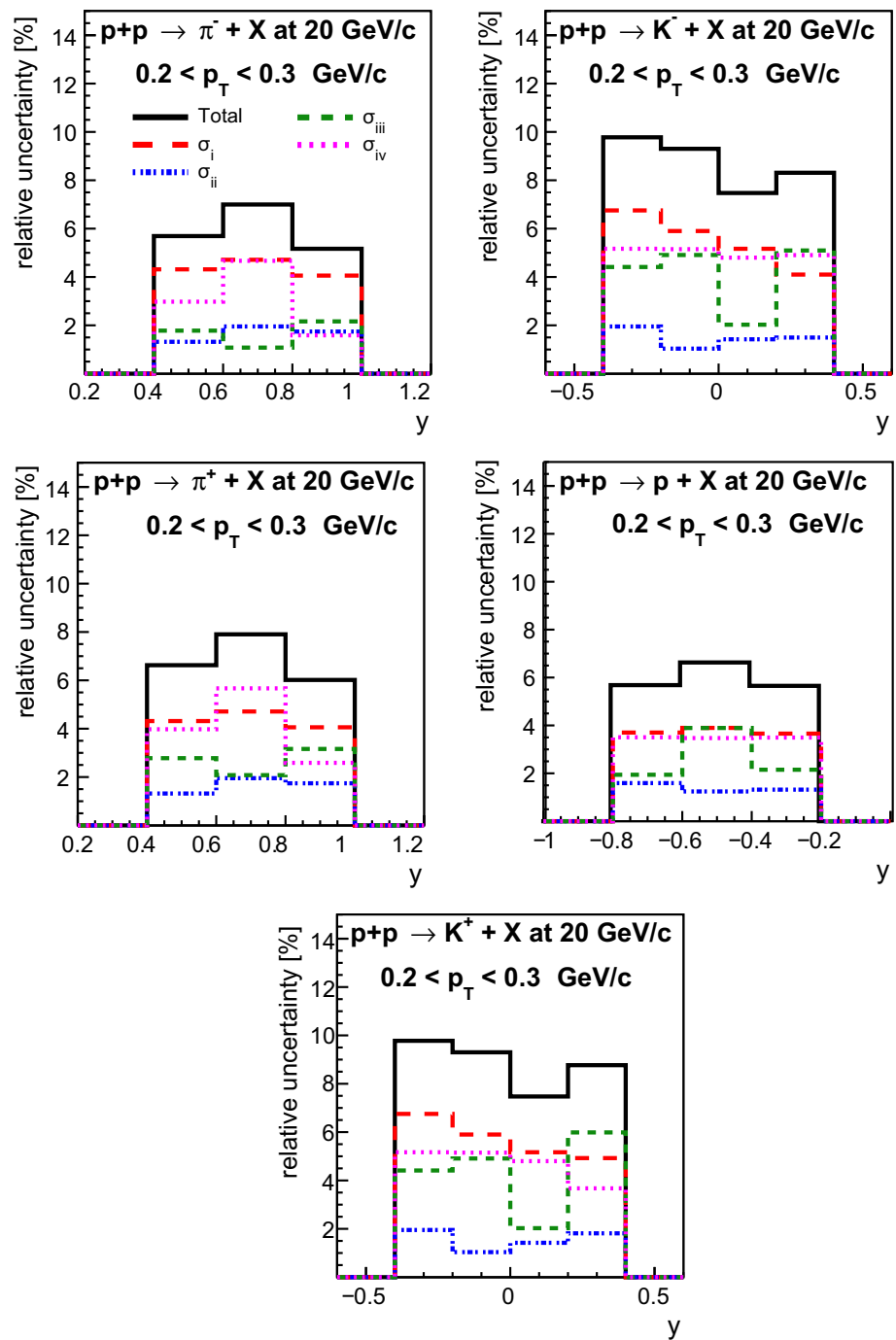
values represent the tof resolution including all detector effects.

The square of the particle mass m^2 is obtained from tof , the momentum p and the fitted trajectory length l :

$$m^2 = (cp)^2 \left(\frac{c^2 tof^2}{l^2} - 1 \right). \quad (3)$$

For illustration distributions of m^2 versus p_{lab} are plotted in Fig. 7 for negatively (*left*) and positively (*right*) charged

Fig. 18 Components of systematic uncertainty of particle spectra obtained from the *tof*- dE/dx method in inelastic p + p interaction at 20 GeV/c as function of rapidity for the transverse momentum interval between 0.2–0.3 GeV/c. σ_i refers to removal of events with off-time beam tracks, σ_{ii} to possible bias of the S4 trigger, σ_{iii} to event vertex and track selection procedure and σ_{iv} to the identification technique. Black lines (Total) show the total systematic uncertainty calculated as the square root of the sum of squares of the components



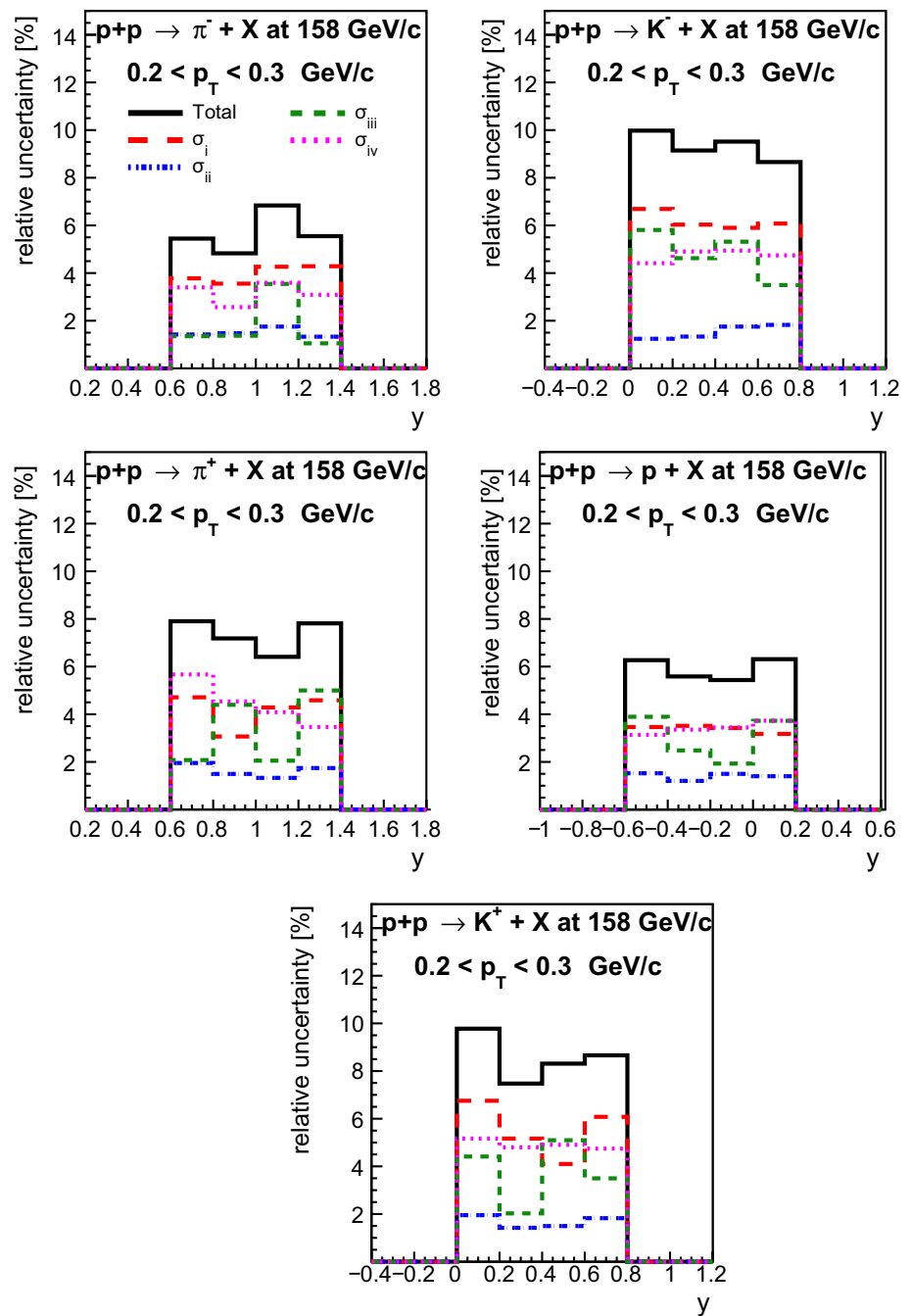
hadrons produced in p + p interactions at 80 GeV/c. Bands which correspond to different particle types are visible. Separation between pions and kaons is possible up to momenta of about 5 GeV/c, between pions and protons up to about 8 GeV/c.

Example distributions of particles in the m^2 - dE/dx plane for p + p interactions at 40 GeV/c are presented in Fig. 8. Simultaneous dE/dx and *tof* measurements lead to improved separation between different hadron types. In this case a sim-

ple Gaussian parametrization of the dE/dx distribution for a given hadron type can be used.

The *tof*- dE/dx identification method proceeds by fitting the 2-dimensional distribution of particles in the dE/dx - m^2 plane. Fits were performed in 7 equal momentum bins from 1 to 8 GeV/c and 20 equal bins in transverse momentum in the range 0–2 GeV/c. For positively charged particles the fit function included contributions of p, K^+ , π^+ and e^+ , whereas for negatively charged particles the corresponding

Fig. 19 Components of systematic uncertainty of particle spectra obtained from the *tof*- dE/dx method in inelastic $p + p$ interaction at 158 GeV/c as function of rapidity for the transverse momentum interval between 0.2–0.3 GeV/c. σ_i refers to removal of events with off-time beam tracks, σ_{ii} to possible bias of the S4 trigger, σ_{iii} to event vertex and track selection procedure and σ_{iv} to the identification technique. Black lines (Total) show the total systematic uncertainty calculated as the square root of the sum of squares of the components



anti-particles were considered. The fit function for a given particle type was assumed to be a product of a Gauss function in dE/dx and the sum of two Gauss functions in m^2 . Then the full fitted function (for simplicity of notation dE/dx is denoted by x and m^2 by y) reads:

$$\begin{aligned} \rho(x, y) &= \sum_i \rho_i(x, y) \\ &= \sum_{i=\pi, p, K} A_i e^{-\frac{(x-x_i)^2}{2\sigma_x^2}} \left(f e^{-\frac{(y-y_1)^2}{2\sigma_{y1}^2}} + (1-f) e^{-\frac{(y-y_2)^2}{2\sigma_{y2}^2}} \right), \end{aligned} \tag{4}$$

where A_i and f are the amplitude parameters, x_i , σ_x and y_i , σ_{y1} , σ_{y2} are mean and width of the dE/dx and m^2 Gaussians, respectively. The total number of parameters in Eq. (4) is 16. The fits were performed imposing the following constraints:

- (i) $y_i = m_i^2$, where m_i is a particle mass [19],
- (ii) relative dE/dx positions of electrons, kaons and protons to pions were assumed to be p_T -independent,
- (iii) the fitted amplitudes were required to be greater than or equal to 0,

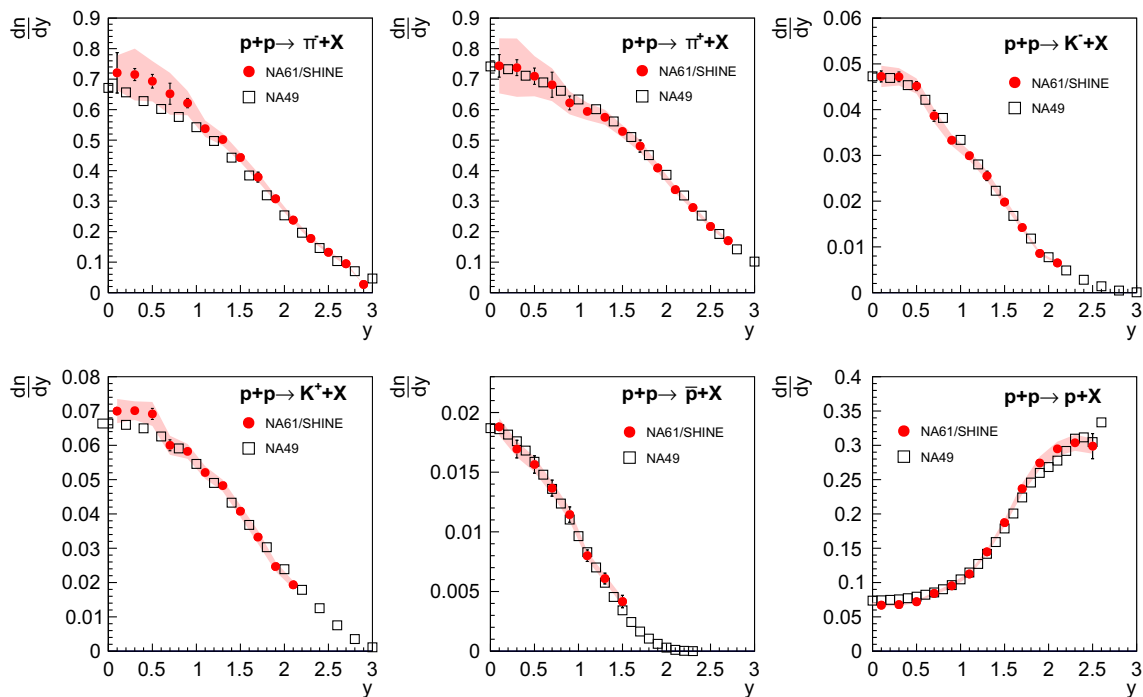


Fig. 20 Comparison of rapidity distributions of pions, kaons and protons produced in inelastic p + p interactions at 158 GeV/c. The plotted NA49 results were published without uncertainties [11–13]. NA61/SHINE systematic uncertainties are shown as shaded red bands

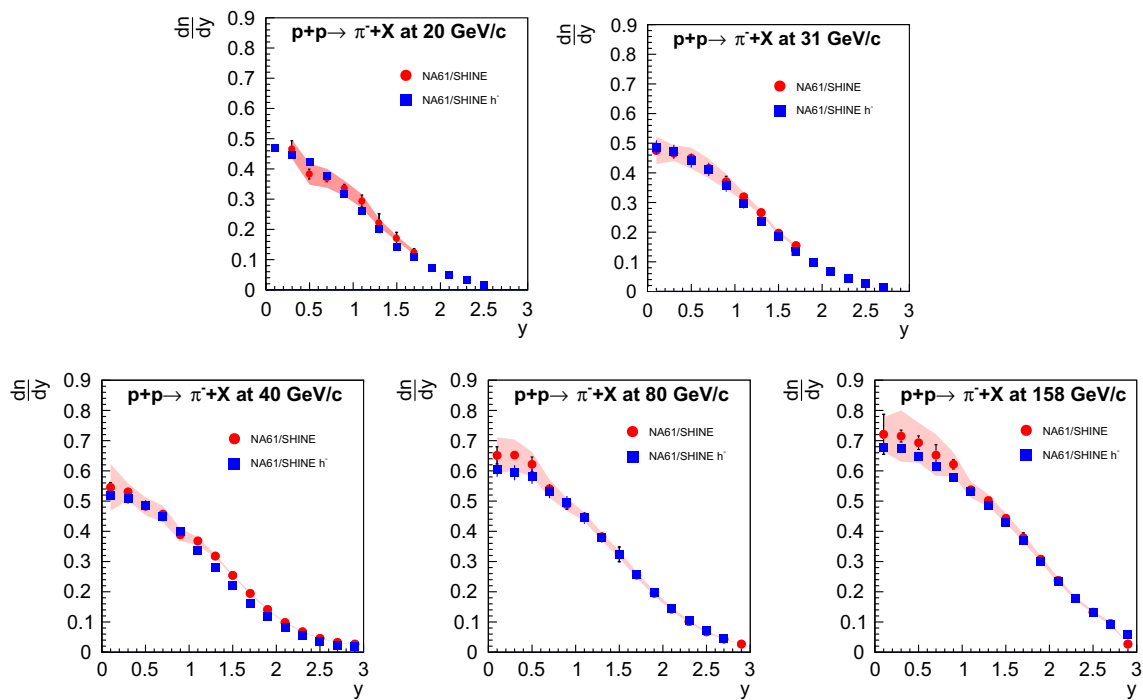


Fig. 21 Comparison of π^- rapidity distributions obtained by dE/dx and $tof-dE/dx$ methods with results from the h^- technique [3]. The h^- results are presented with statistical uncertainty. Red shaded bands

show the systematic uncertainty of particle multiplicities obtained by the $tof-dE/dx$ method

(iv) if possible, the relative dE/dx position of the positive kaon peak was taken to be the same as that of negative kaons determined from the negatively charged particles

in the bin of the same p_{lab} and p_T . This procedure helps to overcome the problem of the large overlap between K^+ and protons in the dE/dx distributions,

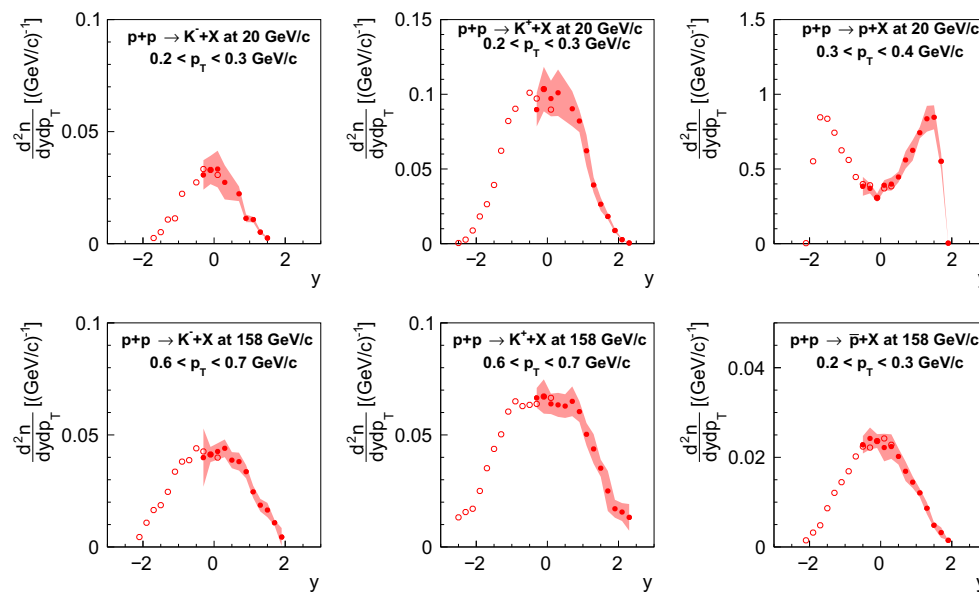


Fig. 22 Rapidity spectra of K^- , K^+ and p measured (filled dots) and reflected with respect to mid-rapidity (open dots) obtained in inelastic $p + p$ interactions in the interval $p_T = 0.2\text{--}0.3$ GeV/c at 20 GeV/c (upper row) and $p_T = 0.6\text{--}0.7$ GeV/c at 158 GeV/c (bottom row)

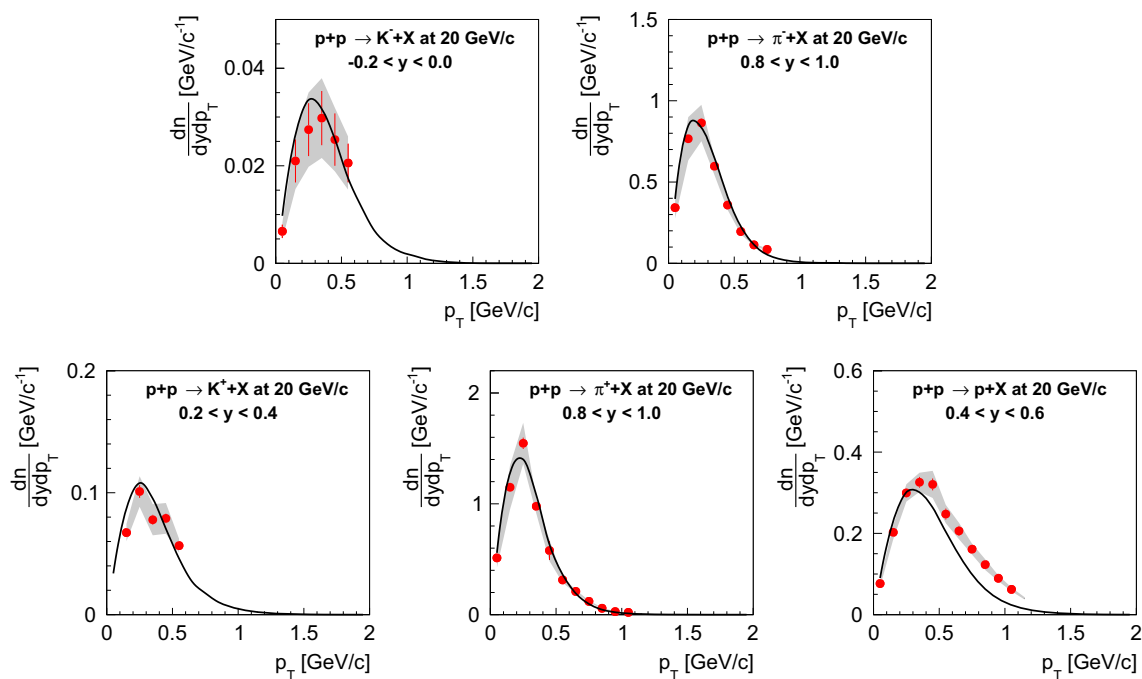


Fig. 23 Transverse momentum spectra of identified hadrons produced in inelastic $p + p$ interactions at 20 GeV/c in selected rapidity intervals in comparison to the EPOS model [21] (black line). Systematic uncertainties are shown as shaded bands

(v) $\sigma_{y1} < \sigma_{y2}$ and $f > 0.7$, the “core” distribution dominates the m^2 fit.

The total number of fitted parameters is then reduced to 5.

An example of the tof - dE/dx fit obtained in a single phase-space bin for positively charged particles in $p + p$ interactions at 158 GeV/c is shown in Fig. 9.

The tof - dE/dx method allows to fit the kaon yield close to mid-rapidity. This is not possible using the dE/dx method. Moreover, the kinematic domain in which pion and proton yields can be fitted is enlarged. The results from both methods partly overlap at the highest beam momenta. In these regions the results from the dE/dx method were selected since they have smaller uncertainties.

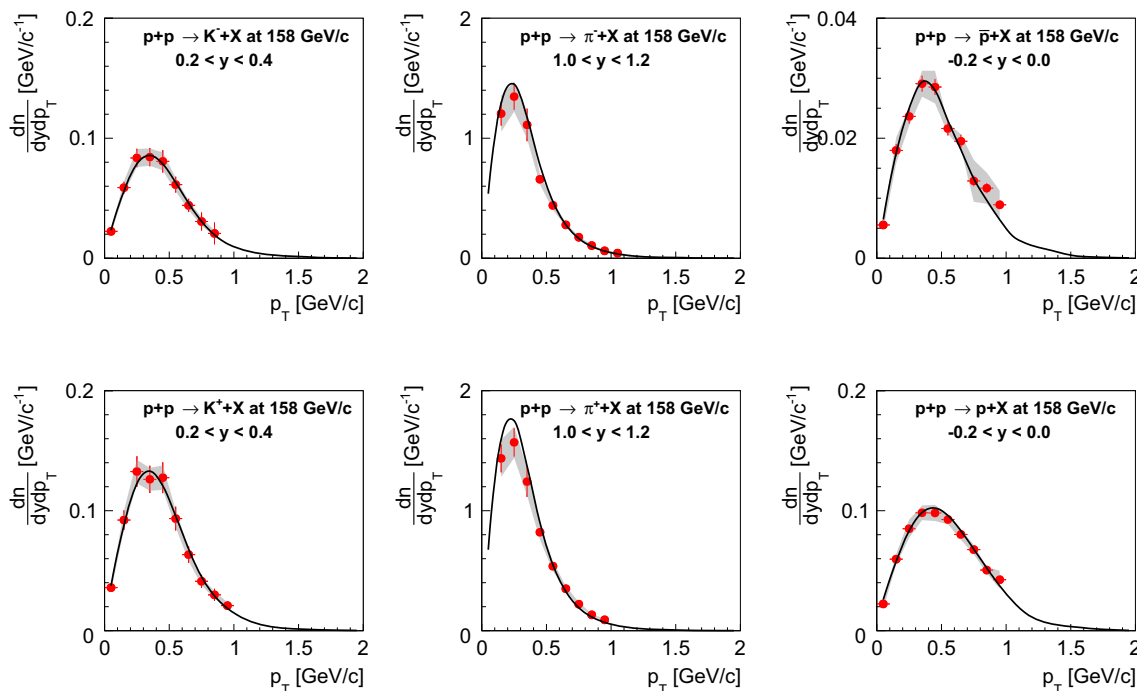


Fig. 24 Transverse momentum spectra of identified hadrons produced in inelastic p + p interactions at 158 GeV/c in selected rapidity intervals in comparison to the EPOS model [21] (black line). Systematic uncertainties are shown as shaded bands

3.2.3 Probability method

The probability method allows to transform fit results performed in (p_{lab}, p_T) bins to results in (y, p_T) bins. The fit results allow to calculate a probability P_i that a measured particle is of a given type $i = \pi, K, p, e$, namely for the dE/dx fits (see Eq. (1)) one gets:

$$P_i(dE/dx)_{p_{lab}, p_T} = \frac{\rho_i(dE/dx)_{p_{lab}, p_T}}{\sum_{i=\pi, K, p, e} \rho_i(dE/dx)_{p_{lab}, p_T}}, \tag{5}$$

where ρ_i is the value of the fitted function in a given (p_{lab}, p_T) bin calculated for dE/dx of the particle.

Similarly the tof - dE/dx fits (see Eq. (4)) give a particle type probability as

$$P_i(dE/dx, m^2)_{p_{lab}, p_T} = \frac{\rho_i(dE/dx, m^2)_{p_{lab}, p_T}}{\sum_{i=\pi, K, p, e} \rho_i(dE/dx, m^2)_{p_{lab}, p_T}}. \tag{6}$$

For illustration particle type probability distributions for positively and negatively charged particles produced in p + p interactions at 20 and 158 GeV/c are presented in Fig. 10 for the dE/dx fits and in Fig. 11 for the tof - dE/dx fits. Only in the case of perfect particle type discrimination the probability distributions in Figs. 10 and 11 will show peaks at 0 or 1. In

the case of non-ideal discrimination (overlapping dE/dx or tof - dE/dx distributions) values between these extremes will be populated.

The numbers of identified particles in a given kinematical bin (e.g., (p_{lab}, p_T)) are given by [20]:

$$n_{i=\pi, K, p} = \sum_{j=1}^n P_j, \tag{7}$$

where P_i is the probability of particle type i given by Eqs. (5) and (6) and n is the number of particles in the given kinematical bin.

Additionally the probability method allows to implement the efficiency correction particle by particle. The corrected number of identified particles in the given kinematical bin is:

$$n_{i=\pi, K, p} = \sum_{j=1}^n P_j \epsilon, \tag{8}$$

where as in Eq. (7) P_i is the probability of particle type i given by Eqs. (5) and (6) and n is the number of particles in the given kinematical bin and ϵ is the efficiency. Usually the efficiency is calculated with a different binning scheme. Thus the value of ϵ has to be taken from the bin which corresponds to the kinematic quantities of particle i .

The probability method has some subtleties when the coverage of phase-space differs between identification and final

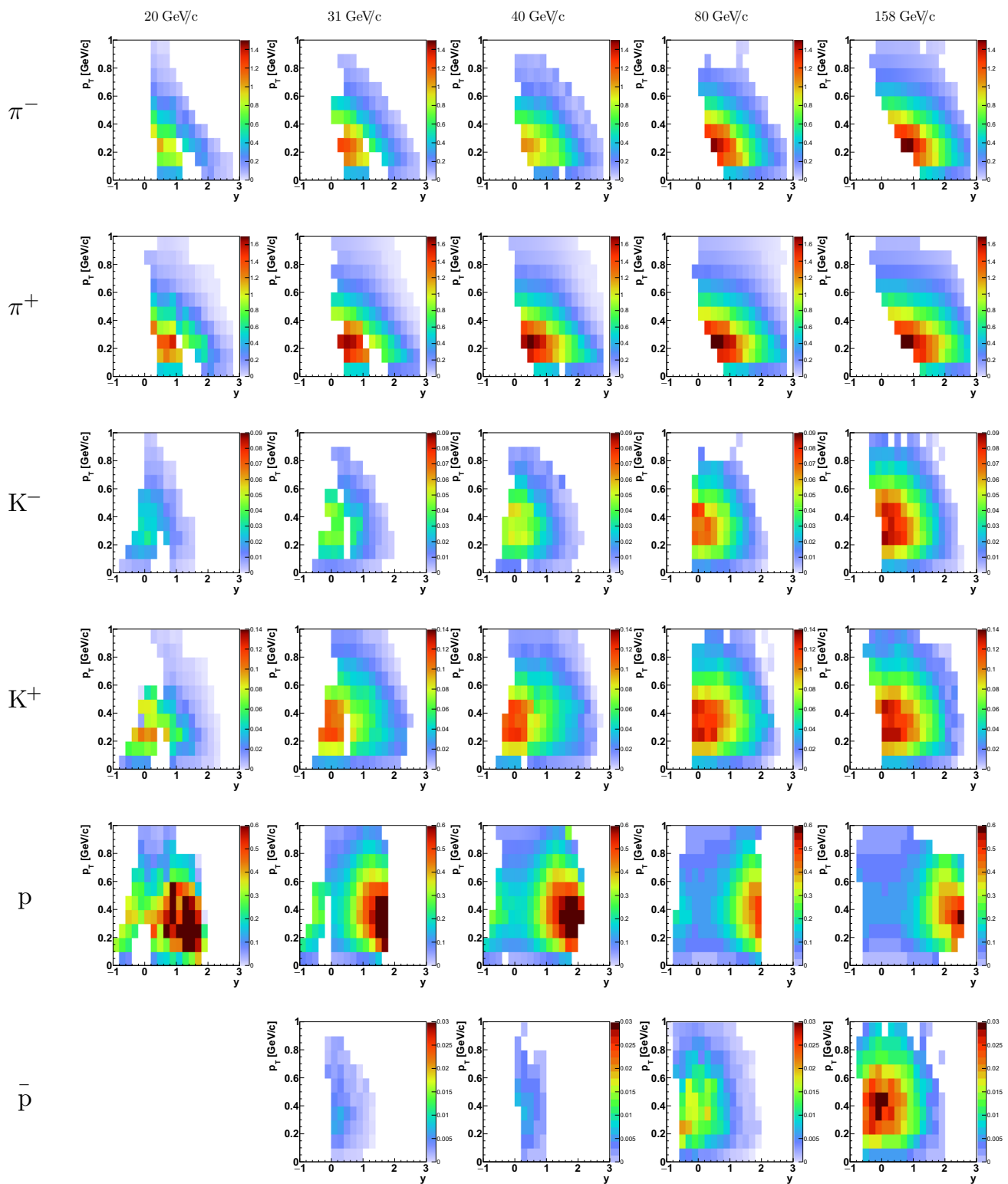


Fig. 25 Transverse momentum-rapidity spectrum of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic $p + p$ interactions at 20, 31, 40, 80 and 158 GeV/c. Color scale represents particle multiplicities normalized to the phase-space bin size ($\frac{dn}{dydp_T}$)

variable. For example particles in bins selected for the identification (p_{lab}) may not fully populate the edges of bins in the final variable (y) due to the non-orthogonal transforma-

tion between them. However, only the edges of the spectra are affected. For the dE/dx analysis method bins could be selected in such a way that edges almost overlap. The

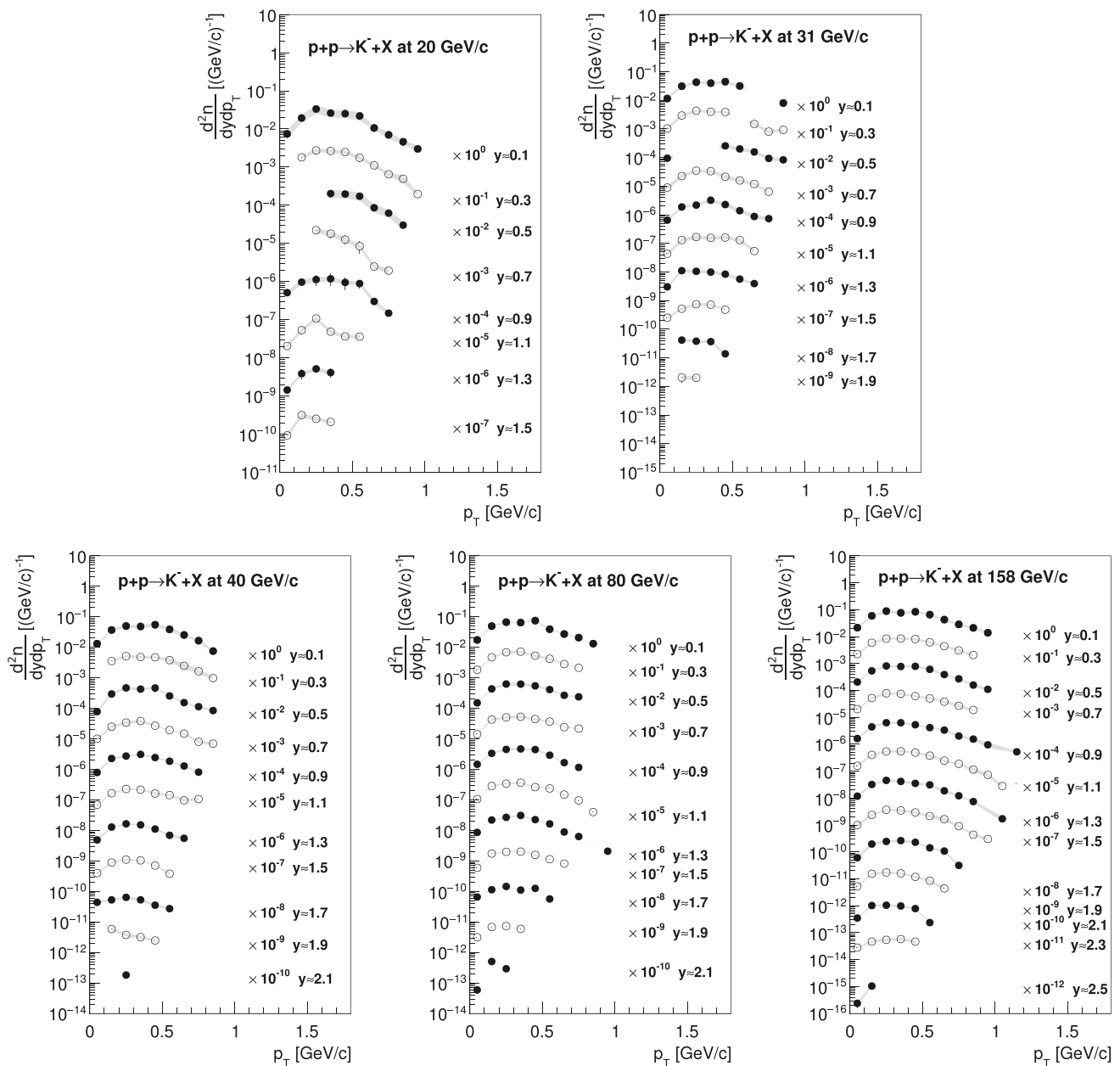


Fig. 26 Transverse momentum K^- spectra in rapidity slices produced in inelastic $p + p$ interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties

remaining small effect was corrected by the overall Monte-Carlo correction factor. The mismatches are larger for the $tof-dE/dx$ method where identification had to be performed in linear, equal bins in total momentum due to the Tof acceptance. Therefore a separate correction factor ϵ was calculated using the simulation based on the EPOS model (see below):

$$\epsilon = \frac{n_{MC}^{accepted}}{n_{MC}^{generated}} \tag{9}$$

where $n_{MC}^{accepted}$ are the numbers of tracks accepted in a rapidity bin within the phase space covered by the identification

technique and $n_{MC}^{generated}$ the number of tracks generated in the corresponding rapidity bin. Bins in which this correction exceeds 30% are rejected and the others are corrected by this factor.

3.3 Corrections

In order to determine the true number of each type of identified particle produced in inelastic $p + p$ interactions a set of corrections was applied to the extracted raw results. The main effects for which corrections were introduced are the follow-

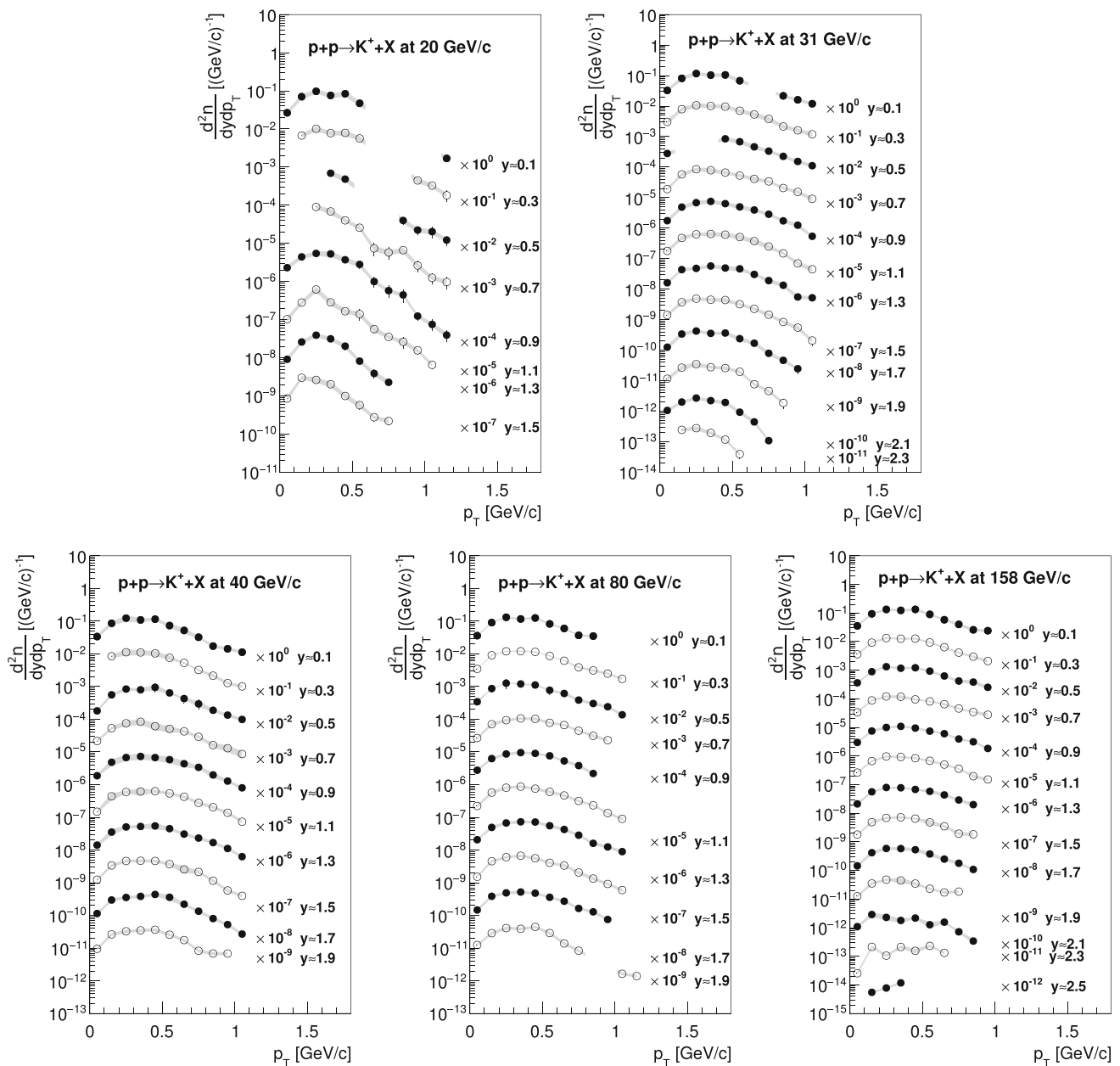


Fig. 27 Transverse momentum K^+ spectra in rapidity slices produced in inelastic $p + p$ interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties

ing: contribution of interactions outside the liquid hydrogen of the target (off-target events), detector effects (acceptance, efficiency) and particles from weak decays (feed-down). Note that the manner of application and the number of used correction factors depend on the particle identification technique (i.e. dE/dx or $tof-dE/dx$).

3.3.1 Correction for off-target interactions

To estimate the off-target interactions about 10% of the data were collected without the liquid hydrogen in the target (so-

called target removed data denoted as R). Before the identification procedure (see Sect. 3.2.1) a suitably normalized target removed yield was subtracted from target inserted data. This correction was applied for each bin of total momentum and transverse momentum.

The normalization of the target removed data was based on the fitted vertex z distribution. The ratio of the numbers of events with fitted vertex outside the target (in the range from -400 to -200 cm) was calculated for target inserted and removed data and used subsequently as the normalization factor. The contamination of out of target events in the target

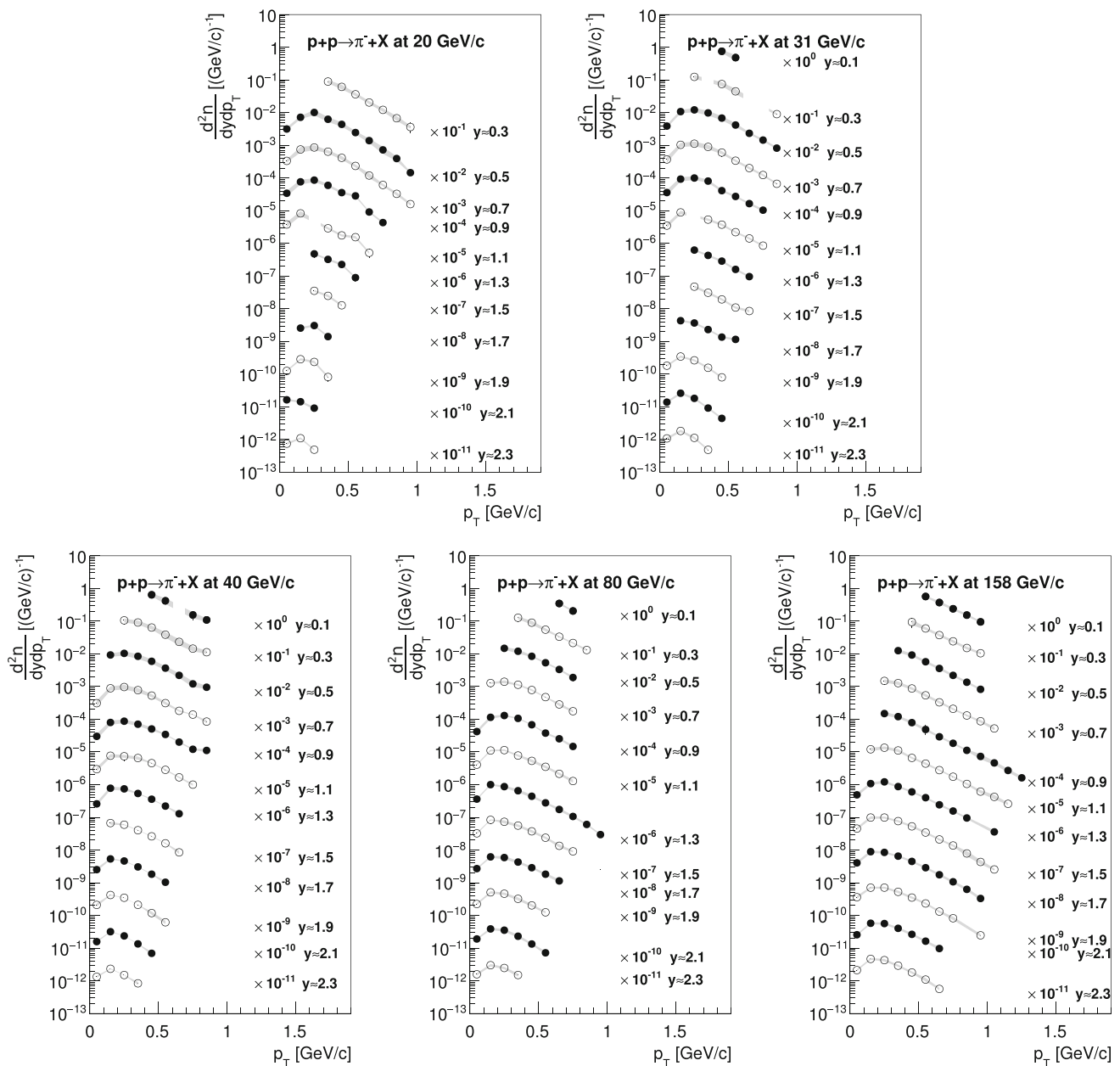


Fig. 28 Transverse momentum π^- spectra in rapidity slices produced in inelastic p + p interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties

inserted sample is given in Table 3 for p + p interactions at 20, 31, 40, 80 and 158 GeV/c.

3.3.2 Corrections for detector effects and particles from weak decays (feed-down)

A simulation of the NA61/SHINE detector is used to correct the data for reconstruction efficiency and acceptance. Only inelastic p + p interactions on the hydrogen in the target cell were simulated and reconstructed. The EPOS model [21] was selected to generate the primary interactions as it best

describes the NA61/SHINE measurements. A Geant3 based program chain was used to track particles through the spectrometer, generate decays and secondary interactions and simulate the detector response (for more detail see Ref. [3]). The reconstructed tracks were matched to the simulated particles based on the cluster positions. The derived corrections can be applied only for inelastic events. The contribution of elastic events in the data was eliminated by the event and track selection cuts. Hadrons which were not produced in the primary interaction can amount to a significant fraction of the selected track sample. Thus a special effort was under-

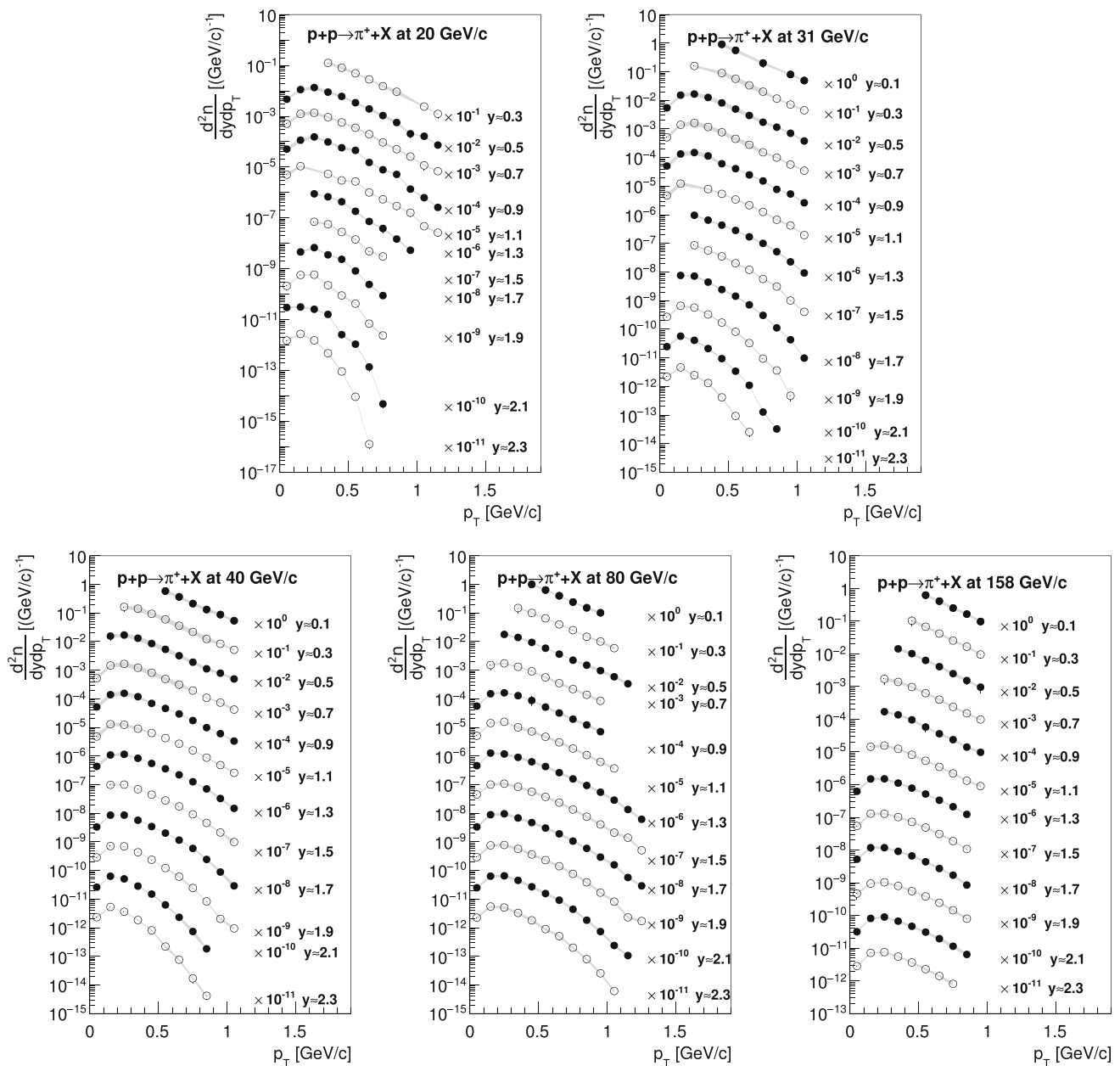


Fig. 29 Transverse momentum π^+ spectra in rapidity slices produced in inelastic p + p interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties

taken to evaluate and subtract this contribution (see above). As mentioned before correction factors depend on the particle identification technique and are described separately.

The dE/dx method.

The correction factor C is defined as:

$$C_i = \frac{(n_i)_{sel}^{MC}}{(n_i)_{gen}^{MC}}, \quad (10)$$

where:

- $(n_i)_{gen}^{MC}$: multiplicity of particle type i ($i = \pi^{+/-}, K^{+/-}, p, \bar{p}$) generated by the EPOS model,
- $(n_i)_{sel}^{MC}$: multiplicity of particle type i ($i = \pi^{+/-}, K^{+/-}, p, \bar{p}$) after applying the selection criteria described in the previous section,

The correction factor was calculated in the same bins of y and p_T as the particle spectra. Bins with correction factor lower than 0.5 and higher than 1.5 were rejected from the final results due to low acceptance or high contamination of particles from weak decays. Statistical uncertainties of the

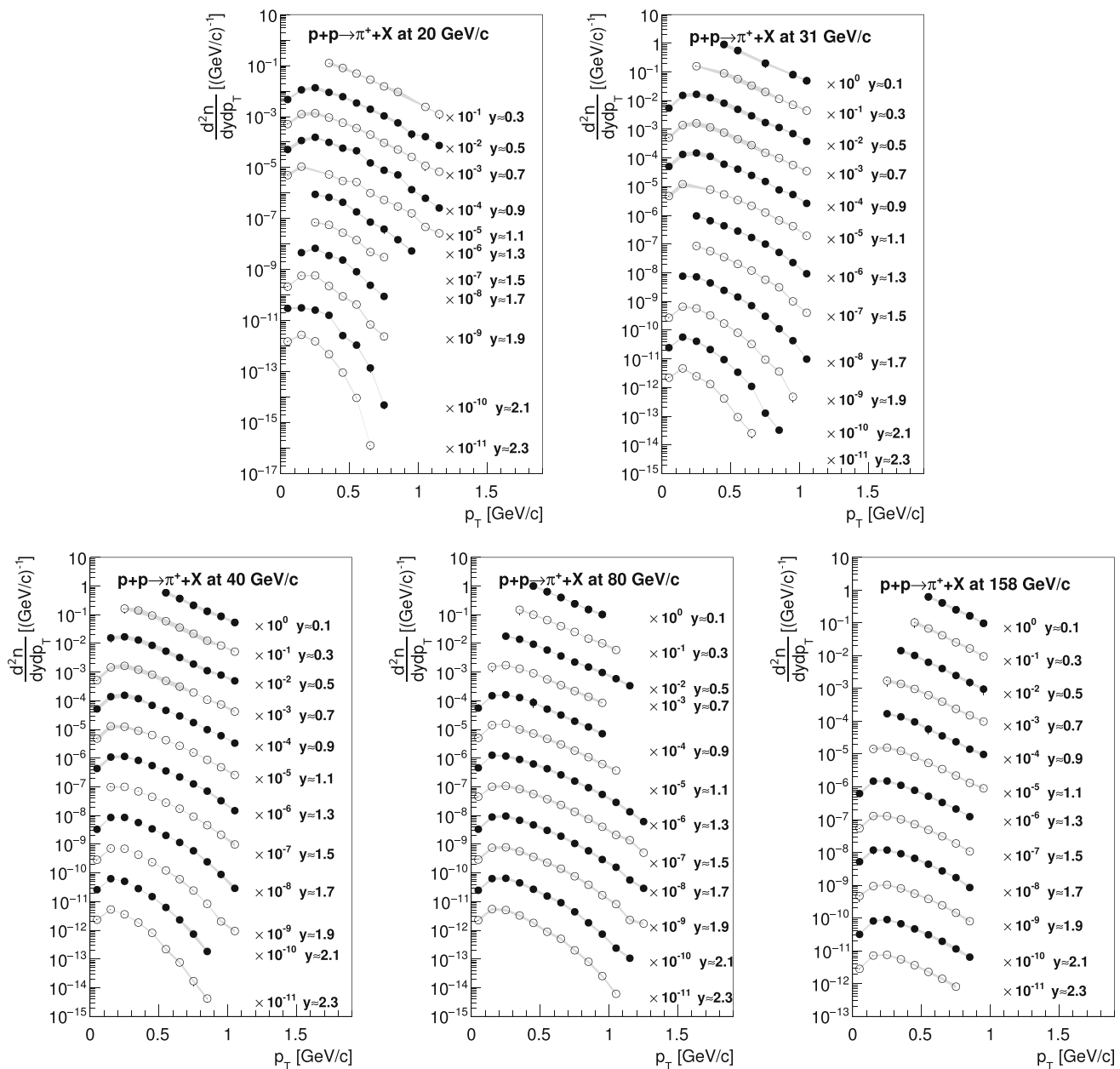


Fig. 30 Transverse momentum p spectra in rapidity slices produced in inelastic $p + p$ interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties

correction factors were calculated from the binomial distribution. The inverse correction factors for $p + p$ interactions at 20 and 158 GeV/c are presented in Figs. 12 and 13.

The $tof-dE/dx$ method.

Due to the lack of a simulation of the ToF system the corrections for the $tof-dE/dx$ identification procedure had to be done in a different way than for the dE/dx method, namely they partially employed a data based approach. Each simulated and reconstructed track was extrapolated to the ToF walls and if it crossed one of the ToF pixels it was classified

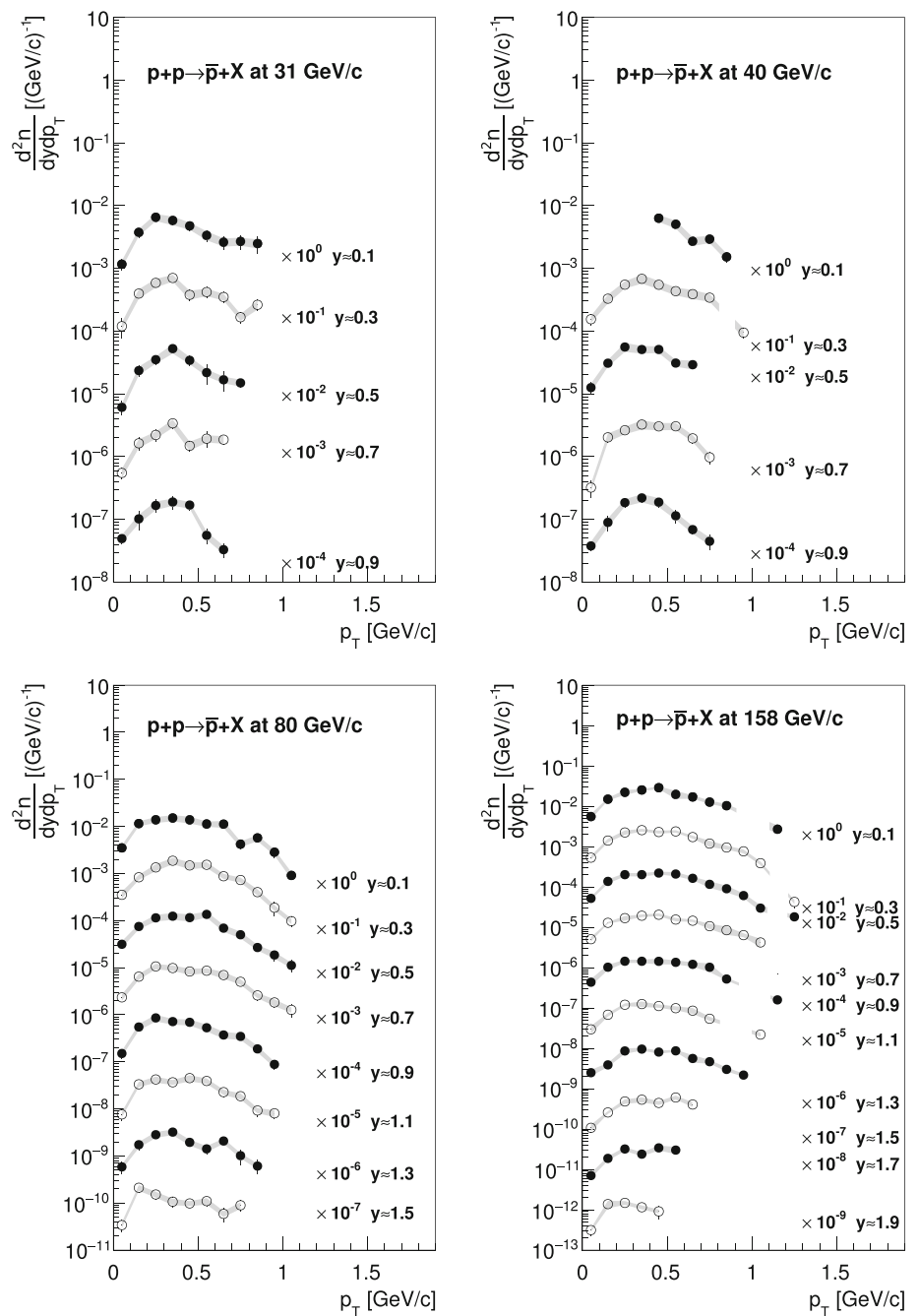
as having a ToF hit. This defined the geometrical acceptance. The efficiency of the ToF pixels was estimated from data.

The correction factor for the $tof-dE/dx$ identification method comprises the following components:

- (i) Correction for the detector efficiency and geometrical acceptance

Based on the event and detector simulation the combined geometrical and reconstruction efficiency C_i^{geo} was calculated as:

Fig. 31 Transverse momentum \bar{p} spectra in rapidity slices produced in inelastic $p + p$ interactions at 20, 31, 40, 80, 158 GeV/c. Rapidity values given in the legends correspond to the middle of the corresponding interval. Shaded bands show systematic uncertainties



$$C_i^{\text{geo}} = \frac{(n_i)_{\text{geo}}^{\text{MCrec}}}{(n_i)^{\text{MCgen}}}, \quad (11)$$

where $(n_i)_{\text{geo}}^{\text{MCrec}}$ is the multiplicity of particle type $i = \pi^-, \pi^+, K^-, K^+, p, \bar{p}$ after the TPC selection criteria and track extrapolation to the ToF wall resulting in a ToF hit, and $(n_i)^{\text{MCgen}}$ is the multiplicity of particle type i generated by the EPOS model. In addition, the last point on the track was required to be located in the last two padrows of a MTPC. The resulting geometrical correction factors for $p + p$ interactions at 158 GeV/c are

presented in Fig. 46. Differences between efficiencies for pions, kaons and protons are due to the different particle lifetimes.

- (ii) Correction for the pixel efficiency of ToF-L and ToF-R detectors

The pixel efficiency was calculated from data as the ratio between $(n_i)_{\text{hit}}^{\text{tof}}$, the number of tracks with ToF hits in working pixels (pixel efficiency from data higher than 50%) with correct TDC and QDC measurements and $(n_i)_{\text{geo}}^{\text{tof}}$, the number of all tracks which were extrap-

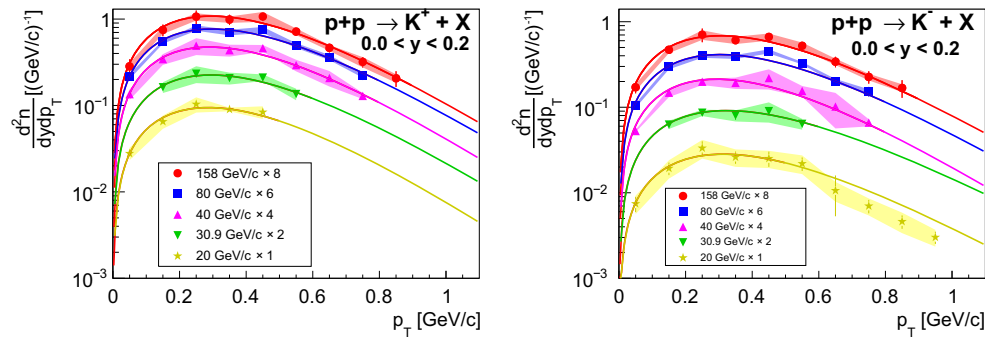


Fig. 32 Transverse momentum spectra of K^+ and K^- mesons produced at $y \approx 0$ in inelastic p + p interactions. Colored lines represent the fitted function (Eq. (19))

olated to the particular pixel.

$$C_i^{pixel} = \frac{(n_i)_{hit}^{tof}}{(n_i)_{geo}^{tof}}, \tag{12}$$

The pixel efficiency obtained for p + p interactions at 158 GeV/c is shown in Fig. 47.

- (iii) Correction for decays and interactions between the last measured point in the MTPC and the ToF detectors
The probability of decays and interactions between the last measured point in the MTPC and the ToF detectors was estimated by simulations. The survival probability is defined in the following way:

$$C_i^{survive} = \frac{(n_i)_{survive}^{MCrec}}{(n_i)_{geo}^{MCrec}}, \tag{13}$$

where $(n_i)_{survive}^{MCrec}$ is the number of particles which hit a working ToF pixel and which did not decay or interact between the last measured point in the MTPC and the ToF walls. The survival probability is lower than expected from decay only, due to interactions in the Forward Time of Flight detector. The survival probability $C_i^{survive}$ is presented in Fig. 48.

The combined efficiency factor C_i^{tof} was calculated as:

$$C_i^{tof} = C_i^{geo} \times C_i^{pixel} \times C_i^{decay} \tag{14}$$

Combined efficiency factors C_i^{tof} for the *tof*-dE/dx method calculated for each (p, p_T) bin independently applied to p + p interactions at 20 and 158 GeV/c are presented in Figs. 14 and 15.

3.4 Corrected spectra and uncertainties

3.4.1 Corrected spectra

The multiplicity of different types of hadrons from inelastic p + p interactions measured by the dE/dx technique is defined as the sum of probabilities divided by the number of events corrected for detector effects, feed-down and contamination by target removed events. For particle type $i = \pi^+, \pi^-, K^+, K^-, p, \bar{p}$, the multiplicity is defined as:

$$\frac{n_i}{N} = \frac{1}{C_i} \frac{\sum_I P_i(dE/dx)_{p_{lab}, p_T} - B \sum_R P_i(dE/dx)_{p_{lab}, p_T}}{N_I - BN_R}, \tag{15}$$

where:

- C_i : correction factor defined in Eq. (10),
- $\sum_I P_i(dE/dx)_{p_{lab}, p_T} \equiv \sum_I P_i$: sum over probabilities P_i defined in Eq. (5) for all tracks for inserted target (abbreviated as “I”),
- $\sum_R P_i(dE/dx)_{p_{lab}, p_T} \equiv \sum_R P_i$: sum over probabilities P_i defined in Eq. (5) for all tracks for removed target (abbreviated as “R”),
- B : the normalization factor applied to target removed events,
- N_I and N_R : the number of events of target inserted and removed, respectively.

Particle multiplicities for the *tof*-dE/dx technique can be calculated in a similar way:

$$\frac{n_i}{N} = \frac{1}{\epsilon} \frac{\sum_I \frac{P_i(dE/dx, m^2)_{p_{lab}, p_T}}{C_{i, p_{lab}, p_T}^{tof}} - B \sum_R \frac{P_i(dE/dx, m^2)_{p_{lab}, p_T}}{C_{i, p_{lab}, p_T}^{tof}}}{N_I - BN_R}, \tag{16}$$

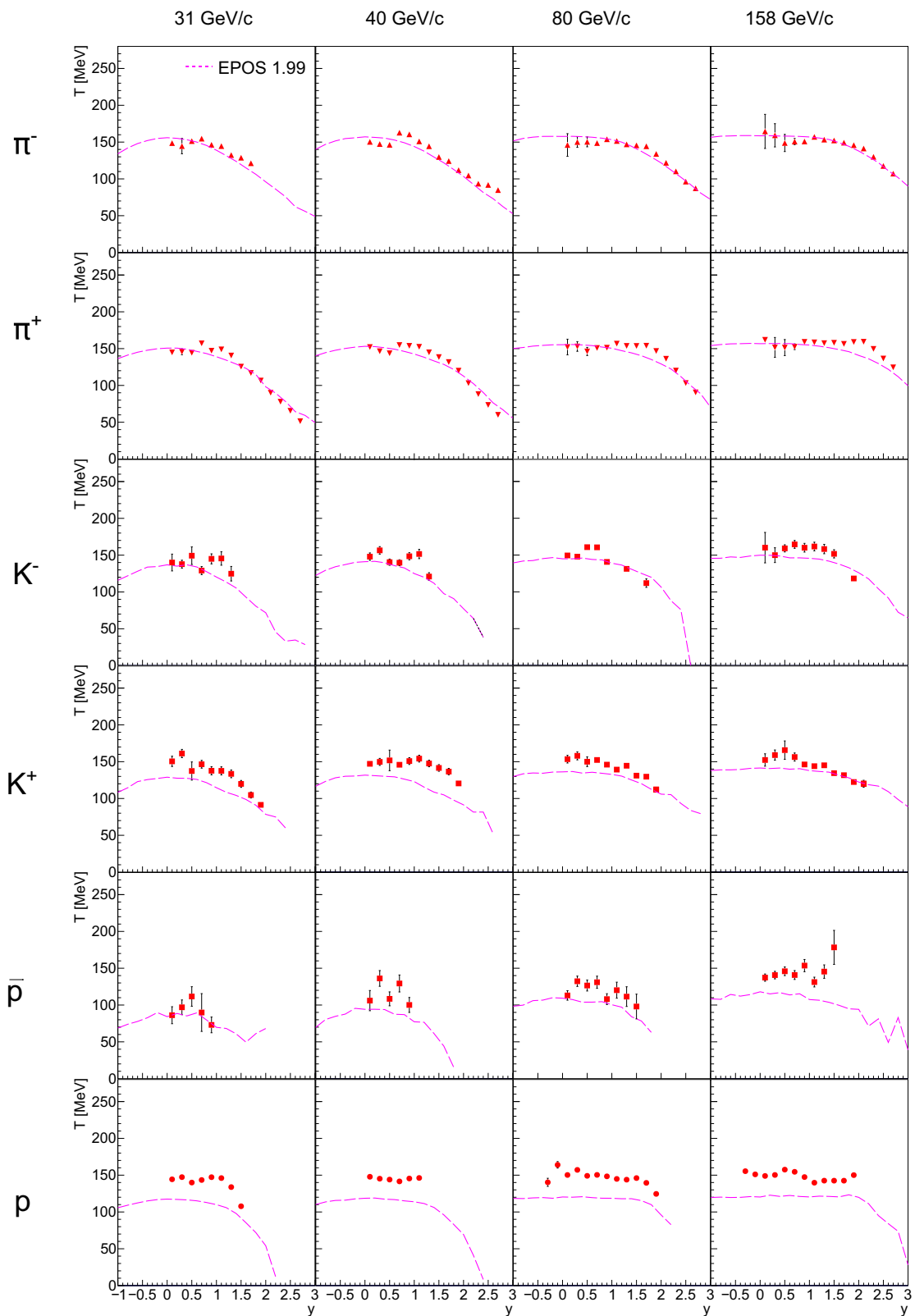


Fig. 33 Inverse slope parameter T obtained from fits with Eq. (19) to the p_T distributions of K^+ , K^- , π^+ , π^- , p and \bar{p} as function of rapidity in inelastic $p + p$ collisions at 30, 40, 80 and 158 GeV/c. Results are

compared with EPOS model [21] predictions fitted in the same range. Bars show statistical uncertainties. Systematic uncertainties of about 10% are not shown

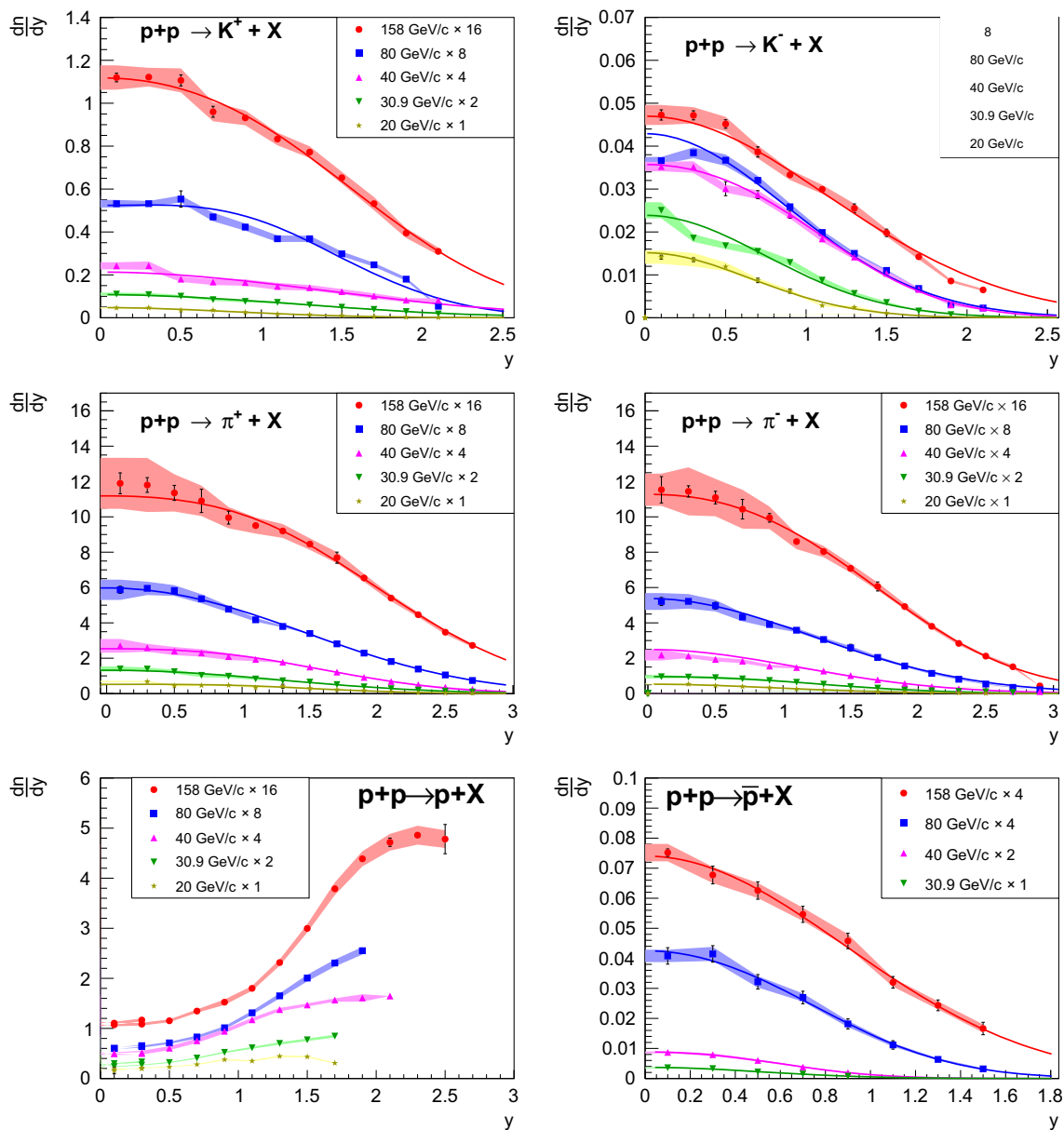


Fig. 34 Rapidity spectra of K^+ , K^- , π^+ , π^- , p and \bar{p} produced in inelastic $p + p$ interactions at SPS energies, scaled by appropriate factors for better visibility. Vertical bars indi-

cate statistical, shaded bands systematic uncertainties of the measurements. Curves depict Gaussian fits used to determine total multiplicities

Table 4 Mean multiplicity of positively charged particles at SPS energies with statistical and systematic uncertainties

	K^+	π^+	p
20 GeV/c	$0.097 \pm 0.014 \pm 0.006$	$1.884 \pm 0.012 \pm 0.20$	$1.069 \pm 0.010 \pm 0.13$
31 GeV/c	$0.157 \pm 0.010 \pm 0.015$	$2.082 \pm 0.021 \pm 0.20$	$0.977 \pm 0.003 \pm 0.14$
40 GeV/c	$0.170 \pm 0.009 \pm 0.023$	$2.390 \pm 0.022 \pm 0.16$	$1.095 \pm 0.003 \pm 0.09$
80 GeV/c	$0.201 \pm 0.010 \pm 0.010$	$2.671 \pm 0.022 \pm 0.14$	$1.093 \pm 0.004 \pm 0.07$
158 GeV/c	$0.234 \pm 0.014 \pm 0.017$	$3.110 \pm 0.030 \pm 0.26$	$1.154 \pm 0.010 \pm 0.04$

where: P_i are the probabilities defined in Eq. (6), C_i^{tof} is the efficiency described by Eq. (14) and ϵ is the correction for the non-orthogonal transformation between the phase spaces

(momentum \rightarrow rapidity) described by Eq. (9). Sum over probabilities are the same like in Eq. (15).

Table 5 Mean multiplicity of negatively charged particles at SPS energies with statistical and systematic uncertainties

	K^-	π^-	\bar{p}
20 GeV/c	$0.024 \pm 0.006 \pm 0.002$	$1.082 \pm 0.021 \pm 0.20$	–
31 GeV/c	$0.045 \pm 0.004 \pm 0.003$	$1.474 \pm 0.031 \pm 0.19$	$0.0047 \pm 0.0007 \pm 0.0003$
40 GeV/c	$0.084 \pm 0.006 \pm 0.003$	$1.711 \pm 0.028 \pm 0.17$	$0.0059 \pm 0.0006 \pm 0.0004$
80 GeV/c	$0.095 \pm 0.004 \pm 0.005$	$2.030 \pm 0.031 \pm 0.17$	$0.0183 \pm 0.0015 \pm 0.0010$
158 GeV/c	$0.132 \pm 0.011 \pm 0.009$	$2.404 \pm 0.034 \pm 0.18$	$0.0402 \pm 0.0020 \pm 0.0030$

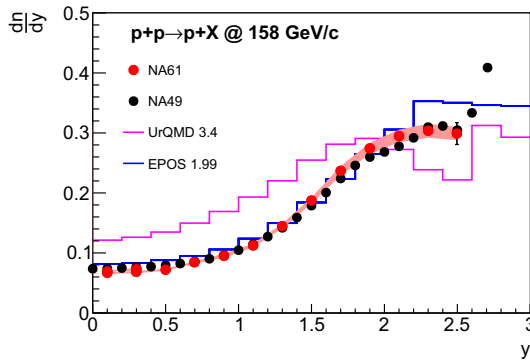


Fig. 35 Proton rapidity distribution in inelastic p + p interactions at 158 GeV/c compared with NA49 measurements [26] and predictions of the UrQMD [27,28] and EPOS [21] models

3.4.2 Statistical uncertainties

Statistical uncertainties of multiplicities obtained by the dE/dx method were calculated in the following way:

$$\begin{aligned}
 \left(\Delta \frac{n_i}{N}\right)^2 = & \left(\left| \frac{-1}{C_i^2} \frac{\sum_I P_i - B \sum_R P_i}{N_I - BN_R} \right| \Delta C_i \right)^2 \\
 & + \left(\left| \frac{1}{C_i} \frac{1}{N_I - BN_R} \right| \sqrt{\sum_I P_i} \right)^2 \\
 & + \left(\left| \frac{1}{C_i} \frac{-B}{N_I - BN_R} \right| \sqrt{\sum_R P_i} \right)^2, \quad (17)
 \end{aligned}$$

where Δ denotes the statistical uncertainty of the quantities used to calculate the particle multiplicity. The uncertainty of the normalization factor (B) as well as of the number of events (N_I and N_R) are not taken into account in this calculation due to their negligible influence on the uncertainty value.

Calculation of statistical uncertainties of the multiplicities from the tof - dE/dx identification technique is more complicated. Assuming that the statistical uncertainty of C_i^{tof} is equal to the mean statistical uncertainty in the full $y - p_T$ bin, it can be moved in front of the sums. The total statistical uncertainty can then be calculated according to the following

formula:

$$\begin{aligned}
 \left(\Delta \frac{n_i}{N}\right)^2 = & \left(\left| \frac{-1}{C_{tof}^2} \frac{\sum_I \frac{P_i}{C_i^{tof}} - B \sum_R \frac{P_i}{\epsilon}}{N_I - BN_R} \right| \Delta \epsilon \right)^2 \\
 & + \left(\left| \frac{1}{\epsilon} \frac{\sum_I \frac{1}{C_i^{tof}}}{N_I - BN_R} \right| \sqrt{\sum_I P_i} \right)^2 \\
 & + \left(\left| \frac{1}{\epsilon} \frac{\sum_R \frac{-B}{C_i^{tof}}}{N_I - BN_R} \right| \sqrt{\sum_R P_i} \right)^2 \\
 & + \left(\left| \frac{-1}{\epsilon \langle C_i^{tof} \rangle^2} \frac{\sum_I P_i - B \sum_R P_i}{N_I - BN_R} \right| \langle \Delta C_i^{tof} \rangle \right)^2. \quad (18)
 \end{aligned}$$

3.4.3 Systematic uncertainties

Systematic biases to the measurements could result mainly from:

- (i) Methods of event selection.

The first uncertainty is related to the acceptance of events with additional tracks from off-time particles. This systematic uncertainty was estimated by changing the width of the time window in which no second beam particle is allowed by $\pm 1 \mu s$ (variation by $\pm 50\%$) with respect to the nominal value of $\pm 2 \mu s$. The maximal difference of the results was assigned as the systematic uncertainty of the selection.

The second source of possible systematic bias are losses of inelastic events due to the interaction trigger. The S4 detector veto mainly selects inelastic and removes elastic scattering events. However, it can also result in some losses of inelastic events. To estimate this effect, the analysis was done using correction factors calculated with and without applying the S4 trigger in the simulation. The difference between these two results was taken as a contribution to the systematic uncertainty.

The next source of systematic uncertainty related to the

Fig. 36 Mean K^+ (left) and K^- (right) multiplicity produced in inelastic $p + p$ interactions as function of collision energy. Measurements of NA61/SHINE are plotted as filled red squares, world data [13, 29–36] are shown by open circles. Statistical uncertainties are indicated by bars, systematic uncertainties of the NA61/SHINE measurements by shaded bands

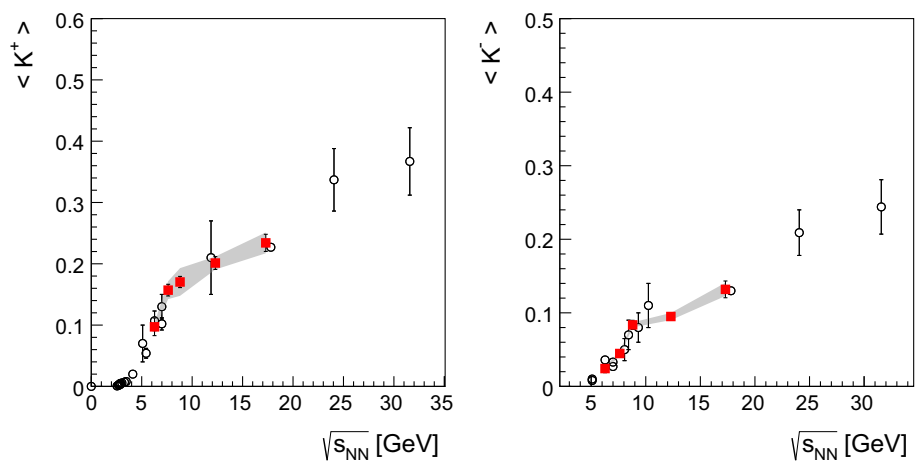
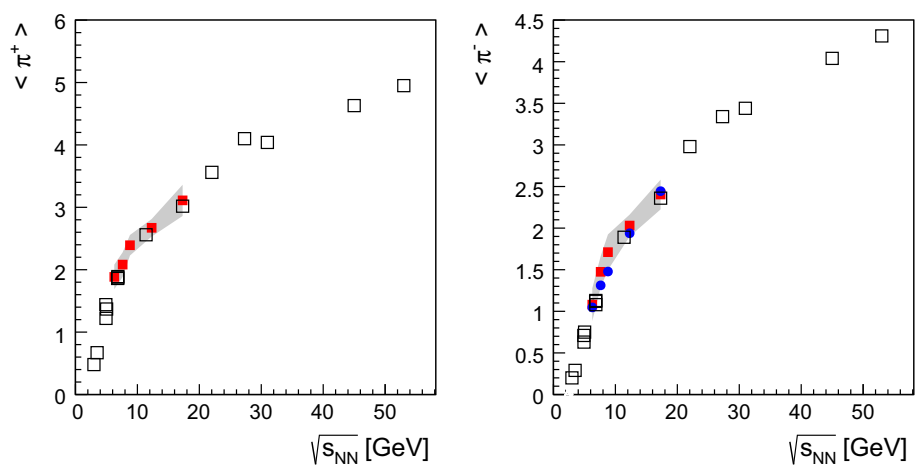


Fig. 37 Mean π^+ (left) and π^- (right) multiplicity produced in inelastic $p + p$ interactions as function of collision energy. Measurements of NA61/SHINE for identified pions are plotted as filled red squares, whereas those obtained by the h^- method [3] by blue dots. Black open squares represent the world data [11, 37–44]. Statistical uncertainties are indicated by bars, systematic uncertainties of the NA61/SHINE measurements by shaded bands



normalization came from the selection window for the z -position of the fitted vertex. To estimate the systematic uncertainty the selection criteria for the data and the EPOS model were varied in the range of ± 10 cm (50%) around the nominal value.

(ii) Methods of track selection.

To estimate systematic uncertainty related to the track selection the following variations were performed independently: number of requested points on a track in all TPCs was changed by ± 5 (33% of the standard selection), number of requested points on a track in the VTTPCs was reduced and increased by 5 (18% of the criterion).

(iii) Identification techniques.

Moreover, uncertainties of the dE/dx identification method were studied and estimated by a 10% variation of the parameter constraints for the function Eq. (1) used for particle identification. In case of tof - dE/dx identification uncertainties were estimated by changing the selection criteria related to this technique – the last point of the track should be in the last 2 ± 1 padrows of the MTPC, the QDC signal is or is not required.

(iv) FeedException correction.

The determination of the feedException correction is based on the EPOS model which describes well the available cross section data for strange particles (see e.g. for Λ at 158 GeV/c Ref. [22] and at 40 GeV/c Ref. [23] and Figs. 23 and 24 in this paper for K^+ and K^-). Systematic uncertainty comes from the lack of precise knowledge of the production cross section of K^+ , K^- , Λ , Σ^+ , Σ^- , K_s^0 and $\bar{\Lambda}$ in case of pions, and in addition of Σ^+ in case of protons, and $\bar{\Lambda}$ in case of antiprotons. Since the corrections are only at the level of a few percent in the phase space region of the measurements a small additional systematic error of 1% was assumed in case of pions and 2% for protons and antiprotons.

The components of the systematic uncertainty and the total for the dE/dx and tof - dE/dx methods, for a selected p_T interval and beam momenta of 20 and 158 GeV/c are presented in Figs. 16, 17, 18 and 19. Assuming independence of all systematic error sources, the total systematic uncertainty was calculated as the square root of the sum of squares of the described components.

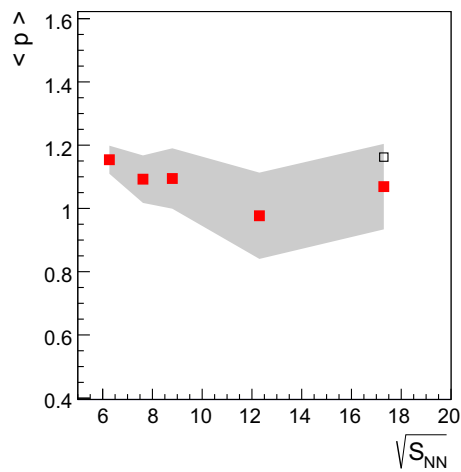


Fig. 38 Mean proton multiplicities produced in inelastic p + p interactions as a function of collision energy. Filled red squares depict results from this analysis, the open black square shows the measurement of NA49 [12]. The dominating uncertainty of the NA61/SHINE measurements is systematic and is indicated by the shaded band

Production of positive and negative pions, kaons and protons in p + p interactions at 158 GeV/c was measured before by the NA49 experiment [11–13]. Comparison of NA61/SHINE and NA49 rapidity distributions is presented in Fig. 20. The results are consistent within the systematic uncertainty.

The NA61/SHINE experiment also published π^- spectra obtained by the so-called h^- [3] analysis procedure. This technique is based on the fact that the majority of negatively charged particles are π^- mesons. The contribution of the other particles was subtracted using predictions of the EPOS model. Comparison of rapidity spectra from the h^- method with those obtained in this publication using particle identification is shown in Fig. 21. Both methods give results for π^- spectra which agree within uncertainties.

Spectra measured in p + p interactions should obey reflection symmetry with respect to mid-rapidity. As the NA61/SHINE acceptance extends somewhat below mid-rapidity a test of the reflection symmetry can be performed to check the consistency of the measurements. As examples these reflection tests are presented in Fig. 22 in selected p_T intervals for positively and negatively charged kaons, antiprotons and protons produced at 20 and 158 GeV/c. One observes that the yields measured for $y < 0$ agree with those measured for $y > 0$ in the reflected acceptance within uncertainties.

The EPOS model was chosen as the event generator in the simulation chain to calculate corrections. Figures 23 and 24 present EPOS model predictions and experimental results obtained in this analysis in selected rapidity intervals for inelastic p + p interactions at 20 and 158 GeV/c. The EPOS model describes well particle production in p + p interactions

at 20 GeV/c and at 158 GeV/c. Since the corrections were applied differentially in rapidity and transverse momentum bins the effect of minor discrepancies are not expected to cause significant biases.

4 Results

4.1 Spectra

Two dimensional distributions normalised per event (y vs. p_T) of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic p + p interactions at different SPS energies are presented in Fig. 25. Where available, results from the dE/dx methods were used because of their smaller statistical uncertainties. Results from the tof - dE/dx method were taken to extend the phase space coverage. Anti-proton yields at 20 GeV/c could not be determined due to the insufficient statistics of the collected data. Empty bins in phase-space (mostly for lower energies) are caused by insufficient acceptance for the methods used in the analysis. Yields for all particle types except protons are seen to increase with beam momentum in the SPS energy range.

The measurements shown in Fig. 25 were studied as a function of transverse momentum (p_T) in intervals of rapidity (y). Resulting double differential spectra of K^- , K^+ , π^- , π^+ , p and \bar{p} produced in p + p interactions at 20, 31, 40, 80, 158 GeV/c are plotted in Figs. 26, 27, 28, 29, 30 and 31, respectively. Spectra in successive rapidity intervals were scaled by appropriate factors for better visibility. Vertical bars on data points correspond to statistical, shaded bands to systematic uncertainties.

Results presented in Figs. 26, 27, 28, 29, 30 and 31 were parametrized by the exponential function [24,25]:

$$\frac{d^2n}{dp_T dy} = \frac{S c^2 p_T}{T^2 + m T} \exp(-(m_T - m)/T), \quad (19)$$

where m is the particle mass and S and T are the yield integral and the inverse slope parameter, respectively. Examples of this parametrization fitted to K^+ and K^- spectra at mid-rapidity are presented in Fig. 32. The obtained values of the inverse slope parameter for all spectra shown in Figs. 26, 27, 28, 29, 30 and 31 are plotted in Fig. 33 as function of the rapidity for four beam momenta 31, 40, 80 and 158 GeV/c. Note that results are only plotted for those rapidity intervals for which there were more than 6 data points in the p_T -distribution.

Rapidity distributions were then obtained by integrating the transverse momentum spectra also using reflection symmetry around mid-rapidity ($y = 0$). Extrapolation to unmeasured regions in p_T was performed in rapidity intervals using fits with function Eq. (19) where results were reliable (number of measured p_T points higher than 6). In the other rapidity

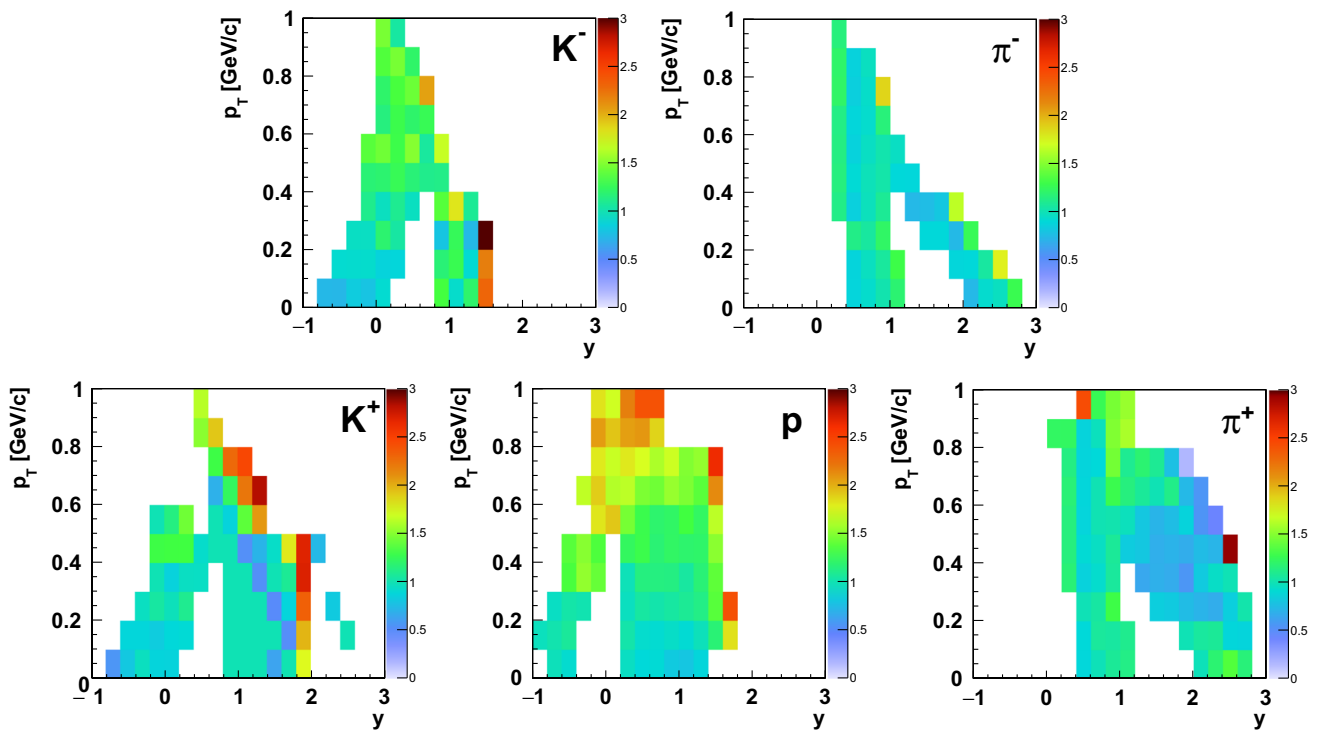


Fig. 39 Two dimensional distributions $d^2n/(dp_T dy)$ of π^- , π^+ , K^- , K^+ and p produced in inelastic $p + p$ interactions at 20 GeV/c divided by the EPOS model [21] calculations

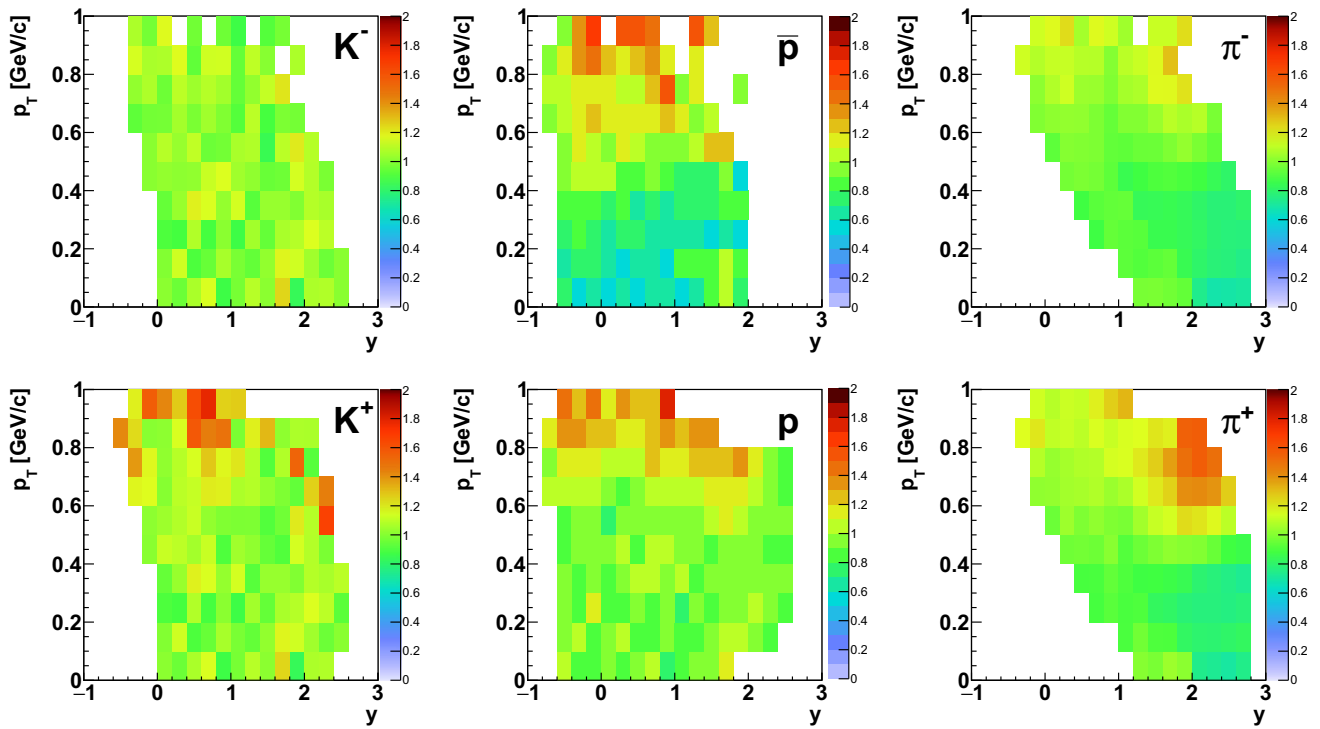


Fig. 40 Two dimensional distributions $d^2n/(dp_T dy)$ of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic $p + p$ interactions at 158 GeV/c divided by the EPOS model [21] calculations

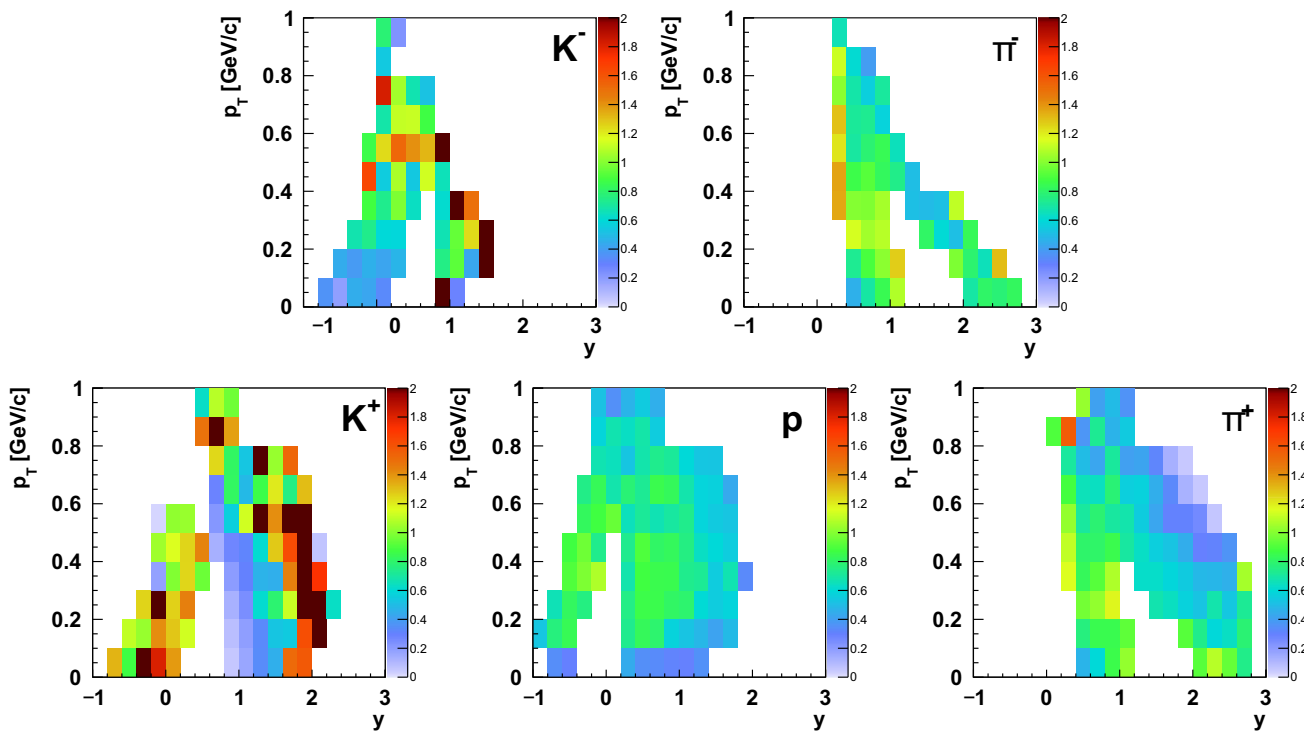


Fig. 41 Two dimensional distributions $d^2n/(dp_T dy)$ of π^- , π^+ , K^- , K^+ and p produced in inelastic $p + p$ interactions at 20 GeV/c divided by the UrQMD 3.4 model [27,28] calculations

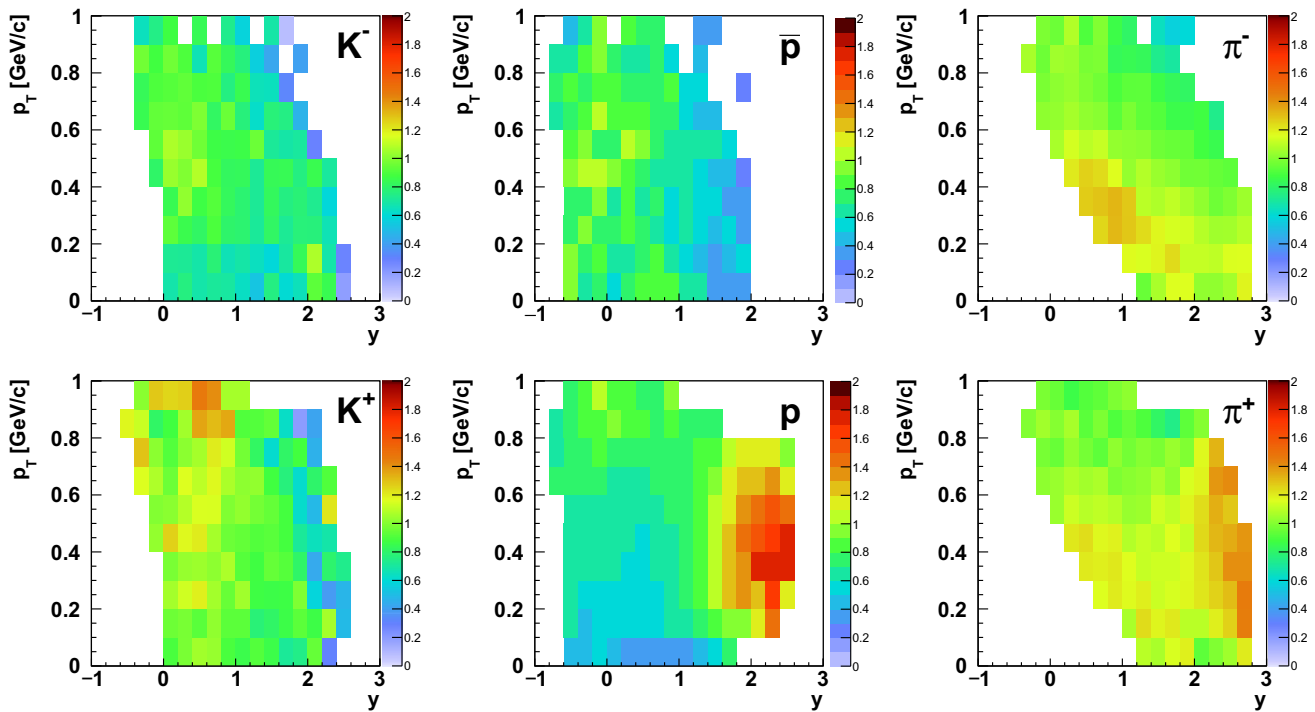


Fig. 42 Two dimensional distributions $d^2n/(dp_T dy)$ of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic $p + p$ interactions at 158 GeV/c divided by the UrQMD 3.4 model [27,28] calculations

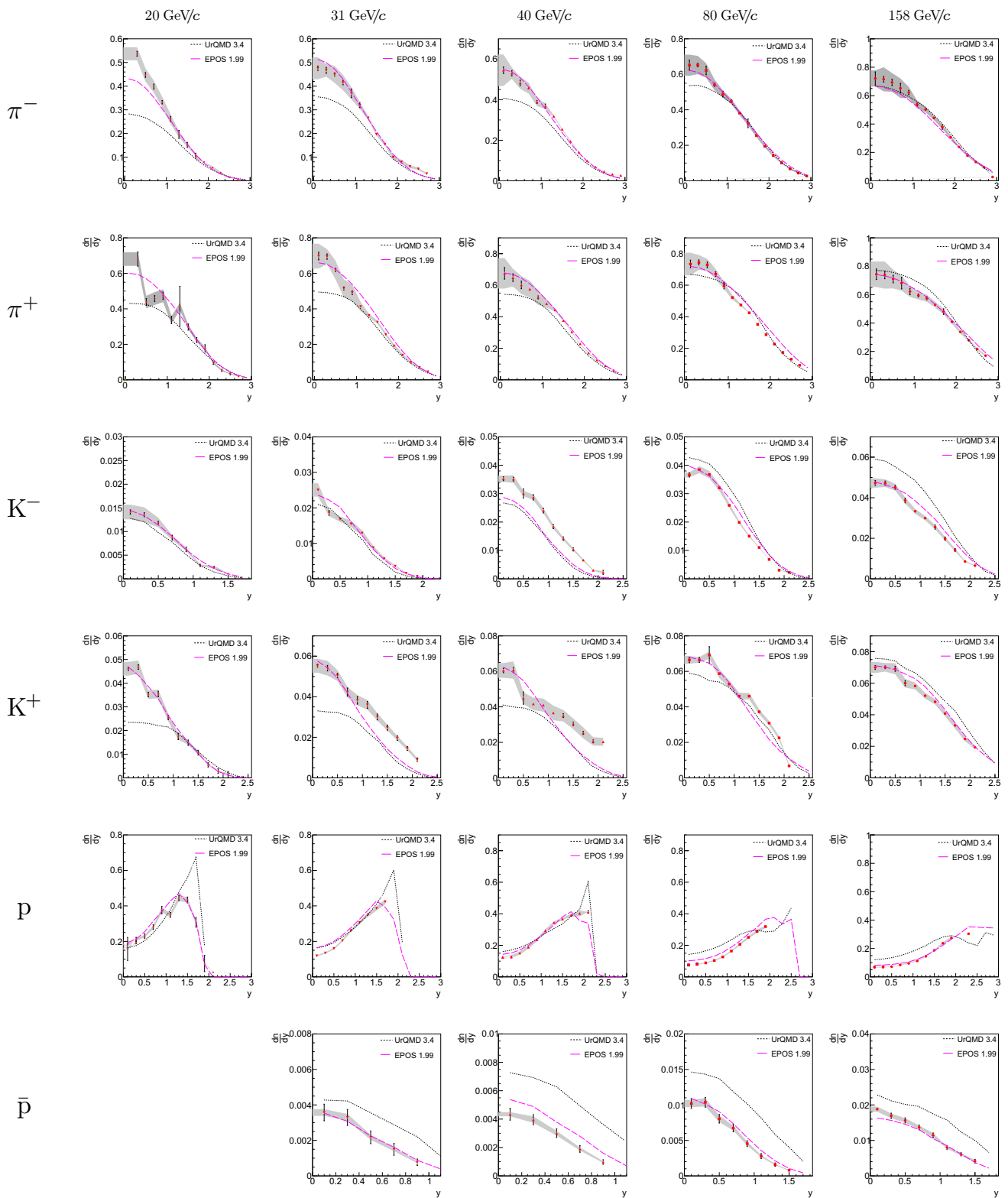
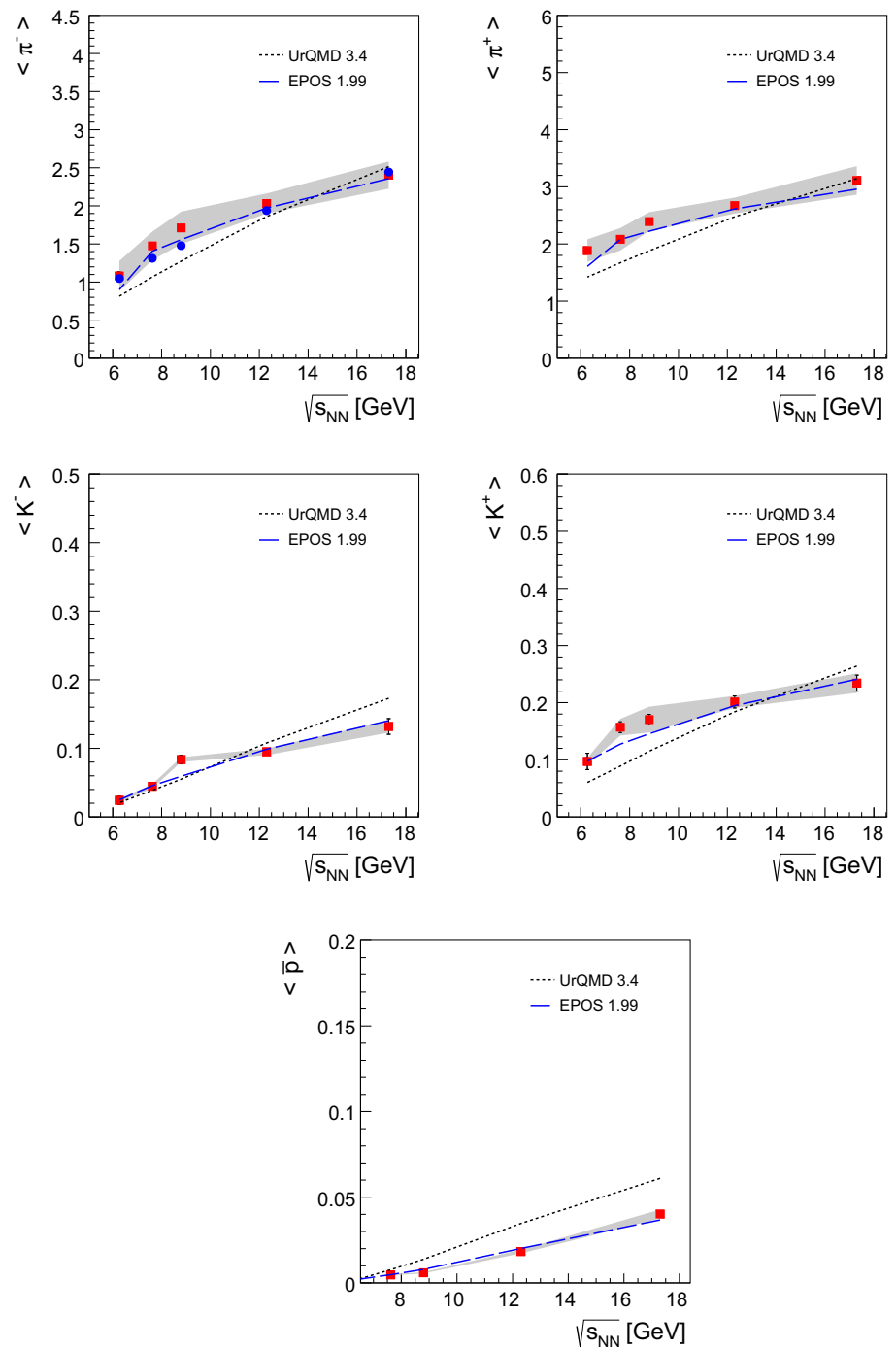


Fig. 43 Rapidity distribution of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic $p + p$ interactions at 20, 31, 40, 80 and 158 GeV/c compared with predictions of the EPOS [21] (dashed lines) and UrQMD [27,28] (dotted lines) models

Fig. 44 Mean multiplicity of π^- , π^+ , K^- , K^+ and \bar{p} multiplicity produced in inelastic p + p interactions as a function of collision energy. Measurements of NA61/SHINE are plotted as filled red squares, EPOS [21] and UrQMD [27,28] models predictions are shown as dashed and dotted lines, respectively. Additionally, blue filled circles correspond to previously published results obtained by NA61/SHINE via the h^- method [3]. Statistical uncertainties are indicated by bars, systematic uncertainties of the NA61/SHINE measurements by shaded bands



intervals the yield was obtained by summing the measured values and multiplying the result by an extrapolation factor calculated from the EPOS model. This factor was taken as the ratio of the integrated yield in the rapidity interval to that in the region of the measurements. The results are shown in Fig. 34. Statistical uncertainties, indicated by vertical bars, were calculated as the square root of the sum of the squares of statistical errors of the summed bins. Systematic uncertainties (shaded bands) were calculated by varying the uncer-

tainty sources described in Sect. 3.4.3 and adding half of the extrapolated yield.

4.2 Mean multiplicities

Next, mean multiplicities produced in the forward region $y > 0$ were calculated by integrating the rapidity distributions shown in Fig. 34. The distributions are seen to be nearly Gaussian at all energies except for protons. In order to obtain

a good description of the data points, fits were performed with a sum of two identical Gaussian functions with mean position symmetrically displaced around mid-rapidity. The integrated result was taken as the sum of measured values plus a contribution from the unmeasured region obtained from the fit function. The statistical uncertainty is obtained as the square root of the sum of squares of statistical uncertainties of the measured data points and the square of the statistical error of the extrapolation. The systematic uncertainty was estimated by repeating the complete analysis procedure by varying the components described in Sect. 3.4.3. Doubling of the results gives the 4π multiplicities which are listed in Table 4 for π^+ , K^+ and p and in Table 5 for π^- , K^- and \bar{p} .

The determination of 4π multiplicity is more complicated for protons due to the rapid rise of the yield towards beam rapidity and the lack of measurements in this region. A comparison of the rapidity distributions obtained in this analysis with measurements of the NA49 experiment [26] and calculations using the UrQMD [27,28] and EPOS [21] models at 158 GeV/c beam momentum is shown in Fig. 35. One observes that the models do not describe well the measurements at highest rapidities at this beam energy. Nevertheless, the models were used to extrapolate the proton yields into the unmeasured region since they provide predictions at all beam energies. Extrapolation factors were calculated from the models as the ratio of total multiplicity to that in the region covered by the measurements. The average of the two model results was then used for extrapolating the measured yield to 4π phase space. The difference between results obtained using the UrQMD and EPOS models was added to the systematic uncertainty. Final results for protons are given in Table 4.

4.2.1 Energy dependence of mean multiplicities

The energy dependence of total charged kaon multiplicities produced in inelastic $p + p$ collisions is presented in Fig. 36. One observes a steep threshold rise and a clear flattening above about 8 GeV for both K^+ and K^- . The new NA61/SHINE measurements (filled red squares) agree with the world data (open circles) and locate the change of slope due to the high precision of the actual measurement.

The energy dependence of the NA61/SHINE measurements of charged pion multiplicities $\langle\pi^+\rangle$ and $\langle\pi^-\rangle$ produced in inelastic $p + p$ collisions is compared in Fig. 37 to that of the world data [11,37–43]. Clearly the NA61/SHINE results (filled red squares, filled blue dots) are consistent with measurements published in the literature (open squares). Also the NA61/SHINE measurements for $\langle\pi^-\rangle$ obtained with the identification method (filled red squares) and the h^- method [3] (blue dots) agree. It can be seen, that $\langle\pi^+\rangle$ and $\langle\pi^-\rangle$ increase smoothly with the collision energy. The rate of the increase gradually diminishes with increasing energy. The energy

dependence of the charged pion multiplicity is qualitatively similar to that of charged kaons.

For the determination of total proton multiplicities large acceptance over a full hemisphere of the reaction is particularly important. Due to this feature NA61/SHINE and NA49 were able to provide such measurements in the SPS energy range. The total proton multiplicity in inelastic $p + p$ collisions is presented in Fig. 38 as function of collision energy. One observes that the proton yield is almost constant at SPS energies.

5 Comparison with hadron production models

This section compares the NA61/SHINE measurements with predictions from the publicly available codes of the microscopic models EPOS 1.99 [21] and UrQMD 3.4 [27,28]. In EPOS the reaction proceeds via excitation of strings according to Gribov–Regge theory which subsequently fragment into hadrons. UrQMD generates a hadron cascade using elementary cross sections and supplements this process by string production and fragmentation at higher energies.

Two dimensional distributions $d^2n/(dp_T dy)$ of π^- , π^+ , K^- , K^+ , p and \bar{p} produced in inelastic $p + p$ interactions divided by the EPOS model prediction are presented in Fig. 39 at 20 GeV/c and in Fig. 40 at 158 GeV/c and divided by the UrQMD model calculations in Fig. 41 at 20 GeV/c and in Fig. 42 at 158 GeV/c.

As demonstrated by Figs. 39 and 40 the EPOS model provides a good description of the measurements in most regions of phase space. Only at larger transverse momenta,

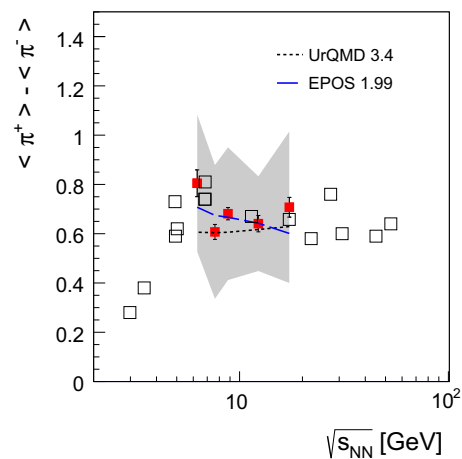


Fig. 45 Difference $\langle\pi^+\rangle - \langle\pi^-\rangle$ in inelastic $p + p$ interactions as function of collision energy. Solid red squares depict NA61/SHINE results from this analysis, open squares show previously published measurements [11,37,38,44]. Statistical uncertainties of the NA61/SHINE results are indicated by bars, systematic uncertainties by the shaded band. The EPOS [21] and UrQMD [27,28] model predictions are shown as dashed and dotted lines, respectively

where particle yields are low, some underprediction occurs. This conclusion is supported by Figs. 23 and 24 which show projected p_T distributions in selected rapidity intervals.

Comparison of the UrQMD 3.4 calculations with the NA61/SHINE measurements show larger discrepancies as seen in Figs. 41, 42 and 43. There are regions of underprediction for K^+ at lower energies and overprediction for K^- at higher energies and especially \bar{p} at all collision energies.

Comparison of the measured rapidity distributions with predictions of both models are shown in Fig. 43. The total multiplicities π^- , π^+ , K^- , K^+ and \bar{p} as function of collision energy are presented and compared in Fig. 44. The EPOS 1.99 model provides a reasonable description of the NA61/SHINE measurements, while significant discrepancies are evident for the UrQMD 3.4 calculations.

Additionally the difference $\langle \pi^+ \rangle - \langle \pi^- \rangle$ is presented as function of collision energy in Fig. 45. It can be observed that this value is almost independent of collision energy. The NA61/SHINE results agree with the measurements of previous experiments. Both EPOS and UrQMD model predictions are consistent with the measurements.

6 Summary and outlook

Spectra and multiplicities of π^+ , π^- , K^+ , K^- , p and \bar{p} produced in inelastic $p + p$ interactions were measured with the NA61/SHINE spectrometer at beam momenta of 20, 31, 40, 80, 158 GeV/c at the CERN SPS. New probabilistic analysis techniques based on the energy loss dE/dx in the TPCs and the combination of the measurement of time of flight and energy loss $tof-dE/dx$ were employed. Statistical and systematic uncertainties were carefully evaluated. The NA61/SHINE results significantly improve the world data both in precision and momentum coverage. The EPOS 1.99 model [21] provides a good description of the measurements in the SPS energy range, while predictions of the UrQMD 3.4 model [27,28] significantly differ from the data.

The new NA61/SHINE measurements of particle production in inelastic $p + p$ collisions provide the baseline for the systematic study of the system size dependence of the onset

of deconfinement observed by the NA49 experiment in central Pb + Pb collisions in the SPS energy range. In the nearest future the NA61/SHINE collaboration will extend the $p + p$ energy scan by results from $p + p$ interactions at 400 GeV/c beam momentum.

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A. ToF correction factors

See Figs. 46, 47 and 48.

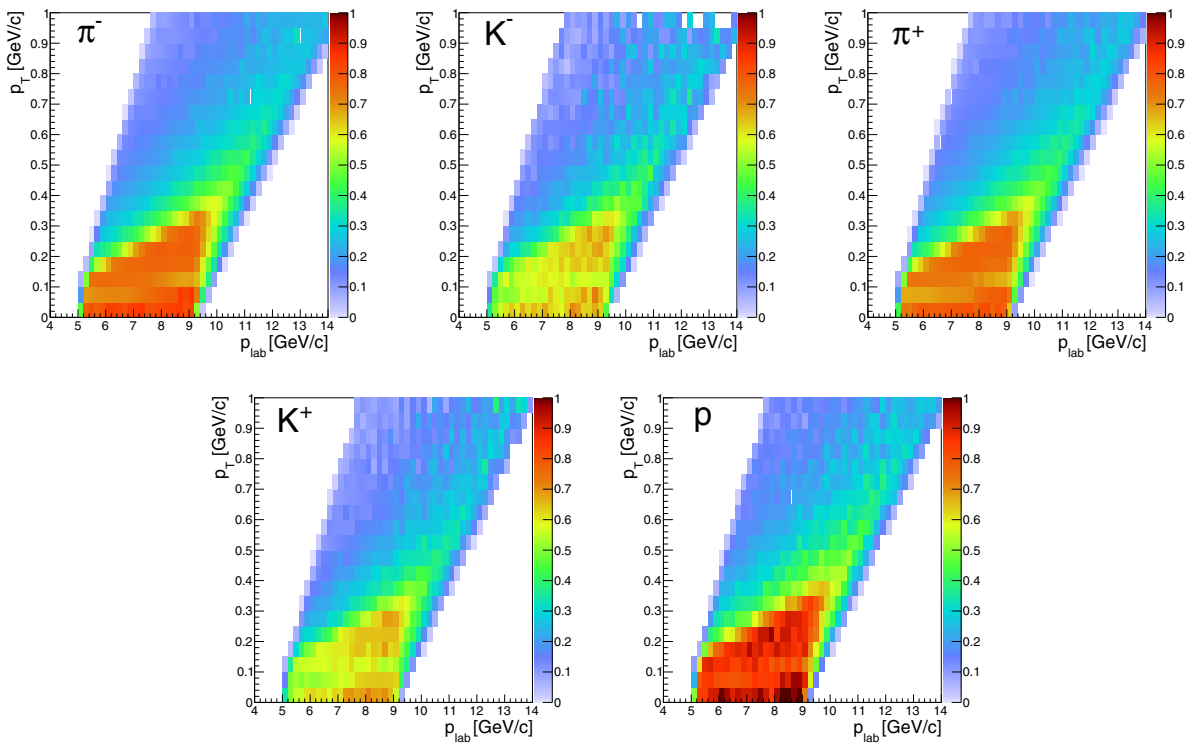


Fig. 46 Acceptance for tracks extrapolating to a pixel of the ToF-L or ToF-R walls and having a last measured point in the two last padrows of the MTPC for p + p interactions at 158 GeV/c

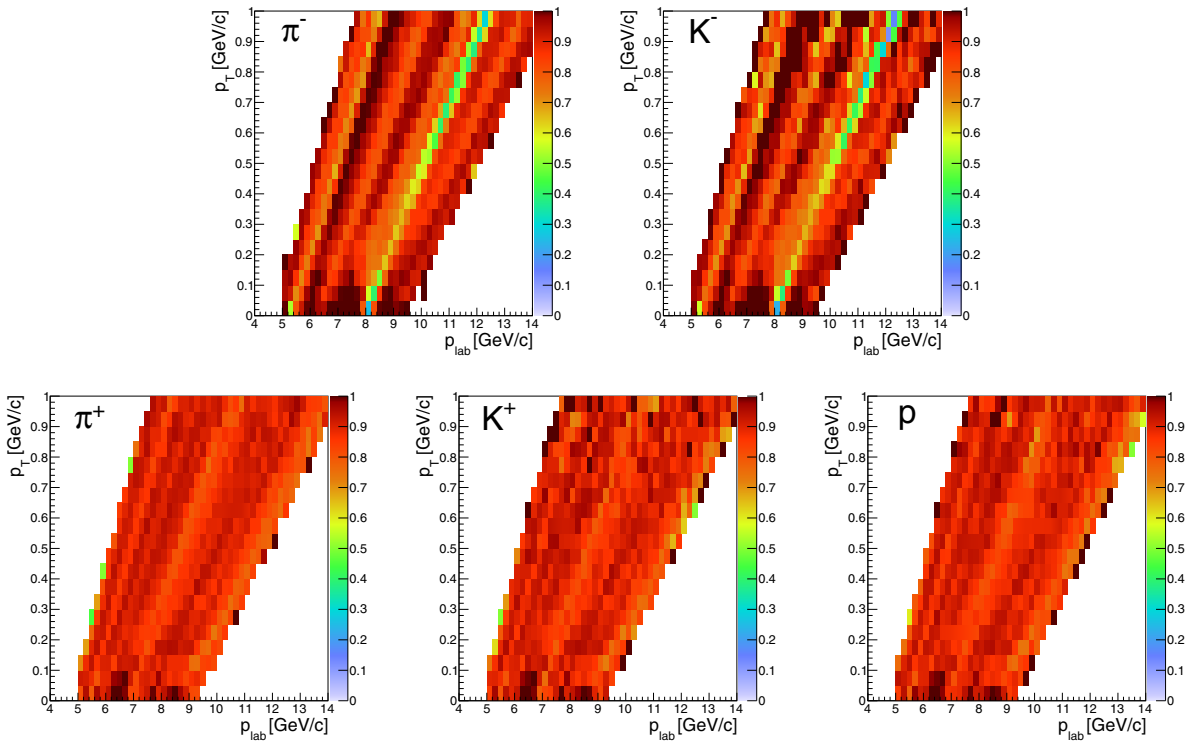


Fig. 47 Fraction of pixels providing a valid ToF measurement for p + p interactions at 158 GeV/c. Visible strips with lower value are due to groups of not working pixels

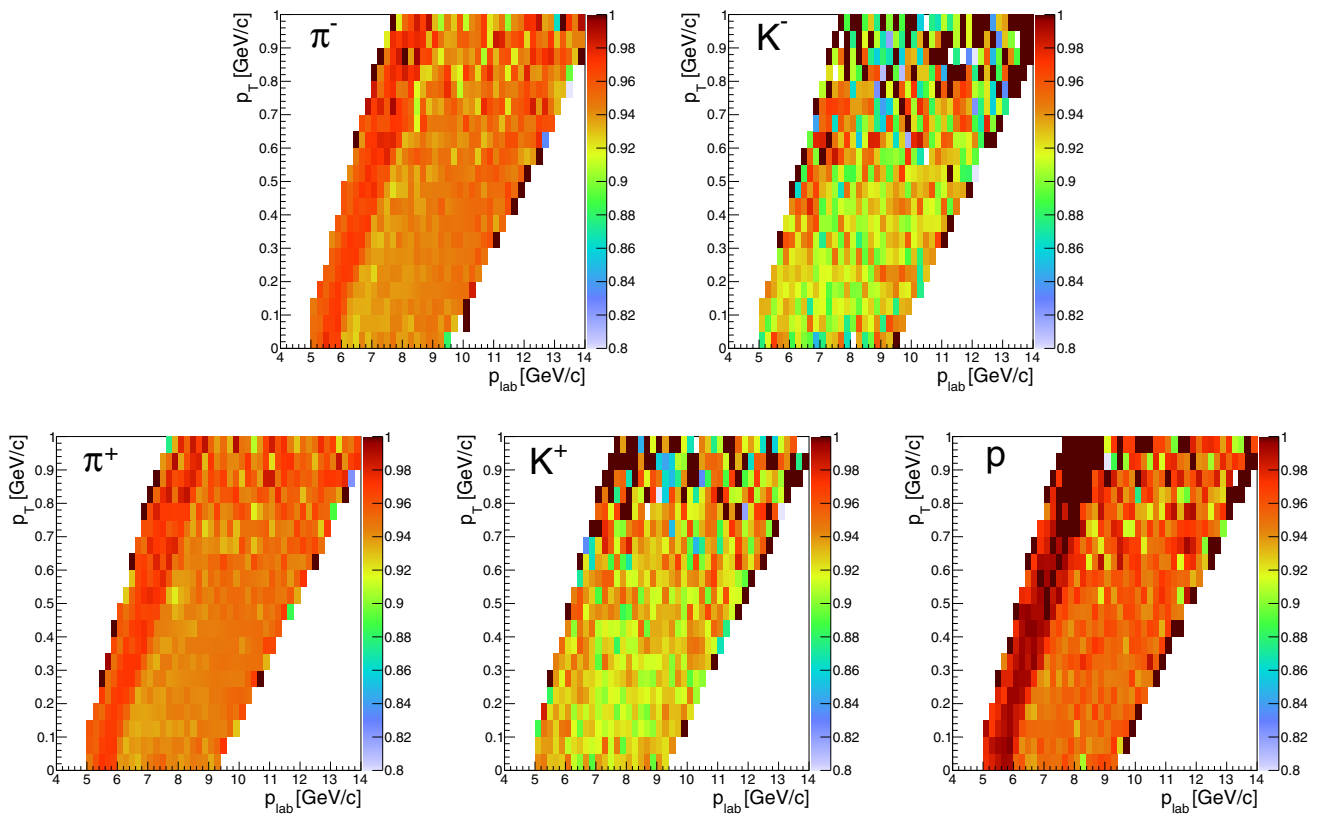


Fig. 48 Survival probability of tracks between the last measured point in the MTPC and the ToF-L or ToF-R walls for p + p interactions at 158 GeV/c

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