

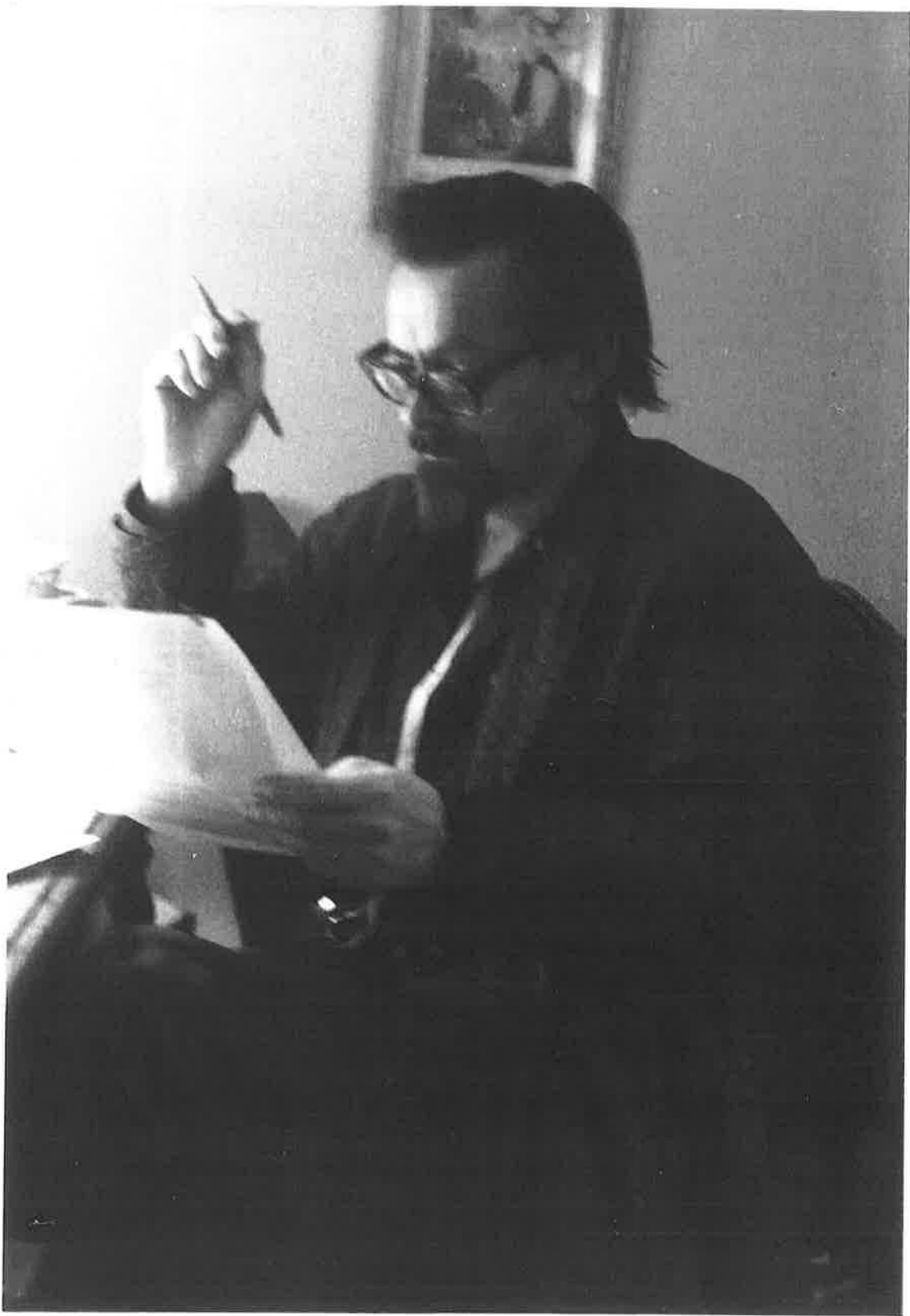
V.Y. Glaser

SOME RETROSPECTIVE REMARKS

by Ph. Blanchard

- OPENINGS
- MATHEMATICS IN PHYSICS
- GREAT ENCOUNTERS ALONG THE WAY
Zagreb, Göttingen, Copenhagen, Geneva, Strasbourg,
Bures sur Yvette
- USING MATHEMATICS WITH CLARITY AND
ELEGANCE

Quantum Mechanics, Quantum Field Theory





Vladimir Glaser

Né le 21/4/1924 à Gorizia (Italie),
Diplômé en Physique à l'Université de Zagreb
(Yougoslavie) en 1950, Thèse en Physique Théori-
que à Zagreb (1953), carrière universitaire
à l'Université de Zagreb: successivement assistant,
puis professeur de Physique Théorique jusqu'en
1957. Durant cette période un séjour à l'Institut
Max Planck à Göttingen (1951/52), plusieurs séjours
de quelques mois à Copenhague à l'Institut de
Niels Bohr. Depuis 1957 membre de la section
théorique du CERN, interrompu par un séjour
d'une année à l'Institut des Hautes Etudes Scienti-
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PHYSICS REPORTS

A Review Section of Physics Letters

ESSAYS IN MATHEMATICAL PHYSICS in memoriam V. Glaser

edited by

A. MARTIN and M. JACOB

Volume 134 Numbers 5 & 6

March 1986

PRPLCM 134(5 & 6) 273-395 (1986)



NORTH-HOLLAND · AMSTERDAM

LAST NUMBER OF THIS VOLUME

O P E N I N G S

I am happy to have been asked to speak about Yurko Glaser, his thinking and its actions. It is an honor for me to pay tribute to the brilliant achievements of this leading mathematical physicist, gifted teacher and exceptional friend.

It was in Strasbourg at the spring meeting of the RCP 25, where we first met 1967. At this time I was in Zürich at the ETH, working on the Paul-Fierz model of the infrared catastrophe under the direction of Res Jost.

Yurko was born on April 21, 1924 just before the discovery by Schrödinger, Heisenberg, Dirac, Born ... of modern Quantum Theory in the mid 1920's.

Carlo Rubbia was also born in Gorizia, Görz, Friaul – Julisch Venetien. Quantum Theory before 1925 – the Old Quantum Theory (Planck, Einstein, Bohr, Sommerfeld ...) – was part craft part art. Old principles had been founded wanting, new ones had not yet been discovered.

Modern Quantum Theory was a real revolution of our understanding of physical process. Compared with this change, Einstein's relativity, born in 1905, seem not much more than very interesting variations on nevertheless classical themes.

Yurko studied at the University of Zagreb, where he received his Diploma in 1950 and his Ph.D in 1953 under the supervision of W. Heisenberg. He moved to Göttingen in 1951-1952 and made his first important contributions to physics, a book of QED published 1955 in Zagreb and outstanding results on QFT, the attempt to clarify the compatibility of special relativity theory with Quantum Theory. Yurko moved back to Zagreb in 1953, initially as a research assistant then as chairman of the Ruder Boskovic Institut.

In 1957 Yurko went to CERN as a permanent member of the Theory Division and then remained there until his death in 1984. Visits to Göttingen, Copenhagen, Strasbourg and Bures sur Yvettes (IHES) had a strong impact on him.

Yurko's main interest was in Quantum Field Theory where he produced his masterpiece in collaboration with Jacques Bros, Henri Epstein and Raymond Stora but he was also interested in nonrelativistic Quantum Theory. He was a man with many cultural interests, with a remarkable taste for music and literature. He appreciated much Dante and Shakespeare. Moreover he was an excellent skier.

I had the big luck to collaborate with Yurko between 1970 and his death. I worked on Epstein-Glaser renormalization. In collaboration with Roland Seneor we proved the existence of the Green's functions in QED in all orders of perturbation theory.

After my departure from CERN I remained in close contacts with Yurko. During my frequent visits to Geneva we had many lively discussions, among other things, about the S-matrix in QED à la Fadeev and the stability of matter.

For Yurko mathematics was invisible culture, a “conditio sine qua non” to structured logical thinking and one of the keys to the development of other sciences. For him mathematics can and must be associated to all types of human activity.

Metaphor and analogy exists in mathematics and physics as well as in literature and religion. Rhetoric exists in mathematics as it exists in politics. Aesthetic exists in mathematics as it exists in the arts.

MATHEMATICS IN PHYSICS

- The role of mathematics
 - Taking by physicists with mixed feeling of admiration and irritation
 - The unreasonable effectiveness (E. Wigner)
 - The pernicious influence (J. Schwartz)
- No “axiomatic” approach (à la Descartes ...) in Physics
 - {Axiom} → Model
- Not essential and perhaps dangerous relation?
 - Physics introduce lack of rigors in M
 - Mathematics would sterilize “true research in ϕ ”

- Intuition to discover

Logic to prove

H. Poincaré

- Some triumphs of theoretical physics non mathematical in their internal structure?

QED the most precise theory ever

invented does not (presumably) make sense

- The way to fundamental discoveries

1) Heuristic non rigorous arguments
(dubious math)

2) Emergence of correct path (swoly!)

3) Proper mathematical framework
appears

- Dyson's birds and frogs

Birds ~ broad visions

Frogs ~ intricate details

Both are needed !

- Dieudonné to Grothendiek:

“to take pleasure by generalizing to

simplify by generalizing” *Poincaré*

- The message of Quantum Science:

Operator algebras, Q-probability, SPD have

been invented to be used in Quantum

Theory.

YURKO's GREAT ENCOUNTERS ALONG THE WAY

Göttingen MPI for Physics W. Heisenberg

„Feldverein“ (Pauli !)

Lehmann Symanzik Zimmermann

LSZ → GSZ

Haag, Lüders, Zumino, Thirring, Källen

➔ 5 books dedicated to QED

- Y. Glaser, Kovarijantna kvanta elektrodynamika
JAZU Zagreb (1955)
- W. Thirring, Principles of QED, Academic Press
(1958) Original version in German 1955
- R. Källen, L'electrodynamique quantique, Lille 1957
CNRS (1959)
- D. Kastler, Introduction à l'electrodynamique
quantique, Dunod (1960)
- P. Urban, Topics in applied QED, Springer (1970)

- Heisenberg's ambitious projects
 - Fundamental theory of elementary particles explaining all known particles (stable and unstable) in terms of a single basic particle
 - Search for observable quantities
 - S-matrix from basic principles

The S-matrix is the roof of the theory, not its foundation (Heisenberg 1956)

- T.D. Lee's model, Phys. Rev. 95 (1954)

$$\begin{array}{ccc}
 \mathcal{H} = \mathcal{H}^B \otimes \mathcal{H}^F & & \\
 \uparrow & & \uparrow \\
 \theta & & N, V
 \end{array}$$

Elementary interaction $N + \theta \leftrightarrow V$

- Modification by Glaser and Källen
 - A model of an unstable particle, Nucl. Phys. 2 (1956)

– The Thirring model in 2 dimensions

$$\mathcal{L} = \bar{\psi} i \gamma \psi - \frac{g}{2} \bar{\psi} \gamma^\mu \psi \cdot \gamma^\mu \psi$$

- renormalizable in 2 dimensions
- explicit solution given by Yurko G.
- equivalence with the Sinus Gordon model

Yurko's first publications

1) New relativistic two-body equation, Phys.

Rev. 98 840 (1955)

2) With H. Lehmann and W. Zimmermann,

Nuovo Cimento 6 (1957) 1122

CERN (Copenhagen then Geneva)

Jacques Prentki, André Martin, Bruno Zumino,
John Bell, Markus Fierz, Raymond Stora, Rudolf
Haag (1975), H. J. Borchers, R. Streater, O.
Steinmann ... and many others

The big time in CERN:

- 20 papers (QM, QFT, Spin Glas),
in collaboration with
P. Collet, J.P. Eckmann, J. Bros, H. Epstein,
D. Iagolnizer, A. Martin, H. Grosse, W. Thirring,
D. Buchholz, S. Coleman, R. Stora, A. Jaffe
- Many discussions with
M. Fierz parastatistics
J. Bell measurement problem
B. Zumino supersymmetry

With experimental physicists:

The ISR and SPS experiments provide spectacular proofs of Yurko's result on maximum growth of cross-sections and comparison of particle-particle and particle-antiparticle collisions

Rudolf Haag spent 1975 one year in CERN
shared the office with Yurko

- Synthesis general relativity of QM
- Events in QM

IHES (Bures sur Yvette)

1958: Motchane's idea: IHES should be a place where

Mathematics: Dieudonné, Grothendieck, Connes, Konsevich, Thom, Bourgignon, ...

and

Physics: Ruelle, Jost, van Hove, Gell Mann, Fröhlich, ...

INTERACT

Yurko was invited to spend a year at IHES (1963-1964) + many short visits

RCP25 (Strasbourg)

Organized by CNRS to improve the

dialogue $M \cap \phi$

2 meetings/year spring and autumn

$M = \{\text{Jean Leray, Pierre Lelong, Bernard}$

$\text{Malgrange, Pierre Cartier, Jacques}$

$\text{Dixmier, Alain Connes, ...}\}$

Yurko enjoyed the lectures and

discussions very much

⑦ USING MATHEMATICS WITH CLARITY AND ELEGANCE

● Stability of Matter

$$H_N = \sum_{i=1}^N \frac{p_i^2}{2m_i} + \sum_{i>j} V(x_i - x_j)$$

$E(N) \sim$ Energy

Problem : $E(N)$ extensive $\Leftrightarrow \lim_{N \rightarrow \infty} \frac{E(N)}{N} = \bar{E}$

One might expect $E(N) \sim N^2$ rather than $E(N) \sim N$

1967 Dyson - Lenard $E(N) \sim N$ for fermions
 V Coulomb but $\bar{E} \gg 1$

1969 Lévy - Leblond
 V Newton $E_N \begin{cases} \nearrow \sim N^3 \text{ Bosons} \\ \searrow \sim N^{7/3} \text{ Fermions} \end{cases}$

1976 Lieb RMP 48
 Simon, Thirring ...

● Hydrogenic atom and Sobolev's inequality

Minimize $E_\psi = T_\psi + W_\psi$ with $\|\psi\|_2 = 1$

$$= \int_{\mathbb{R}^3} |\nabla \psi|^2 dx - z \int |\psi(x)|^2 |x|^{-1} dx$$

$$T_\psi = \|\nabla \psi\|_2^2 \geq S \|\psi\|_6^2$$

$$\Leftrightarrow T_\psi \geq S \|\psi\|_3^2$$

with $S_\psi = \|\psi\|_3^2$

$$E_\psi \geq \inf [S \|\psi\|_3^2 - z \int |x|^{-1} \psi^2 dx]$$

$$E \geq \frac{1}{2} z^2$$

Lower bound of $\sigma(H)$ $H \geq 0$

(8)

Yurko + R.A. Bertlmann

Simplest case

$$H = \frac{p^2}{2m} + V(x) \quad V(x) \geq 0 \quad x \in \mathbb{R}^d$$

$$t > 0 \quad Z(t) = \text{tr} e^{-tH} \leq \text{tr} e^{-\frac{p^2}{2m} t} e^{-tV}$$

$$V(x) = \lambda |x|^s \quad \parallel \quad Z_c(t)$$

$$Z_c(t) = (2m)^{d/2} t^{-s} K_d$$

$$K_d = \int \frac{dy}{(4\pi)^{d/2}} e^{-V(y)}$$

$$Z_c(t) \geq \text{tr} e^{-tH} = \sum_{k=1}^{\infty} e^{-tE_k}$$

$$\sigma(H) = \{E_k\}_{k \in \mathbb{N}}$$

$$\sum_{k=1}^n e^{-tE_k} \geq n e^{-tE_n}$$

$$\Rightarrow E_n \geq \frac{1}{t} \ln \frac{n}{Z_c(t)}$$

Best bound given by sup over t

$$E_n^{s.c.} = n^{\frac{-s}{2+s}} \left(\frac{n}{K_d} \right)^{1/s}$$

Generalize \rightarrow Physics Reports 134 (1986)
279-296

WIGHTMAN QFT IN A NUTSHELL ⑨

- Mathematical definition \rightarrow Q-Field ϕ ?
 \hookrightarrow QFT ?
1956 $\phi(x) \Leftrightarrow$ Operator valued Schwartz distribution
- 1956 QFT \Leftrightarrow Encoded in
 $\Omega \sim$ vacuum $\langle \Omega, \phi(x_1) \dots \phi(x_n) \Omega \rangle$
 $\langle \Omega, \phi(x_1) \dots \phi(x_n) \Omega \rangle = F^{(n)}(x_2-x_1, x_3-x_2, \dots, x_n-x_{n-1})$

- Lorentz invariance
 $F^{(n)}(\Lambda \xi_1, \dots, \Lambda \xi_{n-1}) = F^{(n)}(\xi_1, \dots, \xi_{n-1})$

- Spectral condition

$p =$ energy momentum
Physical states $p \in V_+ = \{p \mid p^2 \geq 0\}$
 $\Rightarrow F^{(n)} = \mathcal{F} G^{(n)}$

$$G^{(n)}(p_1, \dots, p_{n-1}) \quad p_j \in V_+ \quad \forall j$$

$F^{(n)}$ is the boundary value for $z_j \rightarrow 0$
of a function of $z_i = \xi_i + i\eta_i$ holomorphic
for $\eta_i = \text{Im } z_i \in V_+$

This domain is called the tube !

- Lorentz invariance $\Rightarrow F^{(n)}(z_1, \dots, z_{n-1})$
can be continued to complex Lorentz
transformation

New domain of analyticity called
extended tube

Local commutativity

10

$$[\phi(x), \phi(y)] = 0 \quad \text{if } (x-y)^2 < 0$$

$F^{(n)}(z_1, \dots, z_{n-1})$ can be further analytically extended when z_1, \dots, z_{n-1} runs over the extended tube

$$z_1, \dots, z_{j-1} + z_j, -z_j, z_j + z_{j+1}, \dots, z_{n-1}$$

permuted extended tube

$F^{(n)}(z_1, \dots, z_{n-1})$ is analytic and single valued in the union of the extended tube and permuted extended tube.

Main Theorem

To a sequence $F^{(n)}$ of distributions satisfying the Wightman axioms there correspond a unique field satisfying all the axioms and having the distributions $F^{(n)}$ as Wightman distributions

CONNECTION BETWEEN WIGHTMAN, LSZ AND GLZ QFT

(11)

W Phys. Rev (1950)

LSZ Nuovo Cimento (1955)

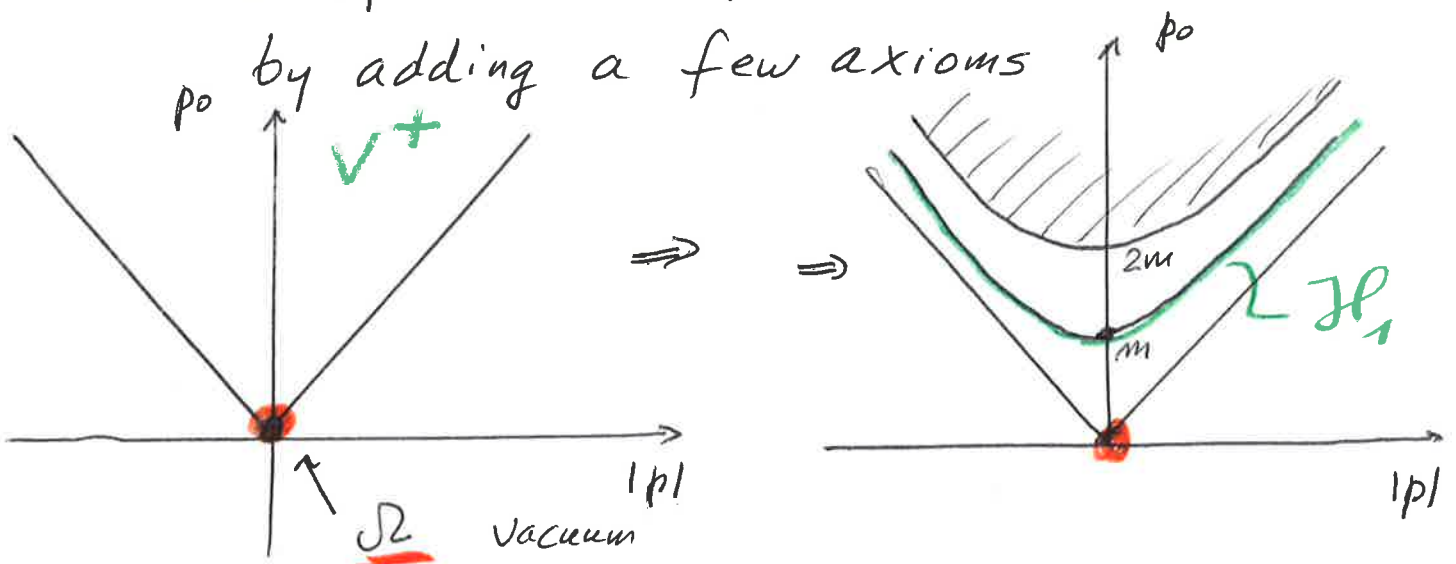
GLZ Nuovo Cimento (1957)

Two formulations of QFT

- W = high level of mathematical rigor, interacting fields, local aspect of the theory, never talks of particles, removed from experiments
- LSZ = less rigor, intuition, S-matrix, perturbation theory, particles in the center, interacting fields called "interpolating fields", more closer to experiments but far away of understanding dynamic

• STEINMAN CMP (1968, 1970)

LSZ can be obtained rigorously as a special case of a Wightman theory by adding a few axioms



To be added

12

$$\langle \mathcal{R}, A \mathcal{R}_1 \rangle \neq 0$$

equal to those of a free field LSZ-assumption

Asymptotic assumptions LSZ

1) describe free particles by free field

2) Cluster property

$$k = 1 \dots n-1, \quad y = y_1 \dots y_{n-k}$$

$$\lim_{\lambda \rightarrow \infty} W_n(x, y + \lambda a) = W_k(x) W_{n-k}(y) \quad \text{if } a^2 < 0$$

Scattering event \Rightarrow particles far apart \Rightarrow
interaction can be neglected \Rightarrow description by
free fields

3) S-matrix

$$A_{(x)}^{\text{out}} = S^* A^{\text{in}}(x) S$$

4) Asymptotic completeness

$$\mathcal{H} = \mathcal{H}_{\text{in}} = \mathcal{H}_{\text{out}}$$

GLZ Theorem \Leftrightarrow LSZ counterpart
of Wightman's
reconstruction
theorem

EQUIVALENCE OF OSTERWALDER-SCHRADER AND WIGHTMAN FORMULATION OF QFT

13

Dyson in 1949: problems in QED can be avoided by replacing t by it

$$\tau = it \quad \text{Wick rotation}$$

Wigner: time ordered Green functions of Euclidean QED

Osterwalder - Schrader (1973, 1975): Euclidean Field Theory

Euclidean QFT $\xrightarrow{t \rightarrow it}$ W-QFT

Euclidean QFT + O.S. Axioms for the Schwinger function S_n

\Downarrow Analytic continuation

W-QFT + W-Axioms

Question:

Wightman Axioms \Leftrightarrow O.S. Axioms

V. Glaser CMP 37 257 - 272 (1974)

The main point of Glaser's approach is to stress the fact that the analytic behavior off the diagonal is completely governed by the analytic structure on the diagonal

$$\phi_m(z) = A(z_1) \dots A(z_n) \Omega$$

$$A_{mm}(\bar{z}', z) = \langle \phi_m(z'), \phi_m(z) \rangle$$

Diagonal $A_{mm} \Leftrightarrow m = m$

(14)

$\phi_m(z)$ is a tempered analytic function in the tube

$$\mathcal{T}_m = \left\{ z \in \mathbb{C}^{4n} \mid \operatorname{Im} z_k \in V_+, \operatorname{Im} (z_k - z_{k-1}) \in V_+ \right\}$$

$k = 2, \dots, n$

Positivity condition

$$\sum_{n, m} \int A_{nm}(\bar{z}', z) f_m(z') f_m(z) d\mu(z) \geq 0$$

$$d\mu(z) = e^{-\phi_m(z)} d\lambda_m(z)$$

↑
Lebesgue measure on \mathbb{C}^{2n}

Results

- The $S_n(x_1, \dots, x_{n+1})$ can be analytically continued into the product of the right complex planes

$$\mathcal{P}_+^{n+1} = \left\{ z = x + iy \in \mathbb{C}^{n+1} \mid x \in \mathbb{R}_+^{n+1} \right\}$$

The functions $W_{n+1}(iz^0, z)$ can be analytically continued into the tube

$$\mathcal{T}_m = \left\{ z \in \mathbb{C}^{4n} \mid \operatorname{Im} z_k \in V_+ \quad k=1 \dots n \right\}$$

Quantum Energy Inequalities

Epstein Glaser Jaffe *Nuovo Cimento* 36
(1965)

- Energy density of Wightman fields admit negative expectation values
- Contradiction with the positivity of the energy-momentum tensor of classical relativity ensuring causality.

Solution of the conflict

Smearing out the densities in space or
time

- Classical positivity restored at medium and large scales

THE POLYNOMIAL MAP

Yurko, R. Stora, J. Wess, B. Zumino in 1981 discussed about the mathematical structure of the Higgs potential in SS theories

B. Zumino in “Unified Theories of Elementary Particles”, Springer Verlag (1988)

J. Wess and J. Gabber, SS and Supergravity, Princeton Series in Physics (1983)

$$Z = (z_1, \dots, z_n), \quad W = (w_1, \dots, w_n) \in \mathbb{C}^n$$

∴ Polynomial maps

$$Z \rightarrow W(Z) \quad w_i(Z) = P_i(Z)$$

Special case

$$P_i(Z) = \frac{\partial}{\partial z_i} L(Z)$$

Minima of

$$V(Z) = |P(Z)|^2 = \sum_{i=1}^n |P_i(Z)|^2$$

- V is a plurisubharmonic function

$$Z(t) = z_0 + ht \quad h \in \mathbb{C}^n$$

$$\frac{\partial^2}{\partial t \partial t} V(Z(t)) = \sum_{k=1}^n \left| \sum z_i \frac{\partial P_k}{\partial z_i} \right|^2 \geq 0$$

V cannot have anywhere a local maximum unless $V = \text{const} \Rightarrow P(Z) = \text{const}$.

- Confining potential

$$\Rightarrow \lim_{|z| \rightarrow \infty} V(Z) = +\infty$$

independently of the way $Z \rightarrow \infty$

Necessary condition for confinement

$$J(P) \neq 0$$

$$J(P) = \det \partial P_i / \partial z_j$$

general class of non-confining potentials

$$P_i(z) = C_i + \sum_{j=1}^{n-1} p_{ij}(z) H_j(z)$$

p_{ij} polynomials

H_i homogeneous polynomials of degree

$$\deg H_i \geq 1$$

For a confining potential $\exists z_0 \in \mathbb{C}^n$ such that $V(z_0) = 0$

This property follows from

V confining $\Rightarrow P(\mathbb{C}^n) = \mathbb{C}^n$

Proof $S = \{z \in \mathbb{C}^n \mid J(z) = 0\}$

$J \neq 0$ S closed algebraic variety of dimension $n-1$

$\Rightarrow \mathbb{C}^n \setminus S$ open connected set

$$\Omega = P(\mathbb{C}^n \setminus S)$$

\Rightarrow non empty open connected set

Consider $\partial \Omega$

$\Rightarrow \mathbb{C}^n \setminus \partial \Omega$ is again an open connected set in \mathbb{C}^n

Philippe Blanchard • Erwin Brüning

Mathematical Methods in Physics

Distributions, Hilbert Space Operators,
Variational Methods, and Applications
in Quantum Physics

Second Edition

*Dedicated to the memory of
Yurko Vladimir Glaser and Res Jost,
mentors and friends*

 Birkhäuser

Green's functions for theories with massless particles (in perturbation theory)

by

Philippe BLANCHARD ⁽¹⁾ and Roland SENEOR ⁽²⁾

ABSTRACT. — With the method of perturbative renormalization developed by Epstein and Glaser it is shown that Green's functions exist for theories with massless particles such as Q. E. D., and $\lambda: \phi^{2n}$: theories. Growth properties are given in momentum space. In the case of Q. E. D., it is also shown that one can perform the physical mass renormalization.

RÉSUMÉ. — A l'aide de la méthode de renormalisation perturbative développée par H. Epstein et V. Glaser on montre l'existence des fonctions de Green pour des théories comprenant des particules de masse nulle telles que l'électrodynamique quantique et les théories $\lambda: \phi^{2n}$. On donne des propriétés de croissance dans l'espace des moments. Pour l'électrodynamique, on montre qu'il est possible d'effectuer la renormalisation de la masse à sa valeur physique.

I. PRELIMINARIES

1. Introduction

Notations are those of [1]. Any change will be explained.

It has been shown in [1] that for $g_i(x)$ in $\mathcal{S}(\mathbb{R}^4)$ the various field ope-

⁽¹⁾ C. E. R. N., Geneva and University of Bielefeld (W. Germany).

⁽²⁾ C. E. R. N., Geneva and Centre de Physique Théorique, École Polytechnique, Paris.

LE RÔLE DE LA LOCALITE DANS LA RENORMALISATION PERTURBATIVE
EN THEORIE QUANTIQUE DES CHAMPS *)

H. Epstein et V. Glaser
CERN - Genève

R E S U M E

Cette conférence, faite à la réunion de Strasbourg de mai 1970 résume un article à paraître prochainement par les mêmes auteurs ¹⁾.

*) Conférence présentée à la réunion de mai 1970 de la R.C.P. No 25 à Strasbourg.

EXISTENCE (EN THEORIE DES PERTURBATIONS) DES FONCTIONS DE GREEN

DE L'ELECTRODYNAMIQUE QUANTIQUE *)

P. Blanchard et R. Seneor +)

CERN - Genève

- *) Rapport présenté au colloque sur la renormalisation,
CNRS, Marseille, 14-18 juin 1971.
- +) Centre de Physique Théorique de l'Ecole Polytechnique
(Paris).

Genève, le 8/2/82

Mon cher Blanchard,

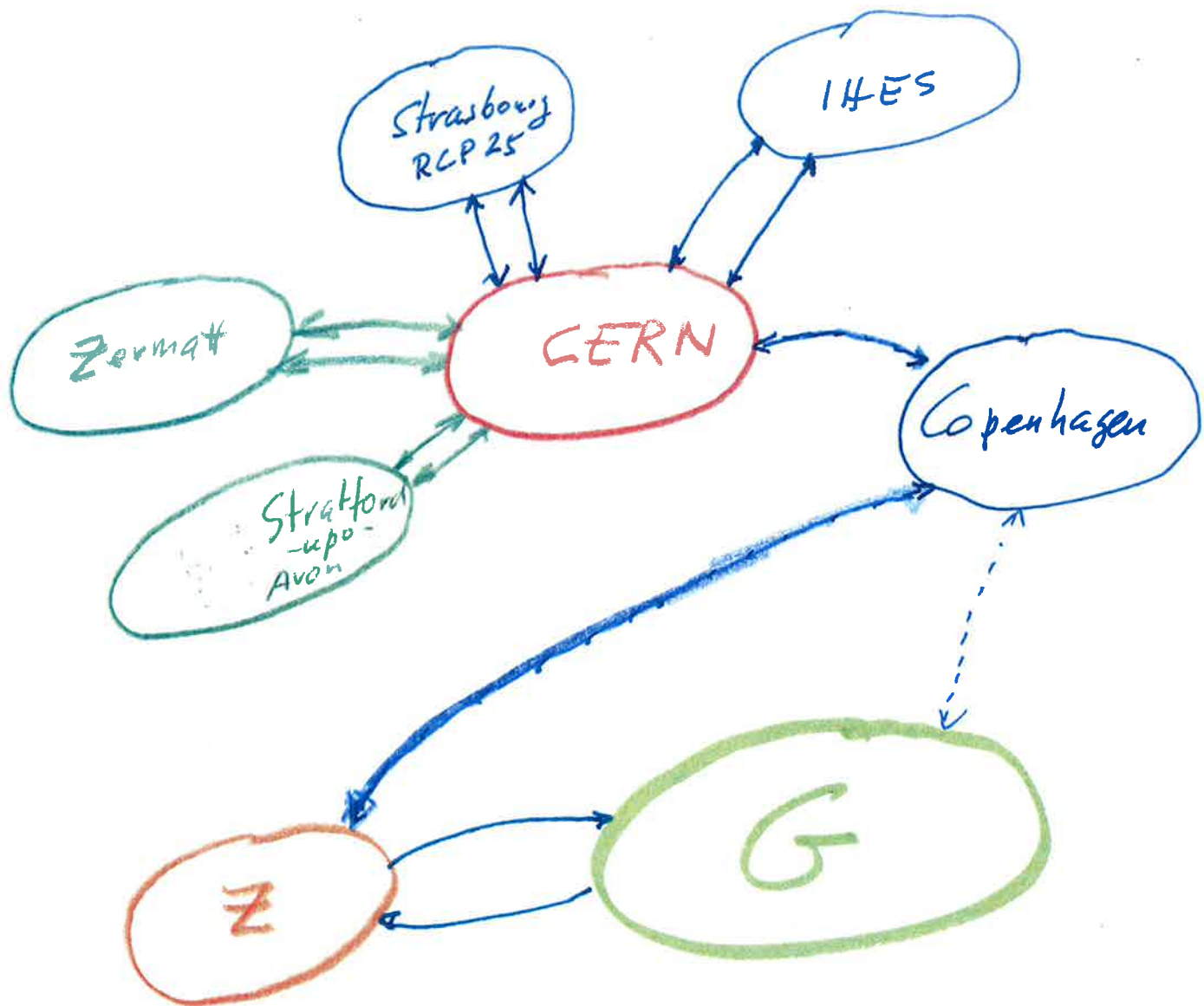
Je t'écris ~~de~~ nouveau parce que je n'ai pas réussi à te joindre par téléphone. Je te remercie d'abord pour ta lettre et ton manuscrit, que j'ai parcouru avec plaisir.

Je t'écris principalement pour te dire, que le CERN est d'accord pour te payer un séjour de 2 semaines, comme convenu. ^{je} Moins ici tout le temps jusqu'au 13 Mars, quand on part pour deux semaines à Zermatt. D'après ta lettre c'est la période qui te convenait le plus.

Donc je t'attends avec plaisir. Après le 27 Mars je suis de nouveau ici si par hasard tu changerais de programme.

Avec toutes mes amitiés ton

Juri Glaser



Yuvko's graph

- \longleftrightarrow } "physical" edges
- \dots }
- \longleftrightarrow spare time activities