

Interpretation of the Depths of Maximum of Extensive Air Showers Measured by the Pierre Auger Observatory

The Pierre Auger Collaboration

P. Abreu⁶¹, M. Aglietta⁴⁹, M. Ahlers⁹⁰, E.J. Ahn⁷⁸,
I.F.M. Albuquerque¹⁵, I. Allekotte¹, J. Allen⁸², P. Allison⁸⁴,
A. Almela^{11, 7}, J. Alvarez Castillo⁵⁴, J. Alvarez-Muñiz⁷¹, R. Alves
Batista¹⁶, M. Ambrosio⁴³, A. Aminaei⁵⁵, L. Anchordoqui⁹¹,
S. Andringa⁶¹, T. Antičić²², C. Aramo⁴³, F. Arqueros⁶⁸, H. Asorey¹,
P. Assis⁶¹, J. Aublin²⁸, M. Ave⁷¹, M. Avenier²⁹, G. Avila¹⁰,
A.M. Badescu⁶⁴, K.B. Barber¹², A.F. Barbosa^{13 ‡}, R. Bardenet²⁷,
B. Baughman^{84 c}, J. Bäuml³³, C. Baus³⁵, J.J. Beatty⁸⁴,
K.H. Becker³², A. Bellétoile³¹, J.A. Bellido¹², S. BenZvi⁹⁰,
C. Berat²⁹, X. Bertou¹, P.L. Biermann³⁶, P. Billoir²⁸, F. Blanco⁶⁸,
M. Blanco²⁸, C. Bleve³², H. Blümer^{35, 33}, M. Boháčová²⁴,
D. Boncioli⁴⁴, C. Bonifazi²⁰, R. Bonino⁴⁹, N. Borodai⁵⁹, J. Brack⁷⁶,
I. Brancus⁶², P. Brogueira⁶¹, W.C. Brown⁷⁷, P. Buchholz³⁹,
A. Bueno⁷⁰, L. Buroker⁹¹, R.E. Burton⁷⁴, M. Buscemi⁴³,
K.S. Caballero-Mora^{71, 85}, B. Caccianiga⁴², L. Caccianiga²⁸,
L. Caramete³⁶, R. Caruso⁴⁵, A. Castellina⁴⁹, G. Cataldi⁴⁷,
L. Cazon⁶¹, R. Cester⁴⁶, S.H. Cheng⁸⁵, A. Chiavassa⁴⁹,
J.A. Chinellato¹⁶, J. Chudoba²⁴, M. Cilmo⁴³, R.W. Clay¹²,
G. Cocciolo⁴⁷, R. Colalillo⁴³, L. Collica⁴², M.R. Coluccia⁴⁷,
R. Conceição⁶¹, F. Contreras⁹, H. Cook⁷², M.J. Cooper¹²,
J. Coppens^{55, 57}, S. Coutu⁸⁵, C.E. Covault⁷⁴, A. Criss⁸⁵, J. Cronin⁸⁶,
A. Curutiu³⁶, R. Dallier^{31, 30}, B. Daniel¹⁶, S. Dasso^{5, 3},
K. Daumiller³³, B.R. Dawson¹², R.M. de Almeida²¹, M. De
Domenico⁴⁵, S.J. de Jong^{55, 57}, G. De La Vega⁸, W.J.M. de Mello
Junior¹⁶, J.R.T. de Mello Neto²⁰, I. De Mitri⁴⁷, V. de Souza¹⁴,
K.D. de Vries⁵⁶, L. del Peral⁶⁹, O. Deligny²⁶, H. Dembinski³³,

N. Dhital⁸¹, C. Di Giulio⁴⁴, J.C. Diaz⁸¹, M.L. Díaz Castro¹³,
P.N. Diep⁹², F. Diogo⁶¹, C. Dobrigkeit¹⁶, W. Docters⁵⁶,
J.C. D'Olivo⁵⁴, P.N. Dong^{92, 26}, A. Dorofeev⁷⁶, J.C. dos Anjos¹³,
M.T. Dova⁴, D. D'Urso⁴³, J. Ebr²⁴, R. Engel³³, M. Erdmann³⁷,
C.O. Escobar^{78, 16}, J. Espadanal⁶¹, A. Etchegoyen^{7, 11}, P. Facal San
Luis⁸⁶, H. Falcke^{55, 58, 57}, K. Fang⁸⁶, G. Farrar⁸², A.C. Fauth¹⁶,
N. Fazzini⁷⁸, A.P. Ferguson⁷⁴, B. Fick⁸¹, J.M. Figueira⁷,
A. Filevich⁷, A. Filipčič^{65, 66}, S. Fliescher³⁷, B.D. Fox⁸⁷,
C.E. Fracchiolla⁷⁶, E.D. Fraenkel⁵⁶, O. Fratu⁶⁴, U. Fröhlich³⁹,
B. Fuchs³⁵, R. Gaior²⁸, R.F. Gamarra⁷, S. Gambetta⁴⁰, B. García⁸,
S.T. Garcia Roca⁷¹, D. Garcia-Gamez²⁷, D. Garcia-Pinto⁶⁸,
G. Garilli⁴⁵, A. Gascon Bravo⁷⁰, H. Gemmeke³⁴, P.L. Ghia²⁸,
M. Giller⁶⁰, J. Gitto⁸, C. Glaser³⁷, H. Glass⁷⁸, G. Golup¹, F. Gomez
Albarracin⁴, M. Gómez Berisso¹, P.F. Gómez Vitale¹⁰,
P. Gonçalves⁶¹, J.G. Gonzalez³⁵, B. Gookin⁷⁶, A. Gorgi⁴⁹,
P. Gorham⁸⁷, P. Gouffon¹⁵, S. Grebe^{55, 57}, N. Griffith⁸⁴,
A.F. Grillo⁵⁰, T.D. Grubb¹², Y. Guardincerri³, F. Guarino⁴³,
G.P. Guedes¹⁷, P. Hansen⁴, D. Harari¹, T.A. Harrison¹²,
J.L. Harton⁷⁶, A. Haungs³³, T. Hebbeker³⁷, D. Heck³³,
A.E. Herve¹², G.C. Hill¹², C. Hojvat⁷⁸, N. Hollon⁸⁶, V.C. Holmes¹²,
P. Homola⁵⁹, J.R. Hörandel^{55, 57}, P. Horvath²⁵, M. Hrabovský^{25, 24},
D. Huber³⁵, T. Huege³³, A. Insolia⁴⁵, F. Ionita⁸⁶, S. Jansen^{55, 57},
C. Jarne⁴, S. Jiraskova⁵⁵, M. Josebachuili⁷, K. Kadija²²,
K.H. Kampert³², P. Karhan²³, P. Kasper⁷⁸, I. Katkov³⁵, B. Kégl²⁷,
B. Keilhauer³³, A. Keivani⁸⁰, J.L. Kelley⁵⁵, E. Kemp¹⁶,
R.M. Kieckhafer⁸¹, H.O. Klages³³, M. Kleifges³⁴, J. Kleinfeller^{9, 33},
J. Knapp⁷², K. Kotera⁸⁶, R. Krause³⁷, N. Krohm³², O. Krömer³⁴,
D. Kruppke-Hansen³², D. Kuempel^{37, 39}, J.K. Kulbartz³⁸,
N. Kunka³⁴, G. La Rosa⁴⁸, D. LaHurd⁷⁴, L. Latronico⁴⁹, R. Lauer⁸⁹,
M. Lauscher³⁷, P. Lautridou³¹, S. Le Coz²⁹, M.S.A.B. Leão¹⁹,
D. Lebrun²⁹, P. Lebrun⁷⁸, M.A. Leigui de Oliveira¹⁹,
A. Letessier-Selvon²⁸, I. Lhenry-Yvon²⁶, K. Link³⁵, R. López⁵¹,
A. Lopez Agüera⁷¹, K. Louedec^{29, 27}, J. Lozano Bahilo⁷⁰, L. Lu⁷²,
A. Lucero⁷, M. Ludwig³⁵, H. Lyberis^{20, 26}, M.C. Maccarone⁴⁸,
C. Macolino²⁸, M. Malacari¹², S. Maldera⁴⁹, J. Maller³¹,
D. Mandat²⁴, P. Mantsch⁷⁸, A.G. Mariazzi⁴, J. Marin^{9, 49},
V. Marin³¹, I.C. Mariş²⁸, H.R. Marquez Falcon⁵³, G. Marsella⁴⁷,
D. Martello⁴⁷, L. Martin^{31, 30}, H. Martinez⁵², O. Martínez Bravo⁵¹,
D. Martraire²⁶, J.J. Masías Meza³, H.J. Mathes³³, J. Matthews⁸⁰,

J.A.J. Matthews⁸⁹, G. Matthiae⁴⁴, D. Maurel³³, D. Maurizio^{13, 46},
E. Mayotte⁷⁵, P.O. Mazur⁷⁸, G. Medina-Tanco⁵⁴, M. Melissas³⁵,
D. Melo⁷, E. Menichetti⁴⁶, A. Menshikov³⁴, S. Messina⁵⁶,
R. Meyhandan⁸⁷, S. Mićanović²², M.I. Micheletti⁶,
L. Middendorf³⁷, I.A. Minaya⁶⁸, L. Miramonti⁴², B. Mitrica⁶²,
L. Molina-Bueno⁷⁰, S. Mollerach¹, M. Monasor⁸⁶, D. Monnier
Ragaine²⁷, F. Montanet²⁹, B. Morales⁵⁴, C. Morello⁴⁹,
J.C. Moreno⁴, M. Mostafá⁷⁶, C.A. Moura¹⁹, M.A. Muller¹⁶,
G. Müller³⁷, M. Münchmeyer²⁸, R. Mussa⁴⁶, G. Navarra^{49 †},
J.L. Navarro⁷⁰, S. Navas⁷⁰, P. Necesar²⁴, L. Nellen⁵⁴, A. Nelles^{55, 57},
J. Neuser³², P.T. Nhung⁹², M. Niechciol³⁹, L. Niemietz³²,
N. Nierstenhoefer³², T. Niggemann³⁷, D. Nitz⁸¹, D. Nosek²³,
L. Nožka²⁴, J. Oehlschläger³³, A. Olinto⁸⁶, M. Oliveira⁶¹,
M. Ortiz⁶⁸, N. Pacheco⁶⁹, D. Pakk Selmi-Dei¹⁶, M. Palatka²⁴,
J. Pallotta², N. Palmieri³⁵, G. Parente⁷¹, A. Parra⁷¹, S. Pastor⁶⁷,
T. Paul^{91, 83}, M. Pech²⁴, J. Pękala⁵⁹, R. Pelayo^{51, 71}, I.M. Pepe¹⁸,
L. Perrone⁴⁷, R. Pesce⁴⁰, E. Petermann⁸⁸, S. Petrera⁴¹,
A. Petrolini⁴⁰, Y. Petrov⁷⁶, C. Pfendner⁹⁰, R. Piegaiá³, T. Pierog³³,
P. Pieroni³, M. Pimenta⁶¹, V. Pirronello⁴⁵, M. Platino⁷, M. Plum³⁷,
V.H. Ponce¹, M. Pontz³⁹, A. Porcelli³³, P. Privitera⁸⁶, M. Prouza²⁴,
E.J. Quel², S. Querchfeld³², J. Rautenberg³², O. Ravel³¹,
D. Ravnani⁷, B. Revenu³¹, J. Ridky²⁴, S. Riggi^{48, 71}, M. Risse³⁹,
P. Ristori², H. Rivera⁴², V. Rizi⁴¹, J. Roberts⁸², W. Rodrigues de
Carvalho⁷¹, I. Rodriguez Cabo⁷¹, G. Rodriguez Fernandez^{44, 71},
J. Rodriguez Martino⁹, J. Rodriguez Rojo⁹,
M.D. Rodríguez-Frías⁶⁹, G. Ros⁶⁹, J. Rosado⁶⁸, T. Rossler²⁵,
M. Roth³³, B. Rouillé-d'Orfeuille⁸⁶, E. Roulet¹, A.C. Rovero⁵,
C. Rühle³⁴, S.J. Saffi¹², A. Saftoiu⁶², F. Salamida²⁶, H. Salazar⁵¹,
F. Salesa Greus⁷⁶, G. Salina⁴⁴, F. Sánchez⁷, C.E. Santo⁶¹,
E. Santos⁶¹, E.M. Santos²⁰, F. Sarazin⁷⁵, B. Sarkar³², R. Sato⁹,
N. Scharf³⁷, V. Scherini⁴², H. Schieler³³, P. Schiffer³⁸,
A. Schmidt³⁴, O. Scholten⁵⁶, H. Schoorlemmer^{55, 57},
J. Schovancova²⁴, P. Schovánek²⁴, F. Schröder³³, J. Schulz⁵⁵,
D. Schuster⁷⁵, S.J. Sciutto⁴, M. Scuderi⁴⁵, A. Segreto⁴⁸,
M. Settimo^{39, 47}, A. Shadkam⁸⁰, R.C. Shellard¹³, I. Sidelnik¹,
G. Sigl³⁸, O. Sima⁶³, A. Śmiałkowski⁶⁰, R. Šmída³³, G.R. Snow⁸⁸,
P. Sommers⁸⁵, J. Sorokin¹², H. Spinka^{73, 78}, R. Squartini⁹,
Y.N. Srivastava⁸³, S. Stanić⁶⁶, J. Stapleton⁸⁴, J. Stasielak⁵⁹,
M. Stephan³⁷, M. Straub³⁷, A. Stutz²⁹, F. Suarez⁷, T. Suomijärvi²⁶,

**A.D. Supanitsky⁵, T. Šuša²², M.S. Sutherland⁸⁰, J. Swain⁸³,
 Z. Szadkowski⁶⁰, M. Szuba³³, A. Tapia⁷, M. Tartare²⁹, O. Taşcău³²,
 R. Tcaciuc³⁹, N.T. Thao⁹², D. Thomas⁷⁶, J. Tiffenberg³,
 C. Timmermans^{57, 55}, W. Tkaczyk^{60 †}, C.J. Todero Peixoto¹⁴,
 G. Toma⁶², L. Tomankova²⁴, B. Tomé⁶¹, A. Tonachini⁴⁶,
 G. Torralba Elipe⁷¹, D. Torres Machado³¹, P. Travnicek²⁴,
 D.B. Tridapalli¹⁵, E. Trovato⁴⁵, M. Tueros⁷¹, R. Ulrich³³,
 M. Unger³³, M. Urban²⁷, J.F. Valdés Galicia⁵⁴, I. Valiño⁷¹,
 L. Valore⁴³, G. van Aar⁵⁵, A.M. van den Berg⁵⁶, S. van Velzen⁵⁵,
 A. van Vliet³⁸, E. Varela⁵¹, B. Vargas Cárdenas⁵⁴, G. Varner⁸⁷,
 J.R. Vázquez⁶⁸, R.A. Vázquez⁷¹, D. Veberič^{66, 65}, V. Verzi⁴⁴,
 J. Vicha²⁴, M. Videla⁸, L. Villaseñor⁵³, H. Wahlberg⁴,
 P. Wahrlich¹², O. Wainberg^{7, 11}, D. Walz³⁷, A.A. Watson⁷²,
 M. Weber³⁴, K. Weidenhaupt³⁷, A. Weindl³³, F. Werner³³,
 S. Westerhoff⁹⁰, B.J. Whelan⁸⁵, A. Widom⁸³, G. Wieczorek⁶⁰,
 L. Wiencke⁷⁵, B. Wilczyńska^{59 ‡}, H. Wilczyński⁵⁹, M. Will³³,
 C. Williams⁸⁶, T. Winchen³⁷, M. Wommer³³, B. Wundheiler⁷,
 T. Yamamoto^{86 a}, T. Yapici⁸¹, P. Younk^{79, 39}, G. Yuan⁸⁰,
 A. Yushkov⁷¹, B. Zamorano Garcia⁷⁰, E. Zas⁷¹, D. Zavrtnik^{66, 65},
 M. Zavrtnik^{65, 66}, I. Zaw^{82 d}, A. Zepeda^{52 b}, J. Zhou⁸⁶, Y. Zhu³⁴,
 M. Zimbres Silva^{32, 16}, M. Ziolkowski³⁹**

¹ Centro Atómico Bariloche and Instituto Balseiro (CNEA-UNCuyo-CONICET), San Carlos de Bariloche, Argentina

² Centro de Investigaciones en Láseres y Aplicaciones, CITEDEF and CONICET, Argentina

³ Departamento de Física, FCEyN, Universidad de Buenos Aires y CONICET, Argentina

⁴ IFLP, Universidad Nacional de La Plata and CONICET, La Plata, Argentina

⁵ Instituto de Astronomía y Física del Espacio (CONICET-UBA), Buenos Aires, Argentina

⁶ Instituto de Física de Rosario (IFIR) - CONICET/U.N.R. and Facultad de Ciencias Bioquímicas y Farmacéuticas U.N.R., Rosario, Argentina

⁷ Instituto de Tecnologías en Detección y Astropartículas (CNEA, CONICET, UNSAM), Buenos Aires, Argentina

⁸ National Technological University, Faculty Mendoza (CONICET/CNEA), Mendoza, Argentina

⁹ Observatorio Pierre Auger, Malargüe, Argentina

¹⁰ Observatorio Pierre Auger and Comisión Nacional de Energía Atómica, Malargüe, Argentina

¹¹ Universidad Tecnológica Nacional - Facultad Regional Buenos Aires, Buenos Aires, Argentina

¹² University of Adelaide, Adelaide, S.A., Australia

¹³ Centro Brasileiro de Pesquisas Físicas, Rio de Janeiro, RJ, Brazil

¹⁴ Universidade de São Paulo, Instituto de Física, São Carlos, SP, Brazil

¹⁵ Universidade de São Paulo, Instituto de Física, São Paulo, SP, Brazil

¹⁶ Universidade Estadual de Campinas, IFGW, Campinas, SP, Brazil

- 17 Universidade Estadual de Feira de Santana, Brazil
- 18 Universidade Federal da Bahia, Salvador, BA, Brazil
- 19 Universidade Federal do ABC, Santo André, SP, Brazil
- 20 Universidade Federal do Rio de Janeiro, Instituto de Física, Rio de Janeiro, RJ, Brazil
- 21 Universidade Federal Fluminense, EEIMVR, Volta Redonda, RJ, Brazil
- 22 Rudjer Bošković Institute, 10000 Zagreb, Croatia
- 23 Charles University, Faculty of Mathematics and Physics, Institute of Particle and Nuclear Physics, Prague, Czech Republic
- 24 Institute of Physics of the Academy of Sciences of the Czech Republic, Prague, Czech Republic
- 25 Palacky University, RCPTM, Olomouc, Czech Republic
- 26 Institut de Physique Nucléaire d'Orsay (IPNO), Université Paris 11, CNRS-IN2P3, Orsay, France
- 27 Laboratoire de l'Accélérateur Linéaire (LAL), Université Paris 11, CNRS-IN2P3, France
- 28 Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE), Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France
- 29 Laboratoire de Physique Subatomique et de Cosmologie (LPSC), Université Joseph Fourier Grenoble, CNRS-IN2P3, Grenoble INP, France
- 30 Station de Radioastronomie de Nançay, Observatoire de Paris, CNRS/INSU, France
- 31 SUBATECH, École des Mines de Nantes, CNRS-IN2P3, Université de Nantes, France
- 32 Bergische Universität Wuppertal, Wuppertal, Germany
- 33 Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany
- 34 Karlsruhe Institute of Technology - Campus North - Institut für Prozessdatenverarbeitung und Elektronik, Karlsruhe, Germany
- 35 Karlsruhe Institute of Technology - Campus South - Institut für Experimentelle Kernphysik (IEKP), Karlsruhe, Germany
- 36 Max-Planck-Institut für Radioastronomie, Bonn, Germany
- 37 RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany
- 38 Universität Hamburg, Hamburg, Germany
- 39 Universität Siegen, Siegen, Germany
- 40 Dipartimento di Fisica dell'Università and INFN, Genova, Italy
- 41 Università dell'Aquila and INFN, L'Aquila, Italy
- 42 Università di Milano and Sezione INFN, Milan, Italy
- 43 Università di Napoli "Federico II" and Sezione INFN, Napoli, Italy
- 44 Università di Roma II "Tor Vergata" and Sezione INFN, Roma, Italy
- 45 Università di Catania and Sezione INFN, Catania, Italy
- 46 Università di Torino and Sezione INFN, Torino, Italy
- 47 Dipartimento di Matematica e Fisica "E. De Giorgi" dell'Università del Salento and Sezione INFN, Lecce, Italy
- 48 Istituto di Astrofisica Spaziale e Fisica Cosmica di Palermo (INAF), Palermo, Italy
- 49 Istituto di Fisica dello Spazio Interplanetario (INAF), Università di Torino and Sezione INFN, Torino, Italy
- 50 INFN, Laboratori Nazionali del Gran Sasso, Assergi (L'Aquila), Italy
- 51 Benemérita Universidad Autónoma de Puebla, Puebla, Mexico
- 52 Centro de Investigación y de Estudios Avanzados del IPN (CINVESTAV), México, Mexico

- 53 Universidad Michoacana de San Nicolas de Hidalgo, Morelia, Michoacan, Mexico
54 Universidad Nacional Autonoma de Mexico, Mexico, D.F., Mexico
55 IMAPP, Radboud University Nijmegen, Netherlands
56 Kernfysisch Versneller Instituut, University of Groningen, Groningen, Netherlands
57 Nikhef, Science Park, Amsterdam, Netherlands
58 ASTRON, Dwingeloo, Netherlands
59 Institute of Nuclear Physics PAN, Krakow, Poland
60 University of Łódź, Łódź, Poland
61 LIP and Instituto Superior Técnico, Technical University of Lisbon, Portugal
62 'Horia Hulubei' National Institute for Physics and Nuclear Engineering, Bucharest-Magurele, Romania
63 University of Bucharest, Physics Department, Romania
64 University Politehnica of Bucharest, Romania
65 J. Stefan Institute, Ljubljana, Slovenia
66 Laboratory for Astroparticle Physics, University of Nova Gorica, Slovenia
67 Institut de Física Corpuscular, CSIC-Universitat de València, Valencia, Spain
68 Universidad Complutense de Madrid, Madrid, Spain
69 Universidad de Alcalá, Alcalá de Henares (Madrid), Spain
70 Universidad de Granada and C.A.F.P.E., Granada, Spain
71 Universidad de Santiago de Compostela, Spain
72 School of Physics and Astronomy, University of Leeds, United Kingdom
73 Argonne National Laboratory, Argonne, IL, USA
74 Case Western Reserve University, Cleveland, OH, USA
75 Colorado School of Mines, Golden, CO, USA
76 Colorado State University, Fort Collins, CO, USA
77 Colorado State University, Pueblo, CO, USA
78 Fermilab, Batavia, IL, USA
79 Los Alamos National Laboratory, Los Alamos, NM, USA
80 Louisiana State University, Baton Rouge, LA, USA
81 Michigan Technological University, Houghton, MI, USA
82 New York University, New York, NY, USA
83 Northeastern University, Boston, MA, USA
84 Ohio State University, Columbus, OH, USA
85 Pennsylvania State University, University Park, PA, USA
86 University of Chicago, Enrico Fermi Institute, Chicago, IL, USA
87 University of Hawaii, Honolulu, HI, USA
88 University of Nebraska, Lincoln, NE, USA
89 University of New Mexico, Albuquerque, NM, USA
90 University of Wisconsin, Madison, WI, USA
91 University of Wisconsin, Milwaukee, WI, USA
92 Institute for Nuclear Science and Technology (INST), Hanoi, Vietnam

(‡) Deceased

(a) Now at Konan University

(b) Also at the Universidad Autonoma de Chiapas on leave of absence from Cinvestav

(c) Now at University of Maryland

(d) Now at NYU Abu Dhabi

E-mail: auger_spokespersons@fnal.gov

Abstract. To interpret the mean depth of cosmic ray air shower maximum and its dispersion, we parametrize those two observables as functions of the first two moments of the $\ln A$ distribution. We examine the goodness of this simple method through simulations of test mass distributions. The application of the parameterization to Pierre Auger Observatory data allows one to study the energy dependence of the mean $\ln A$ and of its variance under the assumption of selected hadronic interaction models. We discuss possible implications of these dependences in term of interaction models and astrophysical cosmic ray sources.

Keywords: cosmic ray experiments, ultra high energy cosmic rays

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1 Introduction

The most commonly used shower observables for the study of the composition of Ultra High Energy Cosmic Rays (UHECR) are the mean value of the depth of shower maximum, $\langle X_{\max} \rangle$, and its dispersion, $\sigma(X_{\max})$. Inferring the mass composition from these measurements is subject to some level of uncertainty. This is because their conversion to mass relies on the use of shower simulation codes which include the assumption of a hadronic interaction model. The various interaction models [1] have in common the ability to fit lower energy accelerator data. However, different physical assumptions are used to extrapolate these low energy interaction properties to higher energies. Consequently they provide different expectations for $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$. The first aim of this paper is to discuss how the mean value of the depth of shower maximum and its dispersion can be used to interpret mass composition even in the presence of uncertainties in the hadronic interaction modeling.

Furthermore, we discuss the different roles of the two observables, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$, with respect to mass composition. In the interpretation of data they are often used as different, and independent, aspects of the same phenomenon. However it is not true to say that both parameters reflect the cosmic ray composition to the same extent. According to the superposition model [2] $\langle X_{\max} \rangle$ is linear in $\langle \ln A \rangle$ and therefore it actually measures mass composition for both pure and mixed compositions. But, we will show that the behaviour of $\sigma(X_{\max})$ is more complex to interpret as there is no one-to-one correspondence between its value and a given mean log mass. Only in the case of pure composition is this correspondence unique.

In this paper we refine the analysis method originally proposed by Linsley [3, 4] and apply it to the Auger data. The Pierre Auger Collaboration has published results on the mean and dispersion of the X_{\max} distribution at energies above 10^{18} eV [5, 6]. In this work we apply the proposed method to convert those observables to the first moments of the log mass distribution, namely $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$.

The paper is organized as follows. In Section 2 we discuss the parameterization for $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$. In Sec. 3 we test the method with shower simulations assuming different mass distributions. Sec. 4 describes the application of the method to data. The

discussion of the results and the conclusions follow in sections 5 and 6 respectively. The details of the parameterization and the best fit values for the hadronic interaction models are summarized in Appendix A.

2 A method to interpret $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$

The interpretation of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ can be simplified by making use of an analysis method based on the generalized Heitler model of extensive air showers [7]. In this context $\langle X_{\max} \rangle$ is a linear function of the logarithm of the shower energy per nucleon:

$$\langle X_{\max} \rangle = X_0 + D \log_{10} \left(\frac{E}{E_0 A} \right), \quad (2.1)$$

where X_0 is the mean depth of proton showers at energy E_0 and D is the elongation rate [8–10], i.e., the change of $\langle X_{\max} \rangle$ per decade of energy. The High Energy hadronic interaction models used in this work are EPOS 1.99 [11], Sibyll 2.1 [12], QGSJet 01 [13] and QGSJet II [14]. Simulated data show that eq. (2.1) gives a fair description of EPOS and Sibyll results in the full range of interest for this work, 10^{18} to 10^{20} eV, but does not reproduce accurately QGSJet models. For this reason we generalize the original representation as:

$$\langle X_{\max} \rangle = X_0 + D \log_{10} \left(\frac{E}{E_0 A} \right) + \xi \ln A + \delta \ln A \log_{10} \left(\frac{E}{E_0} \right), \quad (2.2)$$

where the parameters ξ and δ are expected to be zero if the model predictions are compatible with the superposition result (2.1).

For nuclei of the same mass A one expects the shower maximum to be on average:

$$\langle X_{\max} \rangle = \langle X_{\max} \rangle_p + f_E \ln A, \quad (2.3)$$

and its dispersion to be only influenced by shower-to-shower fluctuations:

$$\sigma^2(X_{\max}) = \sigma_{\text{sh}}^2(\ln A). \quad (2.4)$$

Here $\langle X_{\max} \rangle_p$ denotes the mean depth at maximum of proton showers, as obtained from either eq. (2.1) or (2.2), and $\sigma_{\text{sh}}^2(\ln A)$ is the X_{\max} variance for mass A , $\sigma_{\text{sh}}^2(\ln A) = \sigma^2(X_{\max} | \ln A)$. The energy dependent parameter f_E appearing in (2.3) is:

$$f_E = \xi - \frac{D}{\ln 10} + \delta \log_{10} \left(\frac{E}{E_0} \right). \quad (2.5)$$

The values of the parameters X_0 , D , ξ , δ depend on the specific hadronic interaction model. In this work they are obtained from CONEX [15] shower simulations as described in Appendix A.

In the case of a mixed composition at the top of the atmosphere, the mean and variance of X_{\max} depend on the $\ln A$ distribution. There are two independent sources of fluctuations: the intrinsic shower-to-shower fluctuations and the $\ln A$ dispersion arising from the mass distribution. The first term gives rise to $\langle \sigma_{\text{sh}}^2 \rangle$, the average variance of X_{\max} weighted according to the $\ln A$ distribution. The second contribution can be written as $\left(\frac{d\langle X_{\max} \rangle}{d\ln A} \right)^2 \sigma_{\ln A}^2$ where $\sigma_{\ln A}^2$ is the variance of the $\ln A$ distribution. We can finally write for the two profile observables:

$$\langle X_{\max} \rangle = \langle X_{\max} \rangle_p + f_E \langle \ln A \rangle \quad (2.6)$$

$$\sigma^2(X_{\max}) = \langle \sigma_{\text{sh}}^2 \rangle + f_E^2 \sigma_{\ln A}^2 . \quad (2.7)$$

The two equations depend on energy through the parameters but also via $\langle \sigma_{\text{sh}}^2 \rangle$ and the possible dependence of the two moments of the $\ln A$ distribution.

To obtain an explicit expression for $\langle \sigma_{\text{sh}}^2 \rangle$ we need a parameterization for $\sigma_{\text{sh}}^2(\ln A)$. We assume a quadratic law in $\ln A$:

$$\sigma_{\text{sh}}^2(\ln A) = \sigma_p^2 [1 + a \ln A + b(\ln A)^2] , \quad (2.8)$$

where σ_p^2 is the X_{\max} variance for proton showers. The evolution of $\sigma_{\text{sh}}^2(\ln A)$ with energy is included in σ_p^2 and the parameter a :

$$\sigma_p^2 = p_0 + p_1 \log_{10} \left(\frac{E}{E_0} \right) + p_2 \left[\log_{10} \left(\frac{E}{E_0} \right) \right]^2 \quad \text{and} \quad a = a_0 + a_1 \log_{10} \left(\frac{E}{E_0} \right) . \quad (2.9)$$

The parameters $p_0, p_1, p_2, a_0, a_1, b$ depend on hadronic interactions: the values used in the paper are given in Appendix A.

Using measurements of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$, equations (2.6) and (2.7) can be inverted to get the first two moments of the $\ln A$ distribution. From eq. (2.6) one gets:

$$\langle \ln A \rangle = \frac{\langle X_{\max} \rangle - \langle X_{\max} \rangle_p}{f_E} . \quad (2.10)$$

Averaging eq. (2.8) on $\ln A$ one obtains:

$$\langle \sigma_{\text{sh}}^2 \rangle = \sigma_p^2 [1 + a \langle \ln A \rangle + b \langle (\ln A)^2 \rangle] . \quad (2.11)$$

Substituting in eq. (2.7) we get:

$$\sigma^2(X_{\max}) = \sigma_p^2 [1 + a \langle \ln A \rangle + b \langle (\ln A)^2 \rangle] + f_E^2 \sigma_{\ln A}^2 . \quad (2.12)$$

But by definition $\langle (\ln A)^2 \rangle = \sigma_{\ln A}^2 + \langle \ln A \rangle^2$. Solving in $\sigma_{\ln A}^2$ one finally obtains:

$$\sigma_{\ln A}^2 = \frac{\sigma^2(X_{\max}) - \sigma_{\text{sh}}^2(\langle \ln A \rangle)}{b \sigma_p^2 + f_E^2} . \quad (2.13)$$

Equations (2.10) and (2.13) are the key tools used throughout this work for interpreting Pierre Auger Observatory data in terms of mass composition and assessing the validity of available hadronic interaction models.

3 Testing the method with simulation

Equations (2.6) and (2.7) can be tested with simulations. They contain parameters depending on the hadronic interaction properties and on the mass distribution of nuclei. The mass distribution of nuclei refers to those nuclei hitting the Earth's atmosphere: it does not matter what is the source of the mass dispersion, either a mixed composition at injection or the dispersion caused by propagation. So, in order to test the method we will simply use different test distributions of the masses at the top of the atmosphere.

For this purpose we have chosen three different mass distributions:

1. A distribution uniform in $\ln A$ from $\ln(1)$ to $\ln(56)$ and independent of energy. The values of $\langle \ln A \rangle$ and $\sigma_{\ln A}$ are respectively 2.01 and 1.16.

2. A Gaussian $\ln A$ distribution with $\langle \ln A \rangle$ increasing linearly with $\log E$ from $\ln(4)$ at 10^{18} eV to $\ln(14)$ at 10^{20} eV and $\sigma_{\ln A} = 0.75$ independent of energy. The Gaussian is truncated to less than 2 sigmas to avoid unphysical mass values. In this case the $\ln A$ dispersion is fixed and equal to 0.66 but $\langle \ln A \rangle$ varies with energy.
3. Two masses, H and Fe, with proton fraction $H/(H + Fe)$ decreasing linearly with $\log E$ from 1 at 10^{18} eV to 0 at 10^{20} eV. In this case, both $\langle \ln A \rangle$ and $\sigma_{\ln A}$ vary with energy.

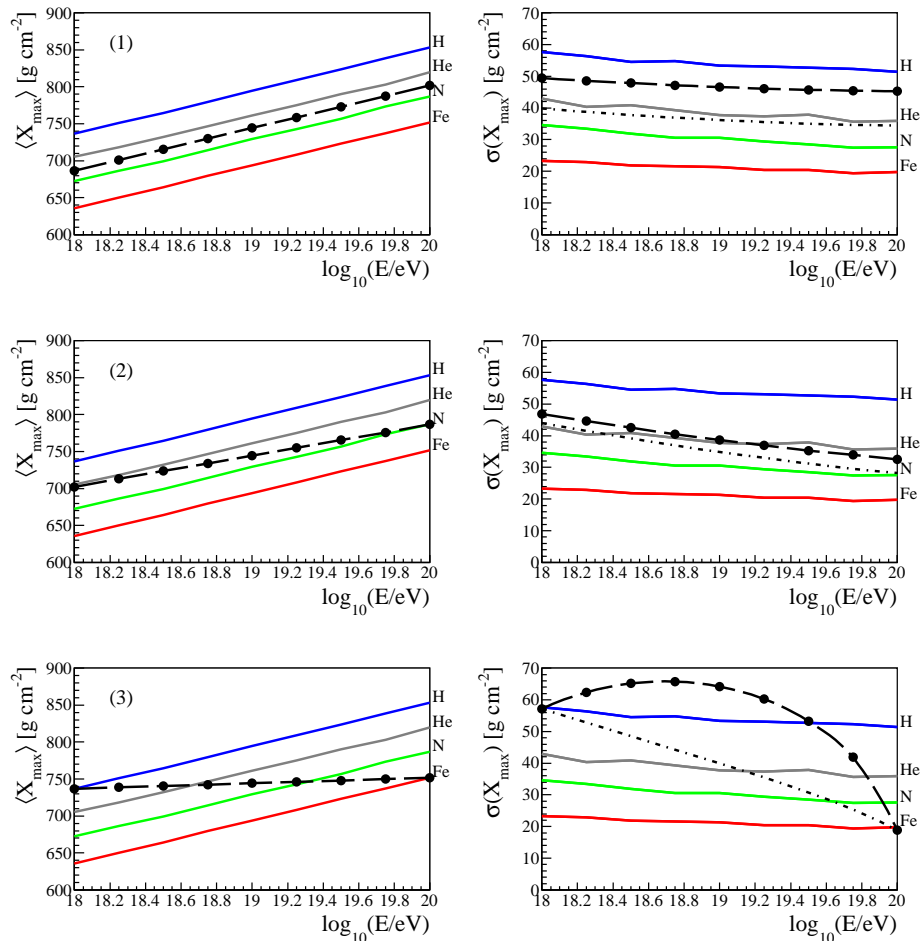


Figure 1. $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ as a function of $\log_{10}(E/\text{eV})$ for three different mass distribution hypotheses (see text). Full circles are calculated from the resulting X_{\max} distributions from the CONEX simulations. Sibyll 2.1 has been chosen for hadronic interactions. The dashed lines show equations (2.6) for $\langle X_{\max} \rangle$ and (2.7) for $\sigma(X_{\max})$. The dot-dashed line refers to the contribution of the first term in (2.7).

Figure 1 shows the result of the test for the three mass distribution hypotheses. To generate the X_{\max} distributions we have used CONEX [15] showers with Sibyll 2.1 [12] as the hadronic interaction model. These distributions do not include detector effects. For each test mass hypothesis, the mean and RMS are retrieved from the resulting X_{\max} distribution obtained from the simulations. These are shown as full circles, $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ in left

and right panels respectively. The dashed lines are calculated using equations (2.6) and (2.7) for the three different mass hypotheses by using only the first two moments $\langle \ln A \rangle$ and $\sigma_{\ln A}$.

One can see that, despite the simple assumptions made, good agreement is achieved for all the three mass distributions. The dot-dashed line refers to the contribution of the first term in eq. (2.7). The comparison between the two lines (dashed vs. dot-dashed) highlights how different the interpretation of $\sigma(X_{\max})$ data can be if one does not take into account the mass dispersion term.

The inverse equations (2.10) and (2.13) have also been tested using Monte Carlo simulation. In this case $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ have been obtained as a function of $\log_{10}(E/\text{eV})$ directly from the input mass distributions. These values are shown as full circles in Figure 2. The $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ retrieved from the corresponding X_{\max} distributions are used in equations (2.10) and (2.13) to get $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$. These are shown in Fig. 2 as dashed lines. Also in this case, the comparison is quite successful.

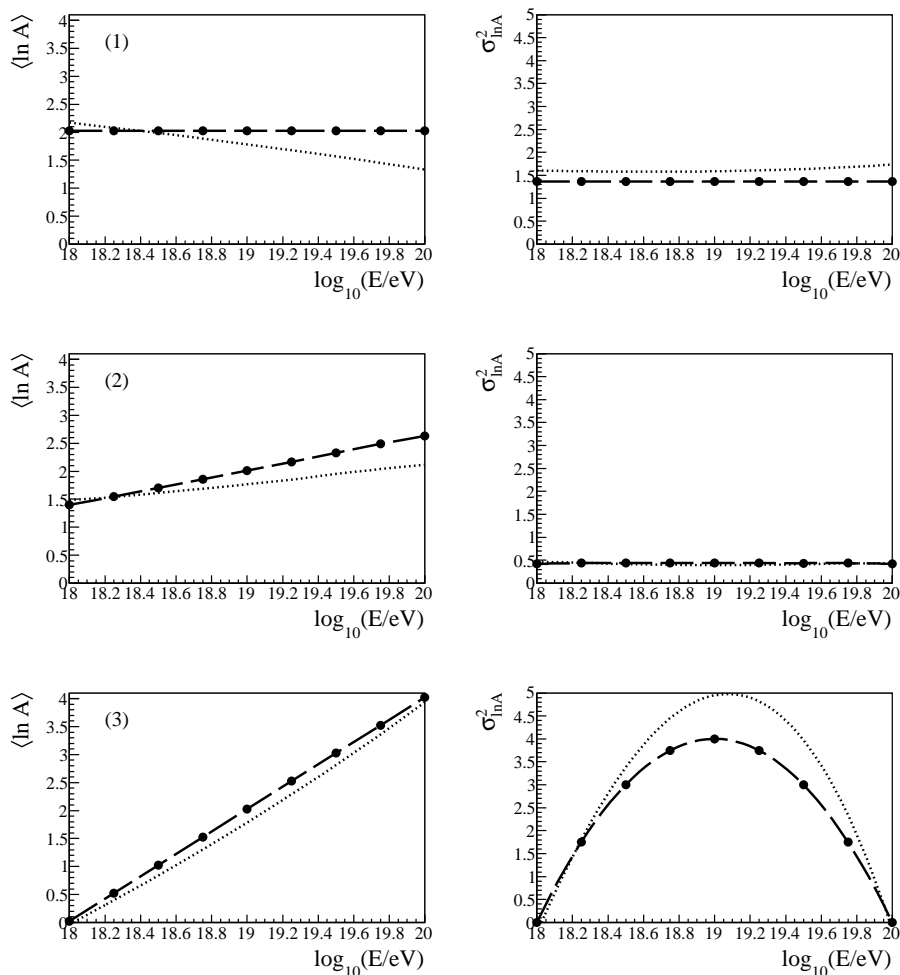


Figure 2. $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ as a function of $\log_{10}(E/\text{eV})$ for three different mass distribution hypotheses. Sibyll 2.1 is the hadronic interaction model. Full circles refer to the values obtained directly from the input mass distributions. The dashed lines show $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ calculated using equations (2.10) and (2.13). The dotted lines refer to the calculation of the same variables using the parameterization for QGSJet II in (2.10) and (2.13).

The simulated data sample can also be used to estimate the systematic uncertainty in the calculation of the moments of the X_{\max} ($\ln A$) distribution induced by the missing knowledge of the hadronic interaction mechanism. This study is pursued using simulated showers generated with a given model together with parameters of another model in equations (2.6) and (2.7) for the profile variables, and (2.10) and (2.13) for the log mass variables. An example of this procedure is shown in Fig. 2 where the dotted lines show the calculation with the parameters of QGSJet II and the full circles refer to data simulated with Sibyll 2.1. As a summary of these cross-model checks, we find mean absolute deviations of 4 to 27 g cm^{-2} for $\langle X_{\max} \rangle$ and 1 to 5.4 g cm^{-2} for $\sigma(X_{\max})$, where the maximum deviations are obtained crossing EPOS with QGSjetII. The same study done for the moments of the log mass distribution gives mean absolute deviations of 0.2 to 1.2 for $\langle \ln A \rangle$ and 0.02 to 0.5 for $\sigma_{\ln A}^2$. In this case the maximum values refer to EPOS vs. QGSJet 01 for the first moment and QGSJet II vs. QGSJet 01 for the second.

4 Application to data

At ultra-high energies, shower development can be directly measured using fluorescence and Cherenkov light profiles. Mean X_{\max} data as a function of energy are available from Fly’s Eye [16], HiRes [17, 18], Auger [5], Yakutsk [19] and Telescope Array [20]. $\langle X_{\max} \rangle$ data were complemented with fluctuation measurements as early as 1980s (see e.g. [21] and references therein) but only recently have precise optical detector measurements become available [5, 18, 19].

The Pierre Auger Collaboration has published results on the mean and dispersion of the X_{\max} distribution at energies above 10^{18} eV [5]. Here we apply the method presented in this work to an updated dataset available in [6, 22]. These data are shown in Figure 3.

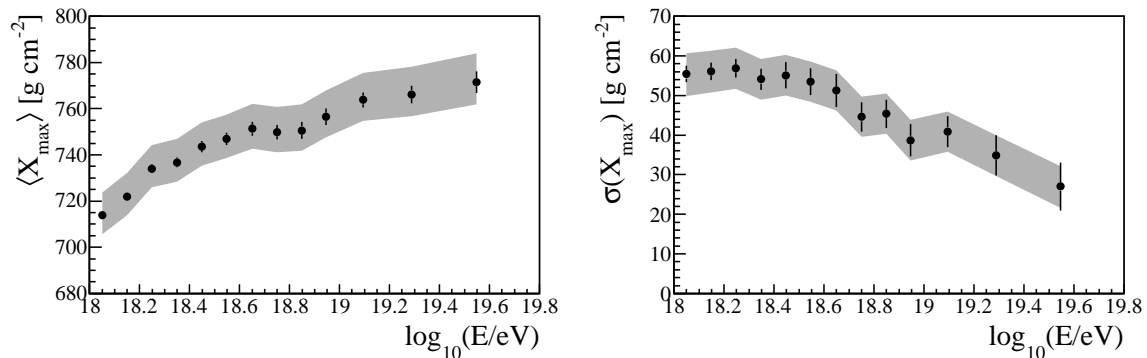


Figure 3. $\langle X_{\max} \rangle$ (left) and $\sigma(X_{\max})$ (right) as a function of $\log_{10}(E/\text{eV})$ from Pierre Auger Observatory data [6, 22]. Data (full circles) are shown with statistical errors. Systematic uncertainties are represented as bands.

In the Auger analysis [5], the events are selected using fiducial volume cuts based on the shower geometry. This ensures that the viewable X_{\max} range for each shower is large enough to accommodate the full X_{\max} distribution. Also, the detector resolution is accounted for by subtracting in quadrature its contribution to the measured dispersion. This allows the direct conversion to the moments of the $\ln A$ distribution using equations (2.10) and (2.13)

without the need of more complex treatment, such as is required in the presence of acceptance biases [23, 24].

The moments of the log mass distribution, $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$, as obtained using equations (2.10) and (2.13), are shown (full circles) as a function of $\log_{10}(E/\text{eV})$ in Figures 4 and 5 respectively. Error bars show the statistical errors obtained from the propagation of data errors and the errors of the fitted parameters. Shaded bands are the systematic uncertainties obtained by summing in quadrature the different individual contributions.

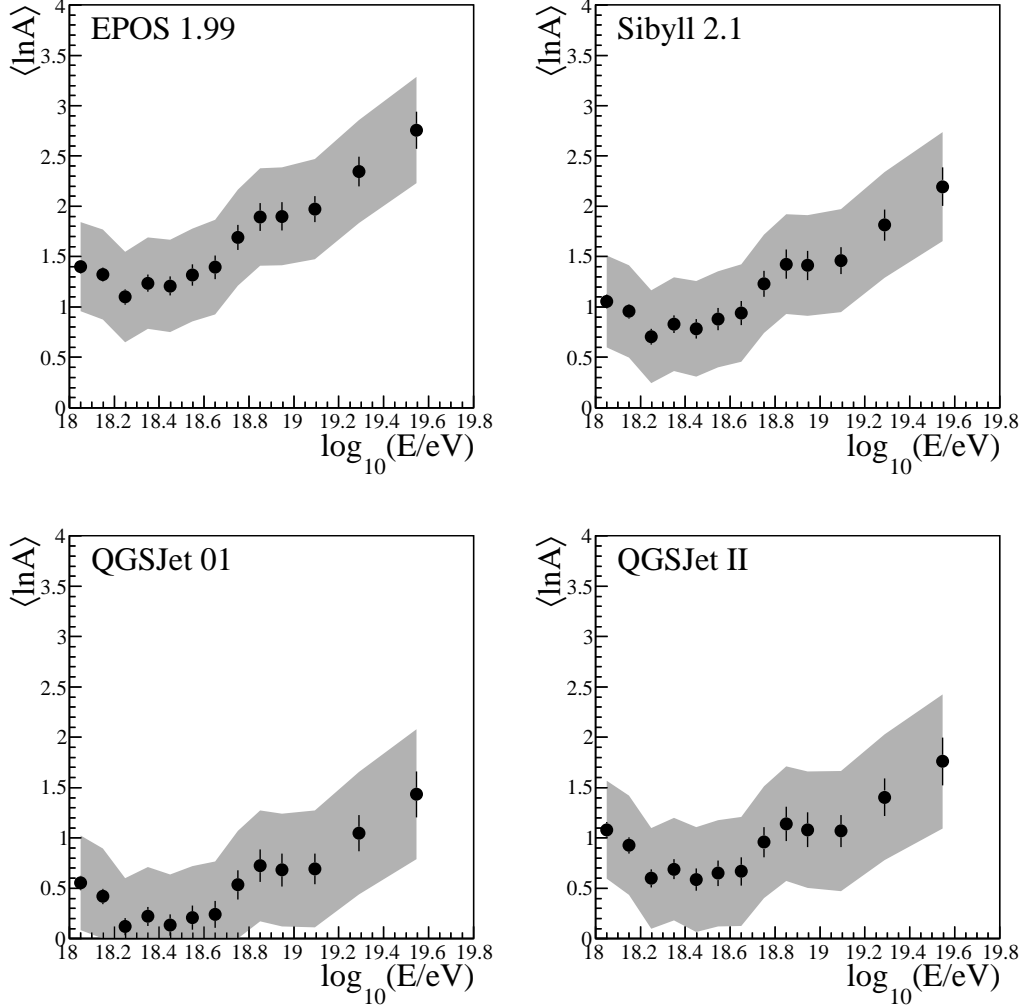


Figure 4. $\langle \ln A \rangle$ as a function of $\log_{10}(E/\text{eV})$ obtained from Auger data [22] are shown as full circles for different hadronic interaction models. Error bars show statistical errors. The shaded areas refer to systematic uncertainties obtained by summing in quadrature the systematic uncertainties on $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ data points and on the FD energy scale.

The systematic uncertainties on $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ data points have different sources: calibration, atmospheric conditions, reconstruction and event selection [5]. Another source of systematics is related to the uncertainty of the FD energy scale [25], 22 %, which induces an uncertainty in $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ via the parameters of the models. All these uncertainties contribute approximately at the same level and independently of energy. The figures show

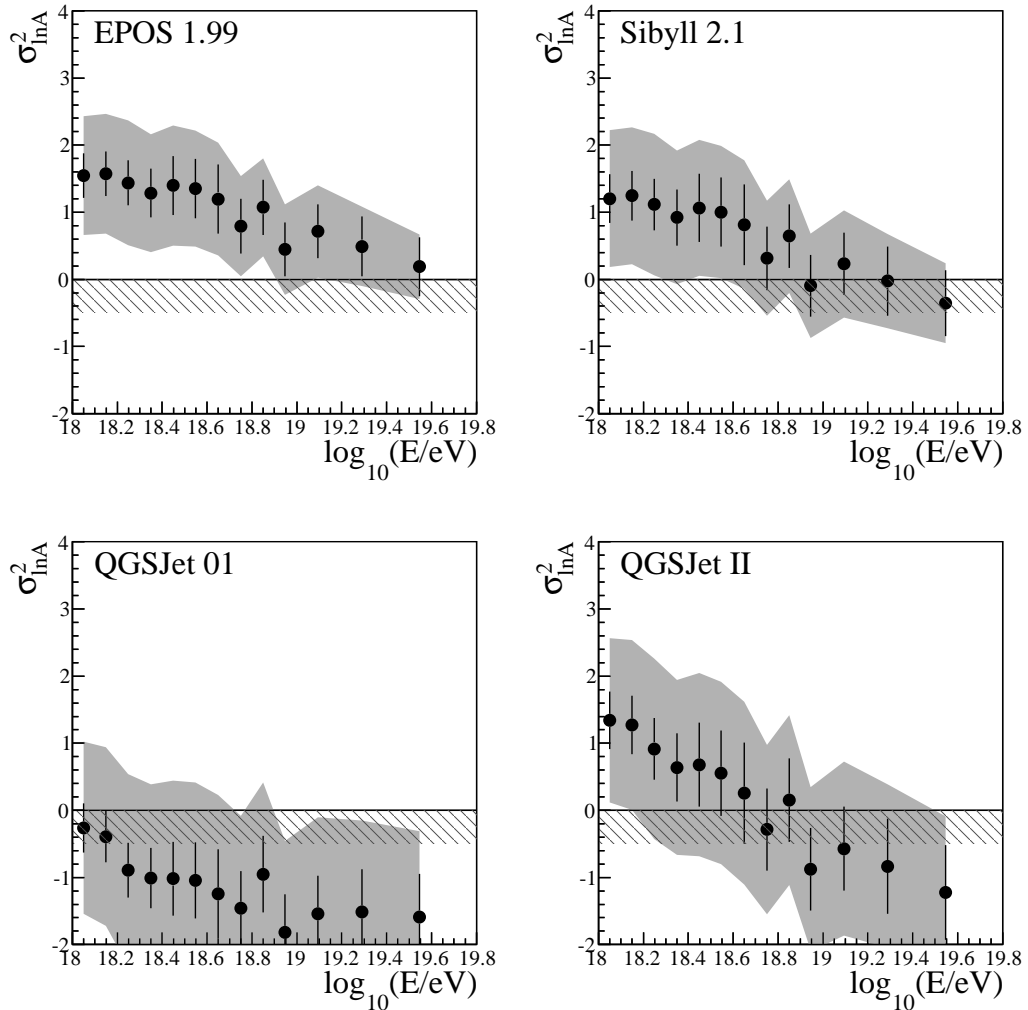


Figure 5. $\sigma_{\ln A}^2$ as a function of $\log_{10}(E/\text{eV})$ obtained from Auger data [22] are shown as full circles for different hadronic interaction models. Error bars show statistical errors. The shaded area refers to systematic uncertainties as in Fig. 4. The lower limit of allowed $\sigma_{\ln A}^2$ is shown by the exclusion line. The upper limit (4.05) is just above the maximum of the vertical axis.

the results for the moments of the log mass distribution for EPOS 1.99 [11], Sibyll 2.1 [12], QGSJet 01 [13] and QGSJet II [14].

Despite the uncertainties and the different mass offsets of the models, the overall features are similar in all the cases. So far as the energy dependence is concerned, the data imply an increasing $\langle \ln A \rangle$ above $10^{18.3}$ eV from light to intermediate masses and a decreasing $\sigma_{\ln A}^2$ over the whole energy range.

Looking more specifically to the different hadronic models we notice a slight change in the log mass scale. The highest masses are obtained for EPOS 1.99. Sibyll 2.1 and QGSJet II show intermediate values, whereas the lowest masses are obtained for QGSJet 01. In particular at $\log_{10}(E/\text{eV}) = 18.25$ the mean log mass, $\langle \ln A \rangle$, is 1.10, 0.70, 0.60 and 0.12 respectively for EPOS 1.99, Sibyll 2.1, QGSJet II and QGSJet 01 with statistical errors of about 0.08 and systematic uncertainty of about 0.6. The Pierre Auger Collaboration has

recently published the measurement of the proton-air cross section for the energy interval 10^{18} to $10^{18.5}$ eV [26]. That measurement is done using the showers with $X_{\max} \geq 768$ g cm $^{-2}$, corresponding to 20% of the total X_{\max} distribution. Even in the most unfavourable case, (the $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ predicted by EPOS), one finds that several realizations obtained from the allowed $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ have enough protons in the most deeply penetrating showers to fulfill the selection criteria adopted in the Auger analysis.

Whereas $\langle \ln A \rangle$ always has valid values (apart a small region which crosses $\langle \ln A \rangle = 0$ for QGSJet 01), there are wide energy intervals where $\sigma_{\ln A}^2$ is negative. Considering eq. (2.13) one can see that these values occur for energies where the shower fluctuations corresponding to the mean log mass exceed the measured X_{\max} fluctuations. Figure 5 shows that $\sigma_{\ln A}^2$ data points are within the allowed physical region only for EPOS 1.99 and Sibyll 2.1. They are partly outside for QGSJet II, and completely outside for QGSJet 01. However the current systematic uncertainties do not allow one to establish stringent tests to the models.

The method presented in this work shows that the Pierre Auger Observatory data can confront hadronic physics models provided that future developments in the shower data analysis reduce systematics. By shrinking the shaded bands in Figure 5 it will be possible to constrain those models.

5 Discussion

The importance of the combined study of the mean values and fluctuations of mass dependent observables has been addressed by several authors [3, 4, 21, 27, 28]. In particular, Linsley [4] showed that a combined analysis of the mean and the variance of $\ln A$ can provide a useful representation of the mass transition (if any) to be found in shower profile data. In fact, possible transitions are constrained to a limited region of the $(\langle \ln A \rangle, \sigma_{\ln A}^2)$ plane. More recently a similar study using the $\langle X_{\max} \rangle$ - $\sigma(X_{\max})$ correlation¹ reached a similar conclusion [29].

Converting X_{\max} data to $\ln A$ variables, as described in Sec. 2, one can plot Pierre Auger Observatory data in the $(\langle \ln A \rangle, \sigma_{\ln A}^2)$ plane. Since this procedure depends on the hadronic model, one gets a plot for each model as shown in Figure 6. Data points are shown as full circles with size increasing in proportion to $\log E$. The error bars are tilted because of correlations arising from equations (2.10) and (2.13) and represent the principal axes of the statistical error ellipses. The solid lines show the systematic uncertainties. The same figure shows the region allowed for mass compositions. The contour of this region (gray thick line) is generated by mixing neighbouring nuclei in the lower edge and extreme nuclei (protons and iron) in the upper edge. Each of these mixings is an arch shaped line in the $(\langle \ln A \rangle, \sigma_{\ln A}^2)$ plane.

Figure 6 shows that the Auger data lie outside the allowed boundaries for part of the energy range in some of the models. As noted previously, systematic uncertainties are still large and thus prevent us from more definite conclusions. However the energy evolution is common to all models suggesting that the average mass increases with decreasing log mass dispersion. This behaviour might imply astrophysical consequences.

In fact there are only a few possibilities for extragalactic source models to produce compositions with small log mass dispersion at the Earth. Protons can traverse their path from sources to the Earth without mass dispersion, but this case is excluded by Pierre Auger Observatory data at the highest energies.

¹ In this case the dependence on hadronic models has been accounted for by subtracting the corresponding observables predicted by the models for iron.

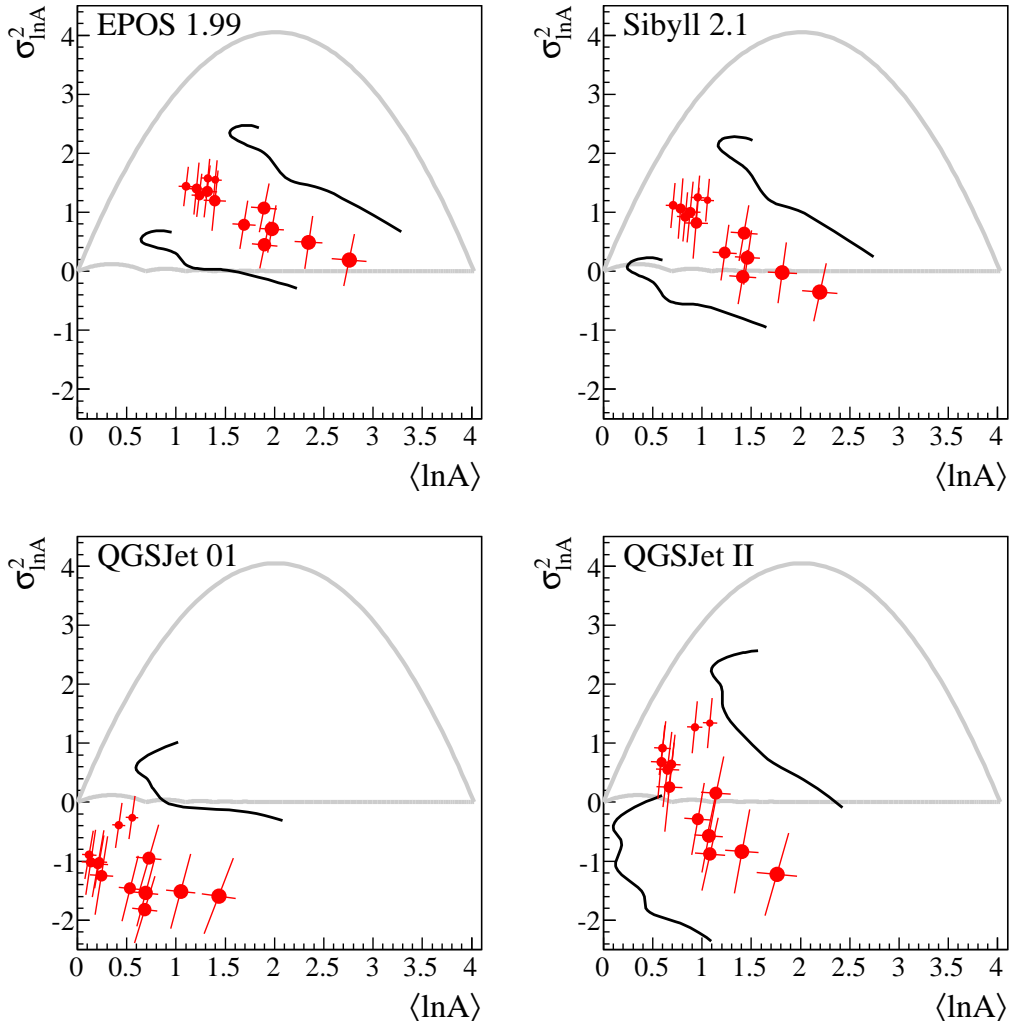


Figure 6. Pierre Auger data in the $(\langle \ln A \rangle, \sigma_{\ln A}^2)$ plane for different hadronic interaction models. Data points are shown as full circles with statistical errors. The marker sizes increase with the logarithm of the energy. Systematic uncertainties are shown as solid lines. The gray thick line shows the contour of the $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$ values allowed for nuclear compositions.

Nuclei originating from nearby sources ($\lesssim 100$ Mpc) might be detected with small mass dispersion. For these sources, propagation does not degrade mass and energy so the spectrum and composition reflect closely their values at injection. But, if sources are distributed uniformly, distant sources induce natural mass dispersions. Small $\ln A$ dispersions are possible only when there is small observed mass mixing so that, at each energy, only nuclei with a small spread in masses are present. This corresponds to the low- $\sigma_{\ln A}^2$ edge of the contour of the allowed region in the $(\langle \ln A \rangle, \sigma_{\ln A}^2)$ plane.

Protons originating by the photo-disintegration of nuclei are the main source of mass dispersion because they populate each energy region. The possible end of the injection spectrum based on a rigidity-dependent mechanism can reduce the proton component at high energies, thus producing a reduction of the mass dispersion at the highest energies. A complete study of source models under several hypotheses is required to study all the source

parameters that limit the mass dispersion in the propagation of extragalactic cosmic rays. Recent studies, see e.g. [30, 31], based on the assumption of a uniform source distribution, have shown that the Auger composition results, when combined with the energy spectrum, require hard injection spectra (i.e. index < 2) with low energy cutoffs and the possible presence of local sources.

6 Conclusions

In this work we presented a method for interpreting $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ in terms of mass composition. The method is based on an extension of the Heitler model of extensive air showers. The parameterization given in equations (2.6) and (2.7) expresses those two profile observables as a linear combination of the first two moments of the log mass distribution, $\langle \ln A \rangle$ and $\sigma_{\ln A}^2$, and of the mean shower fluctuations.

We first note that the method provides an effective key to the interpretation of data. The energy dependences of $\langle X_{\max} \rangle$ and $\sigma(X_{\max})$ are sometimes considered as different expressions of the same physical features, e.g. an increase or decrease of the mean log mass. However their different meanings can be easily understood by looking at the dependence on the mass variables. At a fixed energy $\langle X_{\max} \rangle$ is only function of $\langle \ln A \rangle$; therefore, it only carries information of the average composition. However, $\sigma(X_{\max})$ cannot be interpreted as a measure of the average composition since it is also affected by the log mass dispersion. Similarly, the inference of hadronic interaction properties from $\sigma(X_{\max})$ can be wrong unless the mass dispersion term ($\propto \sigma_{\ln A}^2$) is negligible. The parameter $\sigma_{\ln A}$ represents the dispersion of the masses as they hit the Earth atmosphere. It reflects not only the spread of nuclear masses at the sources but also the modifications that occur during their propagation to the Earth.

The method has been successfully tested, with the simulation of different mass distributions in the energy interval from 10^{18} to 10^{20} eV showing the robustness of the parameterization. We have applied the method to the Pierre Auger Observatory X_{\max} data to get the first two moments of the $\ln A$ distribution. The outcome relies on the choice of a hadronic interaction model to set the parameters and the appropriate shower fluctuations. Four models have been used, EPOS 1.99, Sibyll 2.1, QGSJet 01 and QGSJet II, and the corresponding moments of the log mass distribution have been obtained as a function of energy. Despite the differences in the chosen models, the overall features are quite similar. In particular we find an increasing $\langle \ln A \rangle$ above $10^{18.3}$ eV from light to intermediate masses and a decreasing $\sigma_{\ln A}^2$ over the whole energy range, while the mean log mass scale changes with hadronic models.

The results presented in this paper show the capability of the method to infer important features of the mass distribution of the UHECR nuclei. This is a remarkable outcome with respect to the study of source scenarios and propagation. In fact we do not only access the average mass, but also the mass dispersion. While a pure proton beam at the sources is not changed by propagation, nuclei should increase the mass dispersion in their path towards the Earth. The Auger results seem to imply either close-by sources or hard spectral indices, if the energy evolution of the present hadronic interaction models can be trusted.

The proposed method can also be used as a tool to investigate the validity of hadronic interaction models. In particular it has been shown that the intrinsic shower fluctuations are sometimes larger than the measured X_{\max} dispersions. This happens in different energy intervals for the different models. At the highest energies, all models approach the

lower boundary, and some of them enter the unphysical region, but the current systematic uncertainties prevent us from confidently rejecting any model. Provided that systematic uncertainties can be reduced in future data analysis, the method can be used to constrain hadronic interaction models. The addition of new measurements, such as the muon content of EAS [32, 33], may allow us to place stronger bounds to the models.

A Parameterization of the shower mean depth and its fluctuations

The shower code chosen for this work is CONEX [15]. CONEX is a hybrid simulation code that is suited for fast one-dimensional simulations of shower profiles, including fluctuations. It combines Monte Carlo simulation of high energy interactions with a fast numerical solution of cascade equations for the resulting distributions of secondary particles. In our CONEX simulation we used the default energy thresholds settings of version v2r3.1².

The parameters X_0 , D_1 , ξ and δ used in equations (2.6) and (2.7) have been obtained by fitting CONEX showers for four different primaries (H, He, N and Fe) in nine energy bins of width $\Delta \log_{10}(E/\text{eV}) = 0.25$ ranging from 10^{18} to 10^{20} eV, and for all the hadronic models used in this work: EPOS 1.99 [11], Sibyll 2.1 [12], QGSJet 01 [13] and QGSJet II [14]. In total, about 25,000 showers have been used for each energy bin and for each hadronic model. The fit procedure always converges with mean (maximum) $\langle X_{\text{max}} \rangle$ residuals from the simulated data of about 1 (3) g cm^{-2} for all the models. The best fit values are reported in Table 1 with their errors.

parameter	EPOS 1.99	Sibyll 2.1	QGSJet 01	QGSJet II
X_0	809.7 ± 0.3	795.1 ± 0.3	774.2 ± 0.3	781.8 ± 0.3
D	62.2 ± 0.5	57.7 ± 0.5	49.7 ± 0.5	45.8 ± 0.5
ξ	0.78 ± 0.24	-0.04 ± 0.24	-0.30 ± 0.24	-1.13 ± 0.24
δ	0.08 ± 0.21	-0.04 ± 0.21	1.92 ± 0.21	1.71 ± 0.21

Table 1. Parameters of formulae (2.6) and (2.7) for different hadronic interaction models setting $E_0 = 10^{19}$ eV. The values are obtained fitting the mean X_{max} for showers generated for four different primaries H, He, N and Fe. Statistical error obtained from the fit are also given. All values are expressed in g cm^{-2} .

Shower variances have been fitted using the parameterization given in equations (2.8) and (2.9) and the same simulated data set described above. The mean (maximum) $\sigma(X_{\text{max}})$ residuals from the simulated data are about 1 (3) g cm^{-2} for all the models. The best fit parameters are given in Table 2 with their errors.

Acknowledgments

The successful installation, commissioning, and operation of the Pierre Auger Observatory would not have been possible without the strong commitment and effort from the technical and administrative staff in Malargüe.

² The hadron and muon cutoff (minimum energy) is 1 GeV, the cutoff for electrons, positrons and gammas (e/m particles) is 1 MeV, the threshold energy for solving cascade equations is 0.05, 0.0005 and 0.005 of the primary energy for hadrons, muons and e/m particles respectively. The above-threshold e/m interaction are simulated with the EGS4 program [34]. The low energy ($E < 80$ GeV) interaction model is GEISHA [35]

parameter	EPOS 1.99	Sibyll 2.1	QGSJet 01	QGSJet II
$p_0 \times (\text{g}^{-2}\text{cm}^4)$	3279 ± 51	2785 ± 46	3852 ± 55	3163 ± 49
$p_1 \times (\text{g}^{-2}\text{cm}^4)$	-47 ± 66	-364 ± 58	-274 ± 70	-237 ± 61
$p_2 \times (\text{g}^{-2}\text{cm}^4)$	228 ± 108	152 ± 93	169 ± 116	60 ± 100
a_0	-0.461 ± 0.006	-0.368 ± 0.008	-0.451 ± 0.006	-0.386 ± 0.007
a_1	-0.0041 ± 0.0016	-0.0049 ± 0.0023	-0.0020 ± 0.0016	-0.0006 ± 0.0021
b	0.059 ± 0.002	0.039 ± 0.002	0.057 ± 0.001	0.043 ± 0.002

Table 2. Parameters of formulae (2.8) and (2.9) for different hadronic interaction models setting $E_0 = 10^{19}$ eV. The values are obtained fitting $\sigma^2(X_{\text{max}})$ for showers generated for four different primaries H, He, N and Fe. The statistical errors obtained from the fit are also given.

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