MAGIC GAMMA-RAY TELESCOPE OBSERVATION OF THE PERSEUS CLUSTER OF GALAXIES: IMPLICATIONS FOR COSMIC RAYS, DARK MATTER AND NGC 1275


(The MAGIC Collaboration)

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ABSTRACT

The Perseus galaxy cluster was observed by the MAGIC Cherenkov telescope for a total effective time of 24.4 hours during November and December 2008. The resulting upper limits on the γ-ray emission above 100 GeV are in the range of 4.6 to 7.3 × 10^{-12} cm^{-2} s^{-1} for spectral indices from −1.5 to −2.5; thereby constraining the emission produced by cosmic rays, dark matter annihilations and the central radio galaxy NGC 1275. Results are compatible with cosmological cluster simulations for the cosmic ray induced γ-ray emission, constraining the average cosmic ray-to-thermal pressure to < 4% for the cluster core region (< 8% for the entire cluster). Using simplified assumptions adopted in earlier work (a power-law spectrum with an index of −2.1, constant cosmic ray-to-thermal pressure for the peripheral cluster regions while accounting for the adiabatic contraction during the cooling flow formation), we would limit the ratio of cosmic ray-to-thermal energy to $E_{CR}/E_{th} < 3\%$. Improving the sensitivity of this observation by a factor of about seven will enable us to scrutinize the hadronic model for the Perseus radio mini halo: a non-detection of γ-ray emission at this level implies cosmic rays fluxes that are too small to produce enough electrons through hadronic interactions with the ambient gas protons to explain the observed synchrotron emission. The upper limit also translates into a level of γ-ray emission from possible annihilations of the cluster dark matter (the dominant mass component) that is consistent with boost factors of $\sim 10^{4}$ for the typically expected dark matter annihilation induced emission. Finally, the upper limits obtained for the γ-ray emission of the central radio galaxy NGC 1275 are consistent with the recent detection by the Fermi-LAT satellite. Due to the extremely large Doppler factors required for the jet, a one-zone synchrotron self-Compton model is implausible in this case. We reproduce the observed spectral energy density with the structured jet (spine-layer) model which has previously been adopted to explain the high-energy emission of radio galaxies.

Subject headings: gamma-rays: observations, galaxies: clusters: individual (Perseus)
1. INTRODUCTION

Clusters of galaxies provide us with the opportunity to study an “ecosystem”, a volume that is a high-density microcosm of the rest of the Universe. Clusters of galaxies are the largest and most massive gravitationally bound systems in the Universe, with radii of few Mpc and total masses $M \sim (10^{14} - 10^{15})M_\odot$, of which galaxies, gas and dark matter (DM) contribute roughly for 5, 15 and 80%, respectively (see e.g. Sarazin (1988), Kochanek et al. (2003) and Voi (2005) for a general overview). While no cluster has been firmly detected as a γ-ray source so far, (Reimer et al. 2003; Perkins et al. 2006; Perkins 2008; Aharonian et al. 2009a; Domínguez et al. 2009; Galante et al. 2009; Khur et al. 2009; Acero et al. 2009), they are expected to be significant γ-ray emitters on the following general grounds. (i) Clusters are actively evolving objects and being assembled today, in the latest and most energetic phase of hierarchical structure formation. (ii) Clusters serve as cosmic energy reservoirs for powerful sources such as radio galaxies and supernova-driven galactic winds. (iii) Finally, clusters contain large amounts of gas with embedded magnetic fields, often showing direct evidence for shocks and turbulence as well as relativistic particles. For recent reviews regarding non-thermal processes in clusters as well as numerical simulations, see Blasi et al. (2007) and Dolag et al. (2008).

In the cosmological hierarchical clustering model, large scale structures grow hierarchically through merging and accretion of smaller systems into larger ones, and clusters are the latest and most massive objects to form (e.g. Peebles 1993). Recently, high resolution X-ray observations by Chandra and XMM-Newton orbiting telescopes provided confirmation of this picture (e.g. Rosati et al. 2002; Voi 2005). During the course of cluster assembly, energies of order of the final gas binding energy $E_B \sim 3 \times (10^{61} - 10^{63})$ erg should be dissipated through merger and accretion shocks (collectively called “structure formation shocks”) as well as turbulence. The energy is expected to be dissipated on a dynamical timescale of $\tau_{\text{dyn}} \sim 1$ Gyr. Hence the corresponding rates of energy release are $L \sim (10^{45} - 10^{47})$ erg/s, so even a small fraction of this energy channeled into non-thermal particles can be of major observable consequence. Shocks and turbulence are also likely to accelerate non-thermal electrons and protons to high energies (e.g. Jaffe 1977; Schlickeiser et al. 1987; Brunetti et al. 2001b; Olmo et al. 2002; Miniati 2002, 2003; Sarazin 2002; Brunetti et al. 2003; Inoue et al. 2005; Brunetti et al. 2007; Brunetti & Lazarian 2007; Pfrommer et al. 2007; Pfrommer 2008; Pfrommer 2008; Falcke-Goncalves et al. 2009).

Clusters are also home to different types of energetic outflows, and the intra-cluster medium (ICM) can function as an efficient energy reservoir. Most clusters are seen to harbor radio galaxies around their central regions, whose large, powerful jets of relativistic plasma are interacting vigorously with the ICM (Heinz et al. 1998; Forman et al. 2003; Fabian et al. 2006). A crude estimate of the total energy output by a single powerful radio galaxy is $E_{RG} \sim (10^{60} - 10^{62})$ erg, taking reasonable values for the kinetic luminosity $L_{RG} \sim (10^{45} - 10^{46})$ erg/s and effective duration of activity $t_{RG} \sim (10^7 - 10^8)$ yr (McNamara & Nulsen 2007). The integrated output from the whole cluster radio galaxy population should be even greater (Enßlin et al. 1997; Inoue & Sasaki 2001). Although rarely seen in present-day clusters, another source which should have been active in the past are galactic winds, i.e. outflows driven by the joint action of numerous supernovae (Völk et al. 1996). Taking the observed mass of Fe in the ICM to be $M_{F,ICM} \sim 3 \times (10^9 - 10^{10}) M_\odot$, the energy and Fe mass ejected by each supernovae to be respectively $E_{SN} \sim 10^{54}$ erg and $M_{F,SN} \sim 0.1 M_\odot$, and an outflow efficiency $\xi_{GW} \sim 0.1$ (Veilleux et al. 2005), we estimate the total galactic wind energy output to be $E_{GW} \sim \xi_{GW} E_{SN}/M_{F,SN} M_{F,ICM} \sim 3 \times (10^{60} - 10^{61})$ erg. In any case, along with dumping energy, these sources can inject substantial quantities of non-thermal particles into the ICM, or could have done so in the past.

Faraday rotation measurements provide a powerful tool to probe the strength of the intra-cluster magnetic fields (Kim et al. 1991), and even their distribution (Clarke et al. 2001), resulting in the ICM now being known to be permeated by magnetic fields with strengths $B \sim (1 - 10) \mu$G (Carilli & Taylor 2002; Vogt & Enßlin 2003), which allow for particle acceleration in shocks up to γ-ray emitting energies. Observations of radio halos and radio relics have already established that synchrotron emitting electrons with energies reaching $\sim 10$ GeV are present in at least some clusters (Feretti 2003; Ferrari et al. 2008), although their precise origin is still unclear. Similar populations of electrons but with harder spectra may produce γ-rays efficiently via inverse Compton (IC) up-scattering of the cosmic microwave
MAGIC Observation of the Perseus Galaxy Cluster

2. TARGET SELECTION AND PRELIMINARIES

The Perseus cluster, also called A426, is at a distance of 77.7 Mpc \((z = 0.018)\). It is the brightest X-ray cluster \cite{edge1992} and hosts a massive cooling flow with high central gas densities of 0.05 \(\text{cm}^{-3}\) (see Table 1). Perseus furthermore hosts a luminous radio mini-halo – diffuse synchrotron emission that fills a large fraction of the cluster core region – and shows a source extension of \(\sim 200\) kpc \cite{pedlar1990}. This radio mini-halo is well modeled by the hadronic scenario where the radio emitting electrons are produced in hadronic cosmic ray (CR) proton interactions with ambient gas protons requiring only a very modest fraction of a few percent CR pressure relative to thermal pressure \cite{pfrommer2004}. In particular the similarity of the thermal X-ray emission and that of the radio mini-halo comes about naturally as both processes scale with the number density squared. An alternative model for the radio emission has been proposed by Gitti et al.\cite{gitti2002} which explains the radio mini-halo by re-acceleration of relativistic electrons through second order interactions with magneto-hydrodynamic (MHD) turbulence. However, it remains to be shown whether the necessary turbulent energy density can be provided throughout the entire cooling flow region of Perseus. These conditions provide high target densities for hadronic CR-p-p interactions and enhance the resulting \(\gamma\)-ray flux.

The Perseus galaxy cluster was carefully chosen over other nearby clusters after considering the expected \(\gamma\)-ray emission from the pion-decay and DM annihilation. Moreover, the central radio galaxy NGC 1275 is expected to be a promising GeV-TeV target, and hence is another strong motivation to observe this cluster. In the following subsections, we detail our considerations.

2.1. Cosmic Ray Induced Emission

In the course of this work, we used cosmological simulations of the formation of galaxy clusters to inform us about the expected spatial and spectral characteristics of the CR induced \(\gamma\)-ray emission. A clear detection of the IC emission from shock-accelerated CR electrons will be challenging for Imaging Atmospheric Cherenkov Telescopes (IACTs) due to the large angular extent of these accretion shocks that subtend solid angles corresponding to up to six virial radii. For these instruments, the spatially concentrated pion-decay \(\gamma\)-ray emission resulting from hadronic CR interactions that dominates the total \(\gamma\)-ray luminosity \cite{pfrommer2008} should be more readily detectable than the emission from the outer region.

To address the question of universality and predictability of the expected \(\gamma\)-ray emission we simulated a sample of 14 galaxy clusters that span one and a half decades in mass and show a variety of dynamical states ranging from relaxed cool core clusters to violent merging clusters (details are given in Sect. 2.1). In order to find the most promising target cluster in the local Universe for detecting the pion decay emission, we computed the scaling relations between \(\gamma\)-ray luminosity and cluster mass of our sample \cite{pfrommer2008} and used these to normalize the CR induced emission of all clusters in a complete sample of the X-ray brightest clusters (the extended HI-FLUGCS catalogue, Reiprich & Böhringer \cite{reiprich2002}). This favors high-mass, nearby galaxy cluster with a scaling \(M_{200}^3/\Delta_{\text{that}}^2\), where \(M_{200}\) is the virial mass\(^1\), \(\Delta_{\text{that}}\) the luminosity distance, and \(\beta \simeq 1.32\) a weakly model dependent scaling parameter that provides the rank ordering according to the brightness of each individual cluster \cite{pfrommer2008}. As a second criterion, we required low zenith angle observations, i.e. below 35 deg, that ensure the lowest possible energy thresholds and the maximum sensitivity for the detector. We carefully modeled the most promising targets, accounting for the measured gas density and temperatures from thermal X-ray measurements while assuming a constant CR-to-thermal gas ratio \cite{pfrommer2004}. Cluster-wide ex-

\(^1\) We define the virial mass \(M_\Delta\) and the virial radius \(R_\Delta\) as the mass and radius of a sphere enclosing a mean density that is \(\Delta = 200\) times the critical density of the Universe.
tended radio synchrotron emission that informs about present high-energy processes were additionally taken into account before we selected the Perseus cluster as our most promising source. Although other clusters showed a somewhat higher γ-ray flux in our simulations (e.g. Ophiuchus), the facts that Perseus is observable at low zenith angles and that the expected emission is more spatially concentrated make it the best suited target for this observation.

2.2. Dark Matter Content

Typically up to 80% of the total mass of a galaxy cluster is in the form of non-baryonic DM. Since the DM annihilation γ-ray signal is expected to be proportional to the integrated squared DM density along the line of sight (Evans et al. 2004; Berestrom & Hooper 2004), it is obvious that galaxy clusters could be good candidates to look for DM as well. This is true despite the fact that they are located at much larger distances than other potential DM candidates, such as dwarf spheroidal galaxies satellites of the Milky Way or the Galactic Center. One obvious reason is the huge amount of DM hosted by clusters compared with the rest of candidates. Perseus, for example, is located ~1000 times farther than Milky Way dwarfs, but it contains roughly six orders of magnitude more DM than the Willman 1 dwarf galaxy, one of the most promising DM candidates according to recent work (Strigari et al. 2005; Aliu et al. 2009). Additionally, the presence of substructures could be of crucial importance. Substructures in clusters may significantly enhance the DM signal over the smooth halo, while we do not expect this to be of special relevance for dwarf galaxies since their outer regions are severely affected by tidal stripping (Pinzke et al. 2009; Sánchez-Conde et al., in prep.).

Essentially, the annihilation flux is proportional to the product of two parameters (see e.g. Evans et al. 2004 for details): a first one that captures all the particle physics (DM particle mass, cross section, etc), that we will label as \( f_{\text{PSUSY}} \), and a second one, \( J_{\text{astro}} \), that accounts for all the astrophysical considerations (DM distribution, telescope PSF, etc). The particle physics factor just acts as a normalization in the expected annihilation flux, so we can neglect it when performing a comparative study – as we are doing in this section. Concerning the astrophysical factor, the DM distribution is commonly modeled with radial density profiles of the form \( \rho(r) = \rho_s / \left[ (r/r_s)^\gamma + (r/r_s)\right]^{(\beta-\gamma)/\alpha} \), where \( \rho_s \) and \( r_s \) represent a characteristic density and a scale radius respectively (Kravtsov et al. 1998). These density profiles are well motivated by high-resolution N-body cosmological simulations. Here we adopt the Navarro-Frenk-White (Navarro et al. 1997; hereafter NFW) DM density profile, with \( (\alpha, \beta, \gamma) = (1,3,1) \). For an NFW profile, 90% of the DM annihilation flux comes from the region within \( r_s \), so that the corresponding integrated luminosity is proportional to \( r_s^3 \rho_s^2 \). We can derive \( r_s \) and \( \rho_s \) for Perseus, assuming \( M_{200} = 7.7 \times 10^{14} \, M_\odot \) (as given in Table 1) and a concentration of ~6 (as given by the Bullock et al. 2001 virial mass-concentration scaling relation). We obtain \( r_s = 0.384 \, \text{Mpc} \) and \( \rho_s = 1.06 \times 10^{15} \, \text{M}_\odot \, \text{Mpc}^{-3} \), which translates into a total value of \( J_{\text{astro}} \sim 1.4 \times 10^{16} \, \text{GeV}^2 \, \text{cm}^{-5} \) for the scale radius region. In the case of Coma, although slightly (~15%) more massive than Perseus, the fact that it is located significantly farther (101 Mpc) translates into a slightly lower annihilation flux. Virgo, only 17 Mpc away from us, gives a larger DM annihilation flux, but here the large extension of the region from which most of the annihilation flux is expected to come compared with Perseus \( (r_s \sim 1.2 \, \text{deg} \text{ and } r_s \sim 0.3 \, \text{deg}, \text{respectively}) \) could represent an obstacle from the observational point of view. Source extension is of special relevance for single telescope IACTs, for which point-like sources (sources with an angular extension smaller or similar to the telescope PSF) are more readily observable.

2.3. The NGC 1275 Radio Galaxy

The central NGC 1275 radio galaxy is another strong motivation for γ-ray observations of the Perseus galaxy cluster. The detection at TeV energies of the radio galaxies M 87 (Aharonian et al. 2006b) and Centaurus A (Aharonian et al. 2009b) has forced a substantial revision of the paradigm whereby VHE emission is a characteristic property of highly relativistic jets closely aligned with the line of sight, establishing radio galaxies as a new class of VHE γ-ray emitters. Note that NGC 1275 has various characteristics in common with Centaurus A which has also been interpreted as a possible source of ultra-high energy cosmic rays (Hardcastle et al. 2009).

The NGC 1275 radio galaxy is the brightest radio source in the northern sky. Its jet inclination angle seems to increase from 10 − 20 deg at millarcseconds scales up to 40 − 60 deg at arcseconds scales (Dunn et al. 2006). Note that NGC 1275 was classified as a blazar by Angel & Stockman (1980) because of its optical polarization, and it has been seen to vary in the optical on time scales of a day (Geller et al. 1979). All these elements are promising from the point of view of the TeV detectability, since they suggest that the emission region is located at the base of the jet. In these conditions, in the scenario based on the structured jet model (Tavecchio & Ghisellini 2008), we expected VHE emission from the layer of the jet at a level detectable by MAGIC.

3. MAGIC OBSERVATION AND RESULTS

The MAGIC (Major Atmospheric Gamma Imaging Cherenkov) telescope is located on the Canary Island of

<table>
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<tr>
<th>TABLE 1</th>
<th>PROPERTIES OF THE PERSEUS GALAXY CLUSTER</th>
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<tr>
<td>( z )</td>
<td>( D_{\text{lim}} ) [Mpc]</td>
</tr>
<tr>
<td>0.0183</td>
<td>77.7</td>
</tr>
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</table>

La Palma (2200 m asl, 28.45°N, 17.54°W). With a primary mirror diameter of 17 m, it is currently the largest IACT. CRs impinging the Earth atmosphere originate atmospheric showers that in turn produce Cherenkov light. The ultra-violet Cherenkov flashes are reflected in the focal plane of the telescope, where a camera of 577 photomultipliers records the resulting images. MAGIC reconstructs the incoming γ-ray directions with an accuracy of about 0.1 deg and achieves an energy resolution above 150 GeV of about 20% (see Albert et al. (2008c) and Aliu et al. (2009b) for details).

3.1. Observation and Analysis

MAGIC observed the Perseus cluster for 33.4 hours during November and December 2008, at zenith angles between 12° and 32°, which guarantees the lowest energy threshold. The observation was performed in the false-source tracking (wobble) mode (Fomin et al. 1994) pointing alternatively to two different sky directions, each at 0.4 deg distance from the nominal target position.

The main background for Cherenkov telescopes is due to the hadronic cosmic rays and the night sky background. Our standard analysis procedure is the following (for a detailed description see [Albert et al. 2008c]).

- Data calibration and extraction of the number of photoelectrons per pixel is done (Albert et al. 2008a).
- Image cleaning procedure using the amplitude and timing information of the calibrated signals. Particularly, the arrival times in pixels contain -ions.
- More than 6 photoelectrons (core pixels) are required to be within a time window of 4.5 ns and for pixels containing > 3 photoelectrons (boundary pixels) within a time window of 1.5 ns from a neighboring core pixel. For the surviving pixels of each event, the shower parameters are reconstructed using the Hillas parametrization algorithm (Hillas 1985).
- Hadronic background suppression is achieved using a multivariate method called Random Forest (Breiman 2001, Albert et al. 2008b), that uses the Hillas parameters to define an estimator called hadronness (it runs from 0 for gammas to 1 for hadrons) by comparison with Monte Carlo (MC) γ-ray simulations. Moreover, the Random Forest method is used for the energy estimation of a reconstructed shower. The gamma/hadron (g/h) separation in the analysis was optimized on a sample of well understood Crab Nebula data, which is commonly accepted as standard reference source for VHE astronomy.
- Part of the data have been rejected mainly due to the bad weather conditions during some observation days. The total data rejected amount to ~ 27%, resulting in 24.4 hours effective observation time of very high data quality. Independent cross-checks were performed on the data giving compatible results.

3.2. Results

Given the good data quality and the low zenith angles of observation, the energy threshold results to be 80 GeV. Beyond this threshold, no significant excess of γ-rays above the background was detected in 24.4 hours of observation. In Figure 1 the α-plot for energies above 250 GeV, where the best integral sensitivity is obtained from a Crab Nebula data sample, is reported. The α-parameter is defined as the angular distance between the shower image main axis and the line connecting the observed source position in the camera and the image barycenter. Background events are isotropic in nature, and thus produce randomly oriented shower images. This results in a more or less smooth event distribution in the α-plot. The γ-ray events due to the source, on the other hand, are predominantly aligned to the observed position in the camera. For a detected source, this results in a significant excess of events at small α. A fiducial region α < 6° and a hadronness cut of 0.05 are chosen by optimizing the analysis on a Crab Nebula data sample.

In Figure 2 the significance map for events above 150 GeV in the observed sky region is shown. The source independent DISP method has been used. This implies the rise of the energy threshold from 80 GeV to around 150 GeV (see Domingo-Santamaria et al. 2003 for a detailed description). The significance distribution in the map is consistent with background fluctuations. In Figure 3 X-ray contours from the XMM-Newton observations (Churazov et al. 2003) are also shown.

The significance was calculated according to Eqn. 17 of Li & Ma (1983) and upper limit estimation is performed using the Rolke method (Rolke et al. 2005). The upper limits in number of excess events are calculated with a confidence level of 95%. For the upper limit calculation, a systematic uncertainty of 30% in the energy estimation and effective area calculation is taken into account. Our systematic error budget is obtained by adding up the individual contributions in quadrature. The different sources of systematic uncertainties are mainly related to the differences between the real experimental conditions and the simulated ones (see Albert et al. 2008b for a detailed discussion on the systematic errors). The photon flux upper limit is finally reconstructed for a general γ-ray spectrum as described in Aliu et al. (2009a).

In sections 4 and 5 we will discuss the implications of this observation for the CR and DM annihilation induced γ-ray flux, respectively. Using the true density profile as obtained by X-ray measurements (Churazov et al. 2003), we will be able to model the spatial characteristics of the CR induced γ-ray signal. Our simulations indicate that
60% of the total γ-ray flux are contained within a circle of radius $r_{0.6} = 0.15$ deg (this angular scale corresponds to a physical radius of 200 kpc). We then compare the flux from within this region to the upper limits. As the characteristics of the considered emission region are close to a point source we use point-like upper limits. The same conclusion is valid also for the DM annihilation signal. In this case, as explained in section 2.2, the 90% of the expected emission is coming form the scale radius region. For Perseus, we obtained $r_\gamma \sim 0.3$ deg which is somewhat extended compared to the telescope angular resolution. However, the fact that the NFW profile is very steep implies that the main DM emission comes from the core of the source that can be considered approximately point-like compared to our angular resolution.

To compute flux upper limits, we assume specific spectral indices that have been motivated by an astrophysical scenario in mind (see the following sections). This “scenario guided” approach allows us to provide the tightest limits on physically motivated parameters and underlying astrophysical models. In the next sections we will consider flux upper limits computed using a power-law γ-ray spectrum with spectral indexes $\Gamma$ of $-1.5$, $-2.2$ and $-2.5$. In Table 2, the corresponding integral flux upper limits for energies above 100 GeV are listed.

In Section 3.3 we will use an integral flux upper limit set above given energy thresholds in order to trace the energy range where we can better constrain the models. In Table 3 the obtained integral flux upper limits for $\Gamma = -2.2$ are shown. Note that we do not compute integral upper limits above 80 GeV (as we have not shown a cumulative $\alpha$-plot for energies above this value). This is because the $g/h$ separation for events below 100 GeV works in a substantially different way with respect to the higher energy events. Therefore, we analyze separately the events below 100 GeV and the events of higher energy, with different sets of analysis cuts.

### 3.3. Comparison to Previous Observations

There are few existing IACT observations of galaxy clusters (Perkins et al. 2006; Perkins 2008; Aharonian et al. 2009; Domainko et al. 2009; Galante et al. 2009; Kiuchi et al. 2009; Acciari et al. 2009). In section 4.3, we will compare the limits on the cosmic ray-to-thermal pressure obtained by other IACTs with those derived in this work. However, there are two observations of the Perseus galaxy cluster made by WHipple (Perkins et al. 2006) and VERITAS (Acciari et al. 2009) with which we can directly compare our upper limits.

The WHIPPLE collaboration observed the Perseus galaxy cluster (Perkins et al. 2006) for ~13 hours obtaining an integral upper limit above 400 GeV of $4.53 \times 10^{-12}$ cm$^{-2}$ s$^{-1}$ assuming a spectral index $\Gamma = -2.1$. We can compare this value with our integral upper limit above 400 GeV of $1.83 \times 10^{-12}$ cm$^{-2}$ s$^{-1}$ with $\Gamma = -2.2$ (see Table 3). Our upper limit is significantly lower than the WHIPPLE one; clearly, this is not a surprise as the MAGIC telescope belongs to a new generation of IACTs. More recently, the VERITAS collaboration observed Perseus (Acciari et al. 2009) for ~8 hours and obtained an integral upper limit above 126 GeV of...
Gravitational forces were computed using the parallel TreeSPH code GADGET-2 (Springel et al. 2001; and extended version of the distributed-memory parallel TreeSPH code GADGET-2 (Springel et al. 2001; Springel 2005). Gravitational forces were computed using a combination of particle-mesh and tree algorithms.

Hydrodynamic forces were computed with a variant of the smoothed particle hydrodynamics (SPH) algorithm that conserves energy and entropy where appropriate, i.e. outside of shocked regions (Springel & Hernquist 2002). We have performed high-resolution hydrodynamic simulations of a sample of galaxy clusters that span over one and a half decades in mass and show a variety of dynamical states ranging from relaxed cool core clusters to violent merging clusters. Our simulated clusters have originally been selected from a low-resolution dark-matter-only simulation (Yoshida et al. 2001). Using the ‘zoomed initial conditions’ technique (Katz & White 1993), the clusters have been re-simulated with higher mass and force resolution. In high-resolution regions, the DM particles had masses of \( m_{\text{dm}} = 1.61 \times 10^9 h_{70}^{-1} M_\odot \) and SPH particles \( m_{\text{gas}} = 2.4 \times 10^8 h_{70}^{-1} M_\odot \) so each individual cluster is resolved by \( 8 \times 10^4 \) to \( 4 \times 10^6 \) particles, depending on its final mass. The SPH densities were computed from 48 neighbours, allowing the SPH smoothing length to drop at most to half of the value of the gravitational softening length of the gas particles. This choice of the SPH smoothing length leads to our minimum gas resolution of approximately \( 1.1 \times 10^{10} h_{70}^{-1} M_\odot \). For the initial redshift we chose \( z_{\text{init}} = 60 \). The gravitational force softening was of a spline form (e.g. Hernquist & Katz 1989) with a Plummer equivalent softening length that is assumed to have a constant comoving scale down to \( z = 5 \), and a constant value of \( 7 h_{70}^{-1} \) kpc in physical units at later epochs.

These simulations included radiative hydrodynamics, star formation, supernova feedback and followed CR physics using a novel formulation that followed the most important injection and loss processes self-consistently while accounting for the CR pressure in the equations of motion (Pfrommer et al. 2006; Enßlin et al. 2007; Jubelgas et al. 2008). To obtain predictions of the GeV–TeV \( \gamma \)-ray emission from clusters, we used an updated version of the CR physics in our code. It is capable of following the spectral evolution of the CR distribution function by tracking multiple CR populations in each gaseous fluid element; each of these populations is described by an amplitude, a low-momentum cut-off, and a characteristic power-law distribution in particle momentum with a distinctive slope that is determined by the acceleration process at formation shocks or supernova remnants (Pinzke & Pfrommer, in prep.). Adiabatic CR transport processes such as compression and rarefaction, and a number of physical source and sink terms which modify the CR pressure of each particle are modeled. The most important sources considered are diffusive shock acceleration at cosmological structure

<table>
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<tr>
<th>( \Gamma )</th>
<th>[80-100]</th>
<th>[100-160]</th>
<th>[160-250]</th>
<th>[250-400]</th>
<th>[400-630]</th>
<th>[630-1000]</th>
<th>[1000-10000]</th>
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<td>12.6</td>
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<td>0.168</td>
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<tr>
<td>-2.2</td>
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<td>25.3</td>
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<td>4.57</td>
<td>0.903</td>
<td>0.176</td>
<td>0.018</td>
</tr>
</tbody>
</table>

Notes. Differential flux upper limits are listed in units of \( 10^{-11} \text{ cm}^{-2} \text{ s}^{-1} \text{ TeV}^{-1} \) for a power-law \( \gamma \)-ray spectrum with spectral index \( \Gamma \) in energy ranges in units of GeV.

1.27 \( \times 10^{-11} \) cm\(^{-2}\) s\(^{-1}\) assuming \( \Gamma = -2.5 \). We can compare this value with our corresponding integral upper limit above 100 GeV of \( 7.52 \times 10^{-12} \) cm\(^{-2}\) s\(^{-1}\) (see Table 2). Despite the fact that the VERITAS sensitivity of about 1% of Crab Nebula (Otte et al. 2003) is better than the MAGIC one, our upper limit is slightly lower than that found by Acciari et al. (2009) as expected from the significant difference in observation time.

4. COSMIC RAY INDUCED EMISSION

We use the upper limits on the integrated flux (Table 3) to put constraints on the CR-to-thermal pressure distribution and pursue three different approaches. (1) We perform high-resolution hydrodynamical simulations of cluster formation and evolution in a cosmological framework that include CR physics to predict the \( \gamma \)-ray emission and to obtain limits on the CR-to-thermal pressure. (2) Following Pfrommer & Enßlin (2004a), we use a simplified approach that assumes a constant CR-to-thermal energy density, a power-law spectrum in momentum, and compare the resulting CR-to-thermal pressure limits to those obtained by other IACT observations. (3) We use the observed luminosity of the radio-mini halo to place a lower limit on the expected \( \gamma \)-ray flux in the hadronic model of the radio mini-halo. This translates into a minimum CR pressure that is crucial for disentangling the emission mechanism in the radio and provides a clear prediction for the expected \( \gamma \)-ray flux.

Before doing so, we detail our cosmological simulations that we base our main analysis on. To this end we investigated the spatial and spectral properties of \( \gamma \)-ray emission in these simulations and refer the reader to the theory papers for further details (Pfrommer et al. 2008; Pfrommer 2008, Pinzke & Pfrommer, in prep.).

4.1. Cosmological Simulations

Simulations were performed using the “concordance” cosmological cold DM model with a cosmological constant (LCDM) motivated by First Year cosmological constraints of WMAP. The cosmological parameters of our model are: \( \Omega_m = \Omega_{dm} + \Omega_b = 0.3, \Omega_b = 0.039, \Omega_r = 0.07, h = 0.7, n = 1, \) and \( \sigma_8 = 0.9 \). Here, \( \Omega_m \) denotes the total matter density in units of the critical density for geometrical closure today, \( \rho_{\text{crit}}(z = 0) = 3H_0^2/(8\pi G) \). \( \Omega_b \) and \( \Omega_r \) denote the densities of baryons and the cosmological constant at the present day. The spectral index of the primordial power-spectrum is denoted by \( n_s \) and \( \sigma_8 \) is the rms linear mass fluctuation within a sphere of radius \( 8 h^{-1} \) Mpc extrapolated to \( z = 0 \).

Our simulations were carried out with an updated and extended version of the distributed-memory parallel TreeSPH code GADGET-2 (Springel et al. 2001; Springel 2005). Gravitational forces were computed using a combination of particle-mesh and tree algorithms.
formation shocks and optionally injection by supernovae while the primary sinks are thermalization by Coulomb interactions, and catastrophic losses by hadronic interactions. We note that the overall normalization of the CR distribution scales with the maximum acceleration efficiency at structure formation shock waves. Following recent observations at supernova remnants (Helder et al. 2009), as well as theoretical studies (Kang & Jones 2005), we adopt a realistic value of this parameter and assume that 50% of the dissipated energy at strong shocks is injected into CRs while this efficiency rapidly decreases for weaker shocks (Enßlin et al. 2007).

We computed the $\gamma$-ray emission signal and found that it obeys a universal spectrum and spatial distribution (Pinzke & Pfrommer, in prep.). This is inherited from the universal concave spectrum of CRs in galaxy clusters that is caused by the functional form and redshift dependence of the Mach number distribution of structure formation shocks that are responsible for the acceleration of CRs (Pfrommer et al. 2006). The CR distribution has a spectral index of $\Gamma \simeq -2.5$ at GeV energies and experiences a flattening towards higher energies resulting in $\Gamma \simeq -2.2$ at energies above a few TeV. Hence, the resulting $\gamma$-ray spectrum from CR induced pion-decay shows a characteristic spectral index of $\Gamma \simeq -2.2$ in the energy regime ranging from 100 GeV to TeV. The spatial distribution of the CR number density is mainly governed by adiabatic transport processes (Pfrommer et al. 2007) and similarly attains an approximate universal shape relative to that of the gas density. These findings allow us to reliably model the CR signal from nearby galaxy clusters using their true density profiles as obtained by X-ray measurements that we map onto our simulated density profiles.

In addition to CR protons, we modeled relativistic electrons that have been accelerated at cosmological structure formation shocks (primary CR electrons) and those that have been produced in hadronic interactions of CRs with ambient gas protons (secondary CR electrons). Both populations of CR electrons contribute to the $\gamma$-ray emission through Compton up-scattering photons from the cosmic microwave background as well as the cumulative star light from galaxies. It turns out that the pion-decay emission of the cluster dominates over the contribution from both inverse Compton components—in particular for relaxed systems (Pfrommer 2008).

In our optimistic CR model (radiative physics with galaxies), we calculated the cluster total $\gamma$-ray flux within a given solid angle. In contrast, we cut the emission from individual galaxies and compact galactic-sized objects in our more conservative model (radiative physics without galaxies). In short, the ICM is a multiphase medium consisting of a hot phase which attained its entropy through structure formation shock waves dissipating gravitational energy associated with hierarchical clustering into thermal energy. The dense, cold phase consists of the true interstellar medium (ISM) within galaxies and at the cluster center as well as the ram-pressure stripped ISM. These cold dense gas clumps dissociate incompletely in the ICM due to insufficient numerical resolution as well as so far incompletely understood physical properties of the cluster plasma. All of these phases contribute to the $\gamma$-ray emission from a cluster. To assess the bias associated with this issue, we performed our analysis with both limiting cases bracketing the realistic case.

In Figure 3, we compare the integral flux upper limits obtained in this work (see Table 3 with the simulated integrated spectra of the $\gamma$-ray emission from decaying neutral pions that result from hadronic CR interactions with the ambient gas in the Perseus cluster. Our conservative model without galaxies (solid) is contrasted to our model with galaxies (dashed). We scaled our conservative model with a factor of two so that it is just consistent with the upper limits obtained in this work (dotted). In our simulations, we assume an observationally motivated large value for the maximum CR energy injection efficiency at structure formation shocks and convert half of the dissipated energy to CRs at strong shocks. Smaller values would imply smaller $\gamma$-ray fluxes. Additionally shown are minimum $\gamma$-ray flux estimates for the hadronic model of the radio mini-halo of the Perseus cluster (dash-dotted with minimum flux arrows, see main text for details). Note that a non-detection of $\gamma$-rays at this level seriously challenges the hadronic model.

4.2. Constraints on the Cosmic Ray Pressure

In Figure 4, we show the simulated $\gamma$-ray surface brightness map of a cooling flow cluster of mass similar to Perseus. As the CR induced $\gamma$-ray flux is a radially declining function so is the CR pressure. A quantity that is of great theoretical interest is the CR pressure relative to the thermal pressure. $X_{CR} = P_{CR}/P_{th}$ as it directly assesses the CR bias of hydrostatic cluster masses since the CR pressure enters into the equation of motion. On the right-hand side of Figure 4, we show the profile of the CR-to-thermal pressure (volume-weighted) of this simulated cluster. Moving from the periphery towards the center, this quantity is a steadily declining function until we approach the cooling flow region around the cD galaxy of this cluster (similar to NGC 1275) where the CR pressure rises dramatically relative to that of the thermal gas which cools on a short time scale (Pfrommer et al. 2006). The volume average
is \( \langle X_{\text{CR}} \rangle = P_{\text{CR}}/P_{\text{th}} = 0.02 \), dominated by the region around the virial radius, while the ratio of CR-to-thermal energy is given by \( E_{\text{CR}}/E_{\text{th}} = 0.03^2 \). Perseus has a smaller mass and a corresponding temperature that is only half of that of our simulated cooling flow cluster. Noting that \( X_{\text{CR}} \propto 1/P_{\text{th}} \propto 1/kT \), we expect these values to be a factor of \( \approx 2 \) larger in Perseus, yielding \( \langle X_{\text{CR}} \rangle \approx 0.04 \) for the entire cluster and \( \langle X_{\text{CR}} \rangle \approx 0.02 \) for the core region that we probe with the present observation.

We have to scale our conservative model prediction by a factor of \( \approx 2 \) to reach the upper limits (cf. Figure 3) which implies that this work constrains the relative pressure contained in CRs to \( < 8\% \) for the entire cluster and to \( < 4\% \) for the cluster core region. The presence of dense gas clumps potentially biases the simulated \( \gamma \)-ray flux high and hence the inferred limits on \( X_{\text{CR}} \) low. Another source of bias could be unresolved point sources inside the cluster such as AGN. In the presented simulation of the cool core cluster g51, the bias due to subclumps amounts to a factor of 1.5 but it could be as high as 2.4 which is the mean difference between our conservative and optimistic model across our scaling relations. We note however that the latter case is already excluded by our upper limits provided the maximum shock acceleration efficiency is indeed as high as 50\%. While there are indications from supernova remnant observations of one rim region (Helder et al. 2009) as well as theoretical studies (Kang & Jones 2005) that support such high efficiencies, to date it is not clear whether these efficiencies apply in an average sense to strong collisionless shocks or whether they are realized for structure formation shocks at higher redshifts. Improving the sensitivity of the presented type of observations will help in answering these profound plasma astrophysics questions.

In Figure 4 we additionally compare a simulation where we only accelerate CRs at structure formation shocks with one where we additionally account for CRs that are injected through supernova feedback within the star forming regions in our simulation. Outside the cD galaxy, there is no significant difference visible which suggests that the CRs injected into the ICM by supernova driven winds are negligible compared with those accelerated by structure formation shocks. While this is partly an artifact of our simulations that neglect CR diffusion, we expect this behavior due to the adiabatic losses that CRs suffer as they expand from their compact galactic ISM into the dilute ICM. Assuming a conservative value for the density contrast of \( \Delta = 10^{-3} \), the CR pressure is diluted by \( P_{\text{CR}} \propto \Delta^{4/3} P_{\text{CR,ISM}} \propto 10^{-4} P_{\text{CR,ISM}} \).

4.3. Simplified Approach and Comparison to Previous Results

As anticipated in section 4.2, there are few existing IACT observations of galaxy clusters; some of which derived limits on the CR-to-thermal pressure contained in clusters, in particular the WHIPPLE observation of the Perseus cluster (Perkins et al. 2006) and the HESS observations of the Abell 85 (Aharonian et al. 2009b; Domainko et al. 2009) and Coma (Aharonian et al. 2009a) clusters. These work used simplifying assumptions about the spatial and spectral distribution of CRs. They typically assumed a single CR power-law distribution with a spectral index of \( \Gamma = -2.1 \) (that provides optimistic limits on the CR-to-thermal pressure) and assumed that the CR energy density is a constant fraction of the thermal energy density throughout the entire cluster. Based on these two assumptions, WHIPPLE and HESS found in Perseus and Abell 85 \( E_{\text{CR}}/E_{\text{th}} < 0.08 \), respectively, while HESS found \( E_{\text{CR}}/E_{\text{th}} < 0.2 \) in Coma.
To facilitate comparison with these earlier works, we repeated the data analysis with a spectral index \( \Gamma = -2.1 \) to obtain an integral upper limit \( F_{UL}(>100 \text{ GeV}) = 6.22 \times 10^{-12} \text{ cm}^{-2} \text{ s}^{-1} \). Following the formalism of Pf rommer & Enßlin (2008), we compute the \( \gamma \)-ray flux of a CR population with \( \Gamma = -2.1 \) within a circular region of radius \( r_{0.6} = 0.15 \text{ deg} \) or equivalently 200 kpc. In our isobaric model of CRs we assume that the CR pressure scales exactly as the thermal pressure \( \langle X_{\text{CR}} \rangle = \langle P_{\text{CR}} \rangle / \langle P_{\text{th}} \rangle = 0.033 \). This would be the most stringent upper limit on the CR energy in a galaxy clusters.

In our adiabatic model of CRs we account for the centrally enhanced CR number density due to adiabatic contraction during the formation of the cooling flow (Pf rommer & Enßlin 2004a). We assume that the CRp population scaled originally as the thermal population but was compressed adiabatically during the formation of the cooling flow without relaxing afterwards (we adopted temperature and density proles given by Churazov et al. 2003). In this model, we obtain an enhanced \( \gamma \)-ray flux level for virtually the same volume averaged CR pressure or vice versa for a given flux limit, hence we can put a tighter constraint on the averaged CR pressure. We constrain \( E_{\text{CR}} / E_{\text{th}} < 0.03 \) which corresponds to an averaged relative pressure of \( \langle X_{\text{CR}} \rangle = \langle P_{\text{CR}} \rangle / \langle P_{\text{th}} \rangle = 0.019 \).

How can we reconcile these tighter limits with our simulation based slightly weaker limit? We have to compare our simulated CR profile to a CR distribution that does not show any enhancement relative to the gas density. In the central region for \( r < 200 \text{ kpc} \), we derive an adiabatic compression factor of 1.7 that matches that in our simplified approach – suggesting that our simple adiabatic model captures the underlying physics quite realistically. Secondly, we have then to relate the pressure of a power-law spectrum with \( \Gamma = 2.1 \) to our simulated concave spectrum. Noting that the \( \gamma \)-rays at 100 GeV are produced by CR protons at \( \simeq 1 \text{ TeV} \), we normalize both spectra at 1 TeV and find that the simulated spectrum contains a larger pressure by a factor of 1.8. This factor brings the limit of our simplified adiabatic model into agreement with our simulation-based limit of the relative CR pressure \( \langle X_{\text{CR}} \rangle < 4 \% \) for the cluster core region. Finally, since \( \gamma \)-ray observations are only sensitive to the cluster core regions (the emission is expected to peak in the center due to the high target gas densities), they cannot constrain the average CR-to-thermal pressure within the entire cluster. Hence we have to use cosmological cluster simulations to address how much CR-to-thermal pressure could be additionally hidden in the peripheral cluster regions.

### 4.4. Minimum \( \gamma \)-ray Flux

For clusters that host radio (mini-)halos we are able to derive a minimum \( \gamma \)-ray flux in the hadronic model of CR interactions. The idea is based on the fact that a steady state distribution of CR electrons loses all its energy to synchrotron radiation for strong magnetic fields \( (B \gg B_{\text{CMB}} \simeq 3.2 \mu \text{G}) \) so that the ratio of \( \gamma \)-ray to synchrotron flux becomes independent of the spatial distribution of CRs and thermal gas (Pf rommer 2008). This can be easily seen by considering the pion decay induced \( \gamma \)-ray luminosity \( L_{\gamma} \) and the synchrotron luminosity \( L_{\nu} \) of a steady state distribution of CR electrons that has been generated by hadronic CR interactions,

\[
L_{\gamma} = A_{\gamma} \int dV n_{\text{CR}} n_{\text{gas}},
\]

\[
L_{\nu} = A_{\nu} \int dV n_{\text{CR}} n_{\text{gas}} \left( \frac{\alpha_{\nu} + 1}{2} \right) \frac{\gamma_{\nu}}{\epsilon_{\text{CMB}} + \gamma_B} \epsilon_B
\]

\[
\simeq A_{\nu} \int dV n_{\text{CR}} n_{\text{gas}} \quad \text{for} \quad \epsilon_B \gg \epsilon_{\text{CMB}}.
\]

Here \( A_{\gamma} \) and \( A_{\nu} \) are dimensionless constants that depend on the hadronic physics of the interaction (Pf rommer et al. 2008) and \( \alpha_{\nu} \simeq 1 \) is the observed synchrotron spectral index. Hence we can derive a minimum \( \gamma \)-ray flux in the hadronic model

\[
F_{\gamma, \text{min}} = A_{\gamma} \frac{L_{\nu}}{A_{\nu} 4\pi D_{\text{Lum}}^2},
\]

where \( L_{\nu} \) is the observed luminosity of the radio mini-halo and \( D_{\text{Lum}} \) denotes the luminosity distance to the respective cluster. Lowering the magnetic field would require an increase in the energy density of CR electrons to reproduce the observed synchrotron luminosity and thus increase the associated \( \gamma \)-ray flux.

Using the values of Table 1, we obtain a minimum \( \gamma \)-ray flux in the hadronic model of the radio mini-halo of \( F_{\gamma, \text{min}} (>100 \text{ GeV}) = 6 \times 10^{-11} \text{ cm}^{-2} \text{ s}^{-1} \), assuming a power-law CR distribution with \( \Gamma \simeq -2.3 \). This lower limit is independent of the spatial distribution of CRs and magnetic fields. We note that the spectral index is consistent with the radio data. It turns out that the requirement of strong magnetic fields violates the energy conditions in clusters as it implies a magnetic energy density that is larger than the thermal energy density – in particular at the peripheral cluster regions. The minimum \( \gamma \)-ray flux condition requires a constant (large) magnetic field strength throughout the cluster while the thermal energy density is decreasing by more than a factor of 100 from its central value. This would imply that the magnetic field eventually dominates the energy density at the virial regions – a behavior that is unstable as it is subject to Parker-like buoyancy instabilities. Additionally, such a configuration would be impossible to achieve in first place as the magnetic energy density typically saturates at a fixed fraction of the turbulent energy density which itself is only a small fraction of the thermal energy density in clusters (Schuecker et al. 2004). Hence these considerations call for lowering the assumed cluster magnetic fields which should strengthen the lower limits on the \( \gamma \)-ray flux considerably – however at the expense that these limits inherit a weak dependence on the spatial distribution of magnetic fields and CRs.

Estimates of magnetic fields from Faraday rotation measures (RM) have undergone a revision in the last few years with more recent estimates typically in the order of a few \( \mu \text{G} \) with slightly higher values up to 10 \( \mu \text{G} \) in cooling flow clusters (Clarke 2004; Enßlin & Vogt 2006). For

\footnote{The CR protons responsible for the GHz radio emitting electrons are \( \sim 100 \) times less energetic than those CR protons that are responsible for the TeV \( \gamma \)-ray emission. This is consistent with the concave curvature found in the CR spectrum by Pinzke & Pf rommer (in prep).}
the Perseus radio mini-halo. Faraday RM estimates are available only on very small scales (Taylor et al. 2008), i.e. few tens of pc. RM estimates are of the order of $\sim 7000 \text{ rad m}^{-2}$ leading to magnetic field values of $\sim 25 \mu G$ assuming the Faraday screen is localized in the ICM. This, however, appears to be unlikely as variations of $10\%$ in the RM are observed on pc-scales (Taylor et al. 2002), while ICM magnetic fields are expected to be ordered on significantly larger scales of a few kpc (Taylor et al. 2008; Vogt & Enßlin 2003; Enßlin & Vogt 2006). Application of the classical minimum-energy argument to the Perseus radio mini-halo data leads to estimates for the central magnetic field strength of $B_0 \approx 7 \mu G$ or even $B_0 \approx 9 \mu G$ for the more appropriate hadronic minimum-energy argument (Pfrommer & Enßlin 2001).

We select a cooling flow cluster of our sample that is morphologically similar to Perseus with a mass $M_{500} \approx 10^{15} \odot$ (the simulated cluster g51 of Pfrommer et al. 2008). We adopt a conservative choice for the central magnetic field strength of $\sim 10 \mu G$ and parametrize the magnetic energy density in terms of the thermal energy density by $\varepsilon_B \propto \varepsilon_{\text{th}}^{0.5}$ which ensures $\varepsilon_B < \varepsilon_{\text{th}}/3$ in the entire cluster. This allows us to strengthen the physically motivated lower limit to $F_{\gamma, \text{phys.min}} (>100 \text{ GeV}) = 8.5 \times 10^{-13} \text{ cm}^{-2} \text{ s}^{-1}$ as shown by the dash-dotted line in Figure 3. In the hadronic model, this minimum $\gamma$-ray flux implies a minimum CR pressure relative to the thermal pressure. Figure 3 shows that the minimum CR pressure $F_{\gamma, \text{phys.min}}$ is a factor of 3.6 lower than the simulated flux for Perseus in our conservative model. As seen in Sect. 2.2, this model corresponds to a relative CR pressure of $(X_{CR}) = (P_{CR})/(P_{th}) = 0.04$ where the averages represent volume averages across the entire cluster. Hence we obtain a minimum relative CR pressure, $(X_{CR,\text{min}}) = (P_{CR,\text{min}})/(P_{th}) = 0.01$. This minimum CR pressure corresponds to a minimum total CR energy of $E_{CR,\text{min}} = E_{CR,\text{min}}/E_{th} \times E_{th} = 1.6 \times E_{th}$ where we integrated the temperature and density profiles from X-ray observations (Churazov et al. 2003) to obtain the total thermal energy of $E_{th} = 5.7 \times 10^{63} \text{ erg}$. These considerations show the huge potential of combining future TeV $\gamma$-ray and radio observations in constraining physical models of the non-thermal cluster emission and to obtain important insights in the average distribution of cluster magnetic fields.

5. DARK MATTER ANNihilation

As discussed in Section 2.2, the expected DM annihilation flux is proportional to the product of a factor that encloses all the particle physics and a second factor that accounts for all the involved astrophysics. Therefore, in order to obtain an estimate of the annihilation flux, we need to choose a particular particle physics model (that was not needed in Section 2.2 since only a comparative study was done there) in addition to the modeling of the DM distribution. Although the uncertainties in the particle physics factor $f_s^{\text{SUSY}}$ are very large and spread over some orders of magnitude (see e.g. Albert et al. 2008), it is common to use the most optimistic value for a given energy threshold of the telescope. This factor just acts as a rescaling factor in the total flux, so we could change to other particle physics model simply by rescaling for its new value. Let us assume $f_s^{\text{SUSY}} = 10^{-32} \text{ GeV}^{-2} \text{ cm}^{-3} \text{ s}^{-1}$ above 100 GeV, which corresponds to one of the most optimistic allowed scenarios at the energies of interest here (Sánchez-Conde et al. 2007), with the neutralino as DM particle. Then, taking a value of $1.4 \times 10^{16} \text{ GeV}^2 \text{ cm}^{-5}$ for the integrated astrophysical factor inside $r_e$ (as given in Section 2.2), we obtain a maximum DM annihilation flux of $\sim 1.4 \times 10^{-16} \text{ cm}^{-2} \text{ s}^{-1}$ for energies above 100 GeV. The comparison with the derived upper limits from our observations are not very constraining. Assuming a generic DM annihilation spectrum without cutoff and spectral index $-1.5$ as a good approximation (e.g. Albert et al. 2008a; Aliu et al. 2009a), it can be seen from Table 2 that we need a boost in flux in the order of $10^4$ to reach the predicted DM annihilation flux values, since $F_{UL} (>100 \text{ GeV}) = 4.63 \times 10^{-12} \text{ cm}^{-2} \text{ s}^{-1}$.

This boost factor could come from different uncertainties that may enhance the annihilation $\gamma$-ray flux notably and that were not taken into account in the above calculation. One of them, the presence of substructures, could play a crucial role for Perseus, as explained in section 2.2. Although still uncertain, its effect could enhance the expected annihilation flux by more than a factor of 10 for Perseus-size halos according to Kuhlen et al. (2008). More recent work have shown that the expected boost factors could be as high as 200 (Springel et al. 2008a). However, with IACTs it is challenging to make use of these large boost factors as their contribution is expected to be more important on large angular scales comparable to the virial extend of the cluster. Detailed modeling of the substructures is needed in order to correctly evaluate their impact on the Perseus DM induced signal. Finally, also recently proposed mechanisms in the particle physics side, such as the Internal Bremsstrahlung (Bringmann et al. 2008) and the Sommerfeld effect (Lattanzi & Silk 2006; Pinzke et al. 2009), could enhance the DM annihilation flux by more than one order of magnitude for some particle physics models.

It is worth noting that the result obtained here for the boost factor needed in order to probe the predicted DM annihilation flux is comparable with previous observations of the Milky Way satellite galaxies (Albert et al. 2008a; Aliu et al. 2009a).

6. THE NGC 1275 EMISSION

The SED of the NGC 1275 core is shown in Figure 5. The radio and optical data represented with gray filled circles (Abdo et al. 2009) have been obtained with low resolution and thus include a large contribution from the large scale regions of the jet (radio) and from the host galaxy (optical). In the following, we model the data corresponding to the core emission. This is different to what was done by Abdo et al. (2009) who used the low resolution data in their models. We calculated our upper limit, shown in Figure 5 as a red arrow, assuming that the spectrum in the MAGIC energy band is a power law with spectral index $\Gamma = -2.5$, as indicated by the extrapolation of the last points of the Fermi-LAT spectrum. Note, however, that the level of the differential upper limits is only weakly dependent on the assumed spectral index (see Table 2).

The data clearly show a double peak SED. The radio-optical data suggest a peak of the emission in the IR band, similarly to the case of other $\gamma$-ray emitting ra-
Blazars are around 10 \(2009\). Such large values of the Doppler factor are rather large values of the Doppler factor: \(\delta \approx 258 L_{s,4.28} L_{C,4.34}^{-1/2} \nu_{s,13.5}^{-2} \nu_{C,23} R_{16}^{-1}\) (5)

where \(L_s = \nu_L L_\nu \), \(L_C = \nu_L L_\nu \), \(\nu_s \) and \(\nu_C \) are the synchrotron and SSC peak luminosities and frequencies and \(R \) is the size of the emitting region. Here \(Q = 10^Q \) \(Q_x \) in cgs units and we use the values derived for NGC 1275. In this estimate we assume the typical size of the emission regions derived in blazars, \(R = 10^{16} \) cm, though the Fermi-LAT data does not allow to constrain the radius of the emission region using the variability \(\delta \approx 50 \) – 100 (e.g. Begelman et al. 2008, Ghisellini & Tavecchio 2008). Arguments based on the observation of superluminal motions at VLBI scales (e.g. Celotti & Ghisellini 2008) and on the unification of blazars with radio galaxies also require values around 10 (e.g. Urry & Padovani 1995).

The most direct way to overcome the problem posed by the large Doppler factor is to assume two emission regions, as in the spine-layer model of Ghisellini et al. (2008). In this scenario the jet is assumed to be structured, with a fast inner region (the spine) surrounded by a slower sheet (the layer). Both components produce synchrotron and inverse Compton radiation and they are in radiative interplay: the synchrotron radiation from one component is seen boosted (by the relative velocity) by the other one and thus the IC emission of both regions is enhanced with respect to the standard SSC. In radio galaxies, in which the jet is observed at relatively large angles, the emission is expected to be dominated by the layer, which, due to the lower bulk Lorentz factor, has a larger emission cone. At smaller angle, instead, the emission is dominated by the spine, as in blazars.

We reproduce the SED with the spine-layer model. The orange line in Figure 5 shows the emission from the layer, while the spine produces the emission shown by the blue bottom line. The spine is assumed to be a cylinder of radius \(R = 1.5 \times 10^{16} \) cm, height \(H_s = 1.5 \times 10^{16} \) cm (as measured in the spine frame) and in motion with bulk Lorentz factor \(\Gamma_s = 15\). The layer is modeled as an hollow cylinder with internal radius \(R_r = 1.2 \times R \), height \(H_l = 4 \times 10^{16} \) cm (as measured in the frame of the layer) and bulk Lorentz factor \(\Gamma_l = 3\). Each region contains tangled magnetic field with intensity \(B_s = 2.5 \) G and \(B_l = 1 \) G and it is filled by relativistic electrons assumed to follow a (purely phenomenological) smoothed broken power-law distribution extending from \(\gamma_{\text{min}} \) to \(\gamma_{\text{max}} \) and with indices \(n_l \), \(n_s \) below and above the break at \(\gamma_b \). For the spine we use \(\gamma_{\text{min}} = 40 \), \(\gamma_b = 2 \times 10^4 \), \(\gamma_{\text{max}} = 10^5 \), \(n_1 = 2 \), \(n_2 = 3.5 \). For the layer \(\gamma_{\text{min}} = 10 \), \(\gamma_b = 4 \times 10^3 \), \(\gamma_{\text{max}} = 10^6 \), \(n_1 = 2.4 \), \(n_2 = 4.2 \). The normalization of these distributions is calculated assuming that the systems produce an assumed (bolometric) synchrotron luminosity \(L_{\text{syn, S}} = 10^{42} \) erg s\(^{-1}\) and \(L_{\text{syn, L}} = 2.7 \times 10^{41} \) erg s\(^{-1}\) (as measured in the local co-moving frame of the spine and layer, respectively), which is an input parameter of the model. As said above, the seed photons for the IC scattering are not only those produced locally in the spine (layer), but we also consider the photons produced in the layer (spine). We assume a viewing angle of \(\theta = 15\) deg. As discussed above, the same jet observed at smaller angle would be dominated by the emission from the spine and we expect that its SED resembles those of typical blazars. We show the SED of the jet when observed at angle of 4.5 degree (blue upper line in Figure 5). The SED is dominated by the emission of the spine. For comparison we report historical data for the well known blazar S5 0716+714 (data from Tavecchio & Ghisellini 2008 and references therein).

Note that, as observed, the model naturally predicts a very rapid decrease of the emission level above 10 GeV, due to the decreasing efficiency of the IC scattering in the Klein-Nishina regime. The position of this break is tightly constrained by the Fermi-LAT spectrum and MAGIC upper limit. In our model, this is critically dependent on the value of the frequency of the target photons for the IC scattering that in the spine-layer scenario.

![Graph](image-url)

**Fig. 5.** SED of the NGC 1275 core (lower two lines and data) and that of the well known blazar S5 0716+714 for comparison (upper line and data). Gray filled circles are data points in the radio and optical bands from Abdo et al. (2009). Filled black squares show, instead, the radio (VLBI, Taylor et al. 1999) and the optical emission (HST, Chiaberge et al. 1999) of the core alone. The soft X-ray bow tie is from Chandra (Balawender et al. 2008), while the red filled circles represent the Fermi-LAT spectrum taken from Abdo et al. (2009). The red arrow shows the MAGIC upper limit. In our model, this is critically de-
are mainly those coming from the spine (and scattered by the electrons in the layer). Therefore, the determination of the cut-off frequency between the Fermi-LAT and the MAGIC band allows us to infer the peak frequency of the synchrotron component of the spine. For instance, assuming that the peak of the spine is at IR frequencies or below (using for the layer the same parameters adopted above), we predict a flux in the MAGIC band above the measured upper limit. This argument allows us to fix the synchrotron peak of the spine at optical-UV frequencies. This, in turn, assures that the beamed counterpart of NGC 1275 is an intermediate BL Lac object, as the chosen S5 0716+714. In conclusion, the knowledge of the upper limit at the low energy end of the MAGIC band offers us the important possibility to have independent limits on the characteristics of the emission of the (otherwise invisible) spine and thus to constrain the kind of beamed counterpart of this radio galaxy. Future observations can confirm or rule-out our interpretation. In particular, the detection of photons above $\sim 100$ GeV would be challenging for the scenario depicted here, requiring major changes of the emission properties of the spine.

7. CONCLUSIONS

The Perseus cluster was observed by MAGIC during November and December 2008 resulting in 24.4 hours effective observation time of very high data quality. No significant excess of $\gamma$-ray was detected beyond the energy threshold of 80 GeV.

Using simplified assumptions (power-law CR spectra, constant ratio of CR-to-thermal energy density) that have been adopted in earlier work, we obtain a limit on the CR energy of $E_{\text{CR}}/E_{\text{th}} < 5\%$. This limit could be tightened furthermore by considering an adiabatically contracted CR population during the formation of the cooling flow yielding $E_{\text{CR}}/E_{\text{th}} < 3\%$. This would be the most stringent constraint on the CR energy using $\gamma$-ray observations to date. Using cosmological cluster simulations, it turns out, that these assumptions are not fulfilled for CR populations that have been accelerated by structure formation shocks: while the adiabatic model seems to match the simulated CR profiles towards the center very well, the expected ratio of CR-to-thermal pressure is increasing towards the peripheral cluster regions causing the volume averaged pressure across the entire cluster to increase by a factor of two. In addition the CR spectral distribution shows a concave curvature with a spectrum that flattens towards high energies with a spectral index of $\Gamma \simeq -2.2$ in the TeV regime. This implies that the CR pressure is enhanced by an additional factor of almost two. Using our simulated flux we obtained an upper limit on the CR-to-thermal pressure averaged across the entire cluster volume of $(X_{\text{CR}}) < 8\%$ and $< 4\%$ for the cluster core region. This corresponds to an upper limit on the CR energy of $E_{\text{CR}}/E_{\text{th}} < 13\%$ and $< 6.5\%$, respectively. We note that this is the first work where results from cosmological simulations and observational data analysis are combined. This demonstrates the need for cosmological simulations in order to more reliably predict CR spectra which provides a safeguard against too simplified and optimistic models which then lead to limits that are too tight.

The upper limits resulting from the data analysis are a factor of $\sim 2$ larger than our conservative model prediction for the CR induced $\gamma$-ray emission and hence in agreement with our cosmological cluster simulations. Future more sensitive measurements will be able to put interesting constraints on the maximum shock acceleration efficiency. Using minimum $\gamma$-ray flux arguments, we show that improving the sensitivity of this observation by a factor of about seven will enable us to finally critically test the hadronic model for the Perseus radio mini halo: a non-detection of $\gamma$-ray emission at this level implies cosmic rays fluxes that are too small to produce enough electrons through hadronic interactions with the ambient gas protons to explain the observed synchrotron emission.

As DM dominates the cluster mass, significant $\gamma$-ray emission resulting from its annihilation is also expected. With the assumed particle physics model, one of the most optimistic allowed scenarios (Sánchez-Conde et al. 2007) with the neutralino as DM particle, the boost factor for the typically expected DM annihilation induced emission is constrained to $< 10^4$. Note that for this estimation we neglected possible contributions from Internal Bremsstrahlung, Sommerfeld enhancement as well as enhancement factors due to substructures.

The upper limits obtained for the NGC 1275 emission are consistent with the recent detection by the Fermi-LAT satellite. In this case a one-zone SSC model for the entire emission is implausible, since the large separation in frequency between the two peaks would require extremely large values of the Doppler factor for the jet (Tavecchio & Ghisellini 2008). The most direct way to overcome this problem is to assume two emission regions, as in the spine-layer model (Ghisellini et al. 2003) which explains the radio galaxy emission.

While no galaxy cluster has been detected in $\gamma$-rays up to now, our estimations indicate that Perseus is among the most promising clusters to be detected by IACTs. Using the newly inaugurated MAGIC second telescope and operating the telescopes in stereo mode (Colin et al. 2009), a total observation time of about 150 hours may give us a chance to detect the CR induced $\gamma$-ray emission or to definitively probe the validity of the hadronic model of radio (mini-)halos. As the emission of NGC 1275 dominates the accessible energy range of the Fermi-LAT satellite, it could potentially hinder the satellite from detecting the CR as well as the DM induced $\gamma$-ray emission in this cluster. Similar problems might arise in other clusters. Therefore, the IACTs will play a crucial role in the quest for $\gamma$-ray emission from galaxy clusters.

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REFERENCES

—. 2009d, Science, 314, 1424
—. 2008b, Nuclear Instruments and Methods in Physics Research A, 588, 424
—. 2009d, Science, 314, 1424
—. 2008b, Nuclear Instruments and Methods in Physics Research A, 588, 424