THE JOURNAL OF

Perspective

# Roadmap for Molecular Benchmarks in Nonadiabatic Dynamics

Léon L. E. Cigrang, Basile F. E. Curchod, Rebecca A. Ingle, Aaron Kelly, Jonathan R. Mannouch, Davide Accomasso, Alexander Alijah, Mario Barbatti, Wiem Chebbi, Nadja Došlić, Elliot C. Eklund, Sebastian Fernandez-Alberti, Antonia Freibert, Leticia González, Giovanni Granucci, Federico J. Hernández, Javier Hernández-Rodríguez, Amber Jain, Jiří Janoš, Ivan Kassal, Adam Kirrander, Zhenggang Lan, Henrik R. Larsson, David Lauvergnat, Brieuc Le Dé, Yeha Lee, Neepa T. Maitra, Seung Kyu Min, Daniel Peláez, David Picconi, Zixing Qiu, Umberto Raucci, Patrick Robertson, Eduarda Sangiogo Gil, Marin Sapunar, Peter Schürger, Patrick Sinnott, Sergei Tretiak, Arkin Tikku, Patricia Vindel-Zandbergen, Graham A. Worth, Federica Agostini,\* Sandra Gómez,\* Lea M. Ibele,\* and Antonio Prlj\*



Downloaded via 188.252.185.37 on November 25, 2025 at 15:18:45 (UTC). See https://pubs.acs.org/sharingguidelines for options on how to legitimately share published articles.

Cite This: J. Phys. Chem. A 2025, 129, 7023-7050



**ACCESS** I

Metrics & More

ABSTRACT: Simulating the coupled electronic and nuclear response of a molecule to light excitation requires the application of nonadiabatic molecular dynamics. However, when faced with a specific photophysical or photochemical problem, selecting the

most suitable theoretical approach from the wide array of available techniques is not a trivial task. The challenge is further complicated by the lack of systematic method comparisons and rigorous testing on realistic molecular systems. This absence of comprehensive molecular benchmarks remains a major obstacle to advances within the field of nonadiabatic molecular dynamics. A CECAM workshop, Standardizing Nonadiabatic Dynamics: Towards Common Benchmarks, was held in May 2024 to address this issue. This Perspective highlights the key challenges identified during the workshop in defining molecular benchmarks for nonadiabatic dynamics. Specifically, this work outlines some preliminary

Community simulation assessment Discussion ecommendations 2025 quidelines

Article Recommendations

observations on essential components needed for simulations and proposes a roadmap aiming to establish, as an ultimate goal, a

## 1. INTRODUCTION

Modeling the dynamical behavior of a molecular system upon photoexcitation is a formidable theoretical and computational challenge. This is due to the involved coupled electron-nuclear dynamics, the so-called nonadiabatic effects, that necessitate treatment beyond the Born-Oppenheimer approximation. 1-As a result, the development of methods for simulating nonadiabatic molecular dynamics (NAMD) remains a key area of focus, 5-9 with research groups in theoretical chemistry and chemical physics having been particularly active in improving and testing simulation methods for several decades.

community-driven, standardized molecular benchmark set.

The field of NAMD has benefited from advances in experimental techniques capable of imaging the coupled electron-nuclear dynamics of molecules upon light absorption. The development of ultrashort laser pulses and subsequent experiments in femtochemistry 10 revealed direct measurements of dynamical processes in molecules, 11-15 which have helped validating and guiding advances in NAMD methodologies.

However, the field of NAMD has also been fueled by significant progress in the development of efficient algorithms and software 16-31 able to solve the coupled dynamics of electrons and nuclei. Thanks to all of these developments, strong collaborations between experiments and theory, for example in the context of gas-phase time-resolved spectroscopy, have emerged for studying the excited-state dynamics of many systems, and have sparked community efforts aiming to challenge the predictive power of various NAMD methods.<sup>32</sup> Despite these significant steps toward unraveling the ultrafast photodynamics of numerous molecular systems, the field of

Received: March 31, 2025 Revised: June 30, 2025 Accepted: July 3, 2025 Published: July 15, 2025





NAMD still faces considerable challenges, as the following sections will discuss. At the same time, the reliability and trustworthiness of theoretical predictions often remain difficult to assess.

As a result, the community of developers and users of NAMD has recently pointed out the critical need for established and standardized benchmarks to advance the field. By benchmark here, we mean well-chosen systems that can be used to compare and test computational methods, along with a community-accepted robust procedure to be followed whenever newly developed methods and approximations in NAMD are tested. Benchmarks in NAMD are needed to improve methodologies, ensure reproducibility, estimate the reliability of the predictions, and enable theoretical developments to keep pace with experimental techniques. Further, we believe that benchmarking existing methodologies and codes will ultimately assist users and newcomers to NAMD in identifying the most suitable technique for addressing specific problems.

Benchmarking has long been a cornerstone of computational chemistry, for instance of electronic structure theory, <sup>33–36</sup> and computational sciences in general. <sup>37,38</sup> While such efforts serve as inspiring examples, NAMD presents unique challenges due to its inherent complexity. The outcome of an NAMD simulation relies on the calculation of observables with intricate time and energy dependencies, which are often associated with a wide range of physical and chemical phenomena. The high dimensionality of realistic molecular systems makes it impossible to simulate their quantum dynamics exactly. As a result, using approximations to the time-dependent molecular Schrödinger equation is necessary, which has driven the development of numerous NAMD methods over the past 40 years.

A CECAM workshop,<sup>39</sup> entitled *Standardizing Nonadiabatic Dynamics: Towards Common Benchmarks*, took place in Paris in May 2024 with the central goal of stimulating the NAMD community toward developing a common benchmark set by (i) agreeing on the main ingredients required to test all families of NAMD techniques, of which we will provide examples in Section 2, and (ii) selecting potential molecular systems for further tests. This Perspective summarizes the main conclusions reached during the CECAM workshop, aiming to inform the broader scientific community and encourage future benchmark efforts. More specifically, this Perspective serves as an opportunity to elaborate on key questions that emerged from the workshop regarding what makes a proper benchmark in NAMD.

Discussions made it clear that, given the complexity of NAMD simulations, initial attempts to propose realistic molecular benchmarks should begin with simple systems, namely small or medium-sized molecules in the gas phase. Even with such a limited focus, numerous open questions still arose during the discussions in the workshop.

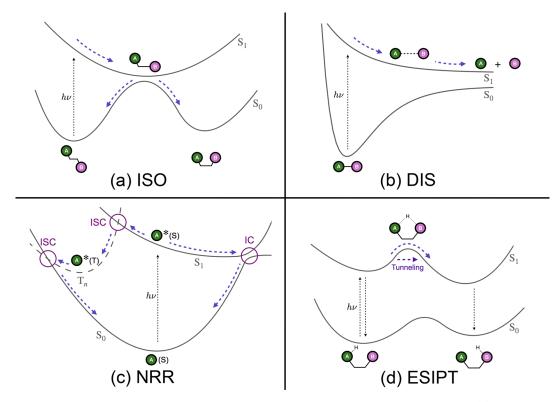
- What constitutes an adequate reference for a benchmark in NAMD? An experiment or an accurate simulation?
- How do we decide which observables should be prioritized when establishing the reliability of a given method?
- How can NAMD methods based on fundamentally different theoretical frameworks be compared, such as those based on wave functions and those based on trajectories?

- How can different electronic-state representations and the intricacies of electronic-structure methods be handled?
- How can we even ensure that different NAMD techniques are initialized in the same way for a given benchmark system?
- How can we ensure that statistical convergence of computational results is achieved?

In addition to offering a structure for this Perspective article, the questions above highlight key topics that require dedicated attention to ensure the definition of proper and generalized benchmark systems in nonadiabatic dynamics. Accordingly, Section 2.1 proposes some prototypical phenomena and related families of molecular systems that were considered appropriate for benchmarking. Section 2.2 is dedicated to the different families of NAMD methods, aiming to identify the most representative theoretical approaches that can be used for a systematic comparison. Section 2.3 provides a brief overview of the issues related to various electronic-structure methods for obtaining electronic energies and other electronic properties. In Section 2.4, we discuss the problem of the initial conditions for NAMD and how to ensure an equivalent initialization of the dynamics across different theoretical methodologies. Section 2.5 identifies suitable physical observables and properties that can be directly calculated in an NAMD simulation and used in the context of benchmarking. In Section 2.6, we examine the role of experimental measurements and their suitability as a reference for NAMD. Finally, Section 3 summarizes the key insights that emerged from the CECAM workshop and outlines practical strategies for the community to advance the initiative of establishing robust benchmark systems for NAMD. We discuss how members of the community with diverse expertise can organize, share data, and collaborate effectively while also briefly exploring the future prospects for benchmarking. In this sense, this Perspective acts as a roadmap for future developments in NAMD.

# 2. TOWARD MOLECULAR BENCHMARKS: GENERAL CONSIDERATIONS

So far, mostly low-dimensional models of nonadiabatic processes have served as benchmark sets for NAMD, 40while many software packages try to incorporate such models in their benchmarking capabilities. <sup>19,47,48</sup> These models have often been engineered to challenge specific aspects of the NAMD formalism and offer the great advantage that they typically have numerically exact results to compare with. The famous Tully models, proposed in 1990 to evaluate the accuracy of the trajectory surface hopping method, 40 are still nowadays widely used by the NAMD community. This set of three onedimensional model systems was specifically designed to investigate prototypical nonadiabatic processes, including single and multiple nonadiabatic crossings. However, the overarching goal of NAMD methods is to describe the photodynamics of a molecule in its full dimensionality. Thus, benchmarking NAMD on realistic photochemical processes is necessary to provide justification for their suitability in the simulations of the molecular systems of interest. In addition, while some approximations are thoroughly tested and understood for lowdimensional problems, their performance in higher dimensions is not necessarily known. In this respect, multidimensional model potentials are also important for benchmarking, and are often used by the community especially to compare fully quantized and mixed quantum-classical approaches. 42,49-51



**Figure 1.** Schematic representation of the four phenomena of interest for the benchmarking of NAMD methods: (a) photoisomerization, i.e., an isomerization induced by photoexcitation; (b) photodissociation, i.e., bond-breaking activated by absorption of light; (c) nonreactive radiationless relaxation, i.e., transition between electronic states initiated by photoabsorption, potentially involving different spin multiplicities, without resulting in different photoproducts; and (d) excited-state intramolecular proton transfer, occurring upon photoexcitation, typically involving hydrogen-bonded donor and acceptor groups. The curves labeled with S and T represent singlet and triplet potential energy curves, respectively, and the asterisk indicates an excited state of a species. The blue dashed arrows show nuclear motion along a molecular coordinate.

Constructing multidimensional potential energy surfaces (PESs) can rapidly become a very difficult task. The situation becomes even more complex for large molecular systems (hundreds of atoms) involving dozens of coupled excited states, where energies, gradients, and nonadiabatic couplings must all be considered. In these cases, strategies to reduce computational costs, such as dynamically limiting the number of excited states or nonadiabatic couplings to be calculated, become indispensable. <sup>52</sup>

The challenge of constructing multidimensional PESs is often circumvented by performing excited-state dynamics based on on-the-fly electronic structure calculations. Therefore, the concept of benchmarks needs to be adapted to on-the-fly NAMD, as was recently done with the "molecular Tully models", composed of ethylene, 4-N,N'-dimethylaminobenzonitrile (DMABN), and fulvene.<sup>53</sup> This benchmark set has been adopted by the community, and already several NAMD methods have been tested on one or more of these systems. 54–61 While useful, the molecular Tully models have shortcomings, such as the limited set of properties that have been used for comparisons, the fact that initial conditions were oriented toward trajectory-based methods, and the fact that only commercial software has been used for the underlying electronic structure, preventing broader accessibility and reproducibility. Even leaving the electronic-structure problem aside, it is evident that developing generalized and reliable benchmark sets for NAMD comes as a stringent challenge and currently hampers further developments in the field.

2.1. Selected Photophysical and Photochemical Phenomena for Benchmarking. This Section describes

photophysical and photochemical processes that could be used to assess the performance of different NAMD methods. In the following, we propose to select a few specific light-triggered phenomena, with the aim of achieving two main goals: narrowing down the choice of current benchmark systems, and providing some clear points of comparison between the results of different NAMD calculations (see also Section 2.5). The chosen phenomena should cover diverse aspects of photodynamics, highlighting the role of both nuclear and electronic effects. They should be generally well understood to avoid controversies related to the interpretation of the results. Additionally, we choose to privilege unimolecular processes in order to avoid unnecessary complexities in the early stage of building a benchmark strategy. With these elements in mind, the following four types of processes, which are briefly described below and illustrated in Figure 1, were preselected as interesting test systems.

- Photoisomerization (ISO): ABC +  $h\nu \rightarrow CAB$
- Photodissociation (DIS): AB +  $h\nu \rightarrow A + B$
- Nonreactive radiationless relaxation (NRR):  ${}^{1}A + h\nu \rightarrow {}^{1}A^{*}[\rightarrow {}^{3}A^{*}] \rightarrow {}^{1}A$
- Excited-state intramolecular proton transfer (ESIPT): AH···B + h\nu → A···HB.

We note, however, that this list of phenomena is by no means exhaustive and future benchmark efforts will extend this selection to include, for instance, systems with high densities of electronic states, initialized in a coherent superposition of states, systems undergoing photoinduced electron transfer, or excited-state energy transfer or charge migration, or complex dynamical processes such as molecular collisions.

The above phenomena are some of the most common photoinduced processes in molecules (see textbooks on molecular photophysics and/or photochemistry<sup>2,62-65</sup>) and are representative of many of the current applications of NAMD methods. A search through the Semantic Scholar Academic Graph<sup>66</sup> indeed reveals that, when using the keywords "nonadiabatic dynamics", at least 50% of research articles on molecular systems published in the last 10 years discuss one of the four phenomena outlined above. Each of these phenomena presents a different challenge from a theoretical perspective: complex interplay between electronic character and nuclear motion (DIS), potential involvement of tunneling effects (ESIPT), molecular rearrangement (ISO), or complex transfer of electronic population (NRR). In the following, we discuss a few selected examples (i.e., not an exhaustive list) that demonstrate the importance of such light-induced processes.

One of the most paradigmatic examples of ISO is the cis  $\rightarrow$ trans isomerization of retinal induced by photon absorption in mammalian eyes. 67,68 Azobenzenes, stilbenes, and spiropyrans are also prominent classes of compounds subject to photoisomerization. 69-71 As shown in Figure 1a, photoisomerization<sup>72</sup> begins with light absorption, which weakens an originally locked bond (for example, by promoting an electron from a  $\pi$  to a  $\pi^*$  molecular orbital in a  $\pi$  bond). This weakening of the originally locked bond allows the molecule to rearrange easily, often by rotation around a (pseudo)single bond. In many photoisomerization processes, such as those involving retinal, azobenzene, and stilbene, the first excited state possesses a minimum located very close to the  $S_0/S_1$  conical intersection (see Figure 1a). This minimum often corresponds to a geometry where the isomerization dihedral angle is close to 90-110°. Upon reaching this region of configuration space, the molecule can either proceed with a full photoisomerization or return to the original isomer, typically through a nonradiative decay involving a conical intersection and additional nuclear motion.

In the field of femtochemistry, DIS was one of the first studied processes,  $^{10,73}$  and is schematically represented in Figure 1b. In the series of pioneering experiments by Zewail, the study of the photodissociation of iodocyanide (ICN)<sup>74</sup> preceded that of sodium iodide (NaI),  $^{75}$  which was already studied in the earliest experiments of Polanyi. Wavepacket dynamics simulations have supported these experiments from the beginning  $^{43,77-81}$  and NaI, as well as similar alkalihalides, has been extensively used as a simple one-dimensional test case for quantum dynamics methods since.  $^{82-84}$  Absorption of UV light by small organic molecules such as, for example, methanol, phenol or pyrrole readily leads to chemical bond breaking via dissociative excited states ( $S_1$  in Figure 1b).  $^{85-87}$ 

NRR involves the complex nonradiative electronic population decay that can be observed between states of the same spin multiplicity (internal conversions) or between states with different spin multiplicity (intersystem crossings), see Figure 1c. Beyond common single crossings between excited states within the singlet manifold, see typical examples of complex internal conversions that do not involve large amplitude nuclear motions are decays induced by repeated crossings of regions of strong nonadiabaticity or reflections, three-state conical intersections or extended degeneracies between electronic states. Intersystem crossings are driven by spin—orbit coupling, and are, thus, most often associated with transition metal complexes.

organic molecules, <sup>93–97</sup> particularly in carbonyl compounds, when sulfur- or selenium-substituted, <sup>98–101</sup> and in nitroaromatic compounds. <sup>102,103</sup> It should be noted that since spin—orbit coupling is generally relatively weak, the time scale necessary for observing significant intersystem crossing can range from few hundreds of femtoseconds to hundreds of nanoseconds. <sup>104</sup> In addition, the performance of simulations of intersystem crossing may depend on the strength of spin—orbit coupling, especially since it is also now established, experimentally and theoretically, that intersystem crossing can compete on similar time-scales as internal conversion, at least in geometrically unconstrained molecules with high density of states and overlapping spin manifolds. <sup>105–107</sup> Although several NAMD approaches have been formulated to describe intersystem crossing, <sup>108</sup> simulations over long time scales still remain challenging.

ESIPT reactions may occur in complex biological systems and are exploited for the development of sensors and sunscreens, among others. <sup>109–112</sup> For the purpose of our benchmark, ESIPT processes taking place on ultrafast time scales are of particular interest as they are generally simpler to simulate with most NAMD methods. 113 Molecules exhibiting ESIPT typically contain donor and acceptor units linked by an intramolecular hydrogen bond, allowing the proton to easily migrate upon photoexcitation, as in molecules like 2-(2-hydroxyphenyl)benzoxazole (HBO) and hydroxybenzo[h]quinolone (HBQ). 114,115 The mechanism of this migration can occur via two distinct pathways, illustrated in Figure 1d. The small barrier is overcome thermally, after which the proton undergoes a "ballistic" type motion between the donor and the acceptor; alternatively, tunneling through the potential barrier is also possible. The proper description of tunneling, which is a classically forbidden process, requires the inclusion of nuclear quantum effects for the treatment of at least some nuclear degrees of freedom (e.g., involving protons). This can be done by either adopting a purely quantum description 116-118 or extending the phase space by employing coupled trajectories as, for example, in the ring polymer formalism. 119,120 Tunneling, however, constitutes a challenge for NAMD methods relying solely on independent classical-like trajectories.

In summary, the phenomena highlighted in this section, i.e., ISO, DIS, NRR and ESIPT, are representative of a large variety of processes found in photophysical and photochemical applications. Simulating the underlying photodynamics requires that NAMD methods are able to capture challenging features, as mentioned above. Therefore, determining the capability of NAMD methods to describe accurately these highlighted phenomena will provide valuable insights into their strengths. Since NAMD methods are inherently approximate and, as expected, may perform well for certain systems but less so for others, the representative phenomena discussed here are not meant to be used as criteria for direct rejection of methods that do not match the reference results. Instead, benchmarking against these phenomena is intended to help users select appropriate methods or identify areas for improvement, depending on the specific problem being addressed.

**2.2.** Computational Methods for NAMD. Many different NAMD methodologies have been developed over the years, <sup>121</sup> and in the interest of treating a comprehensive set of molecular benchmarks, the techniques developed and applied within the NAMD community should be broadly represented. Here, we briefly summarize some of these approaches related to molecular dynamics and (photo)chemical reactions, with a schematic overview being given in Figure 2. The NAMD approaches

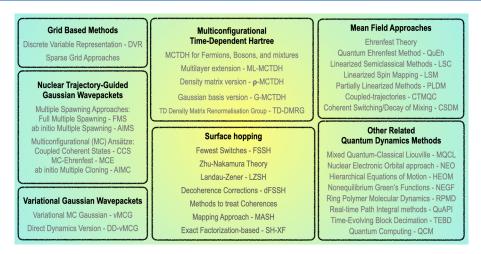


Figure 2. Selected techniques from the range of NAMD methods that are relevant to establishing molecular benchmarks.

presented below are organized mainly based on the underlying assumptions, and for the sake of conciseness, we only provide some general information on the methods and on the key references. Note, however, that we cannot provide details on all the effects that these assumptions have on the outcome of a simulation, as this is, indeed, the ultimate goal of benchmarking.

Early efforts in the field can perhaps be traced back to the development of real-space grid-based solvers for the timedependent Schrödinger equation, such as the discrete variable representation (DVR) approach, 122,123 or sparse-grid approaches.<sup>24,124</sup> Going beyond the DVR picture while maintaining the concept of a fixed underlying basis, the multiconfigurational time-dependent Hartree (MCTDH) family of methods 125,126 comprises a powerful range of exact numerical wave function solvers, including the original and multilayer (ML-MCTDH) formulations, <sup>127,128</sup> which are available for fermions, bosons, and mixtures of the two. 129 There are also approaches within this framework to treat density operators ( $\rho$ -MCTDH). 130-133 While fundamentally different at first sight, the time-dependent density matrix renormalization group (TD-DMRG)<sup>134,135</sup> and tree tensor network state (TTNS) extensions thereof actually are another way to solve the ML-MCTDH equations of motions. 136,137

A challenge for applying these approaches to high-dimensional systems is that the global electronic PESs and related couplings as well as local operators are required to be in a separable form, either sum-of-products (for MCTDH) or a tree, multilayer representation (for ML-MCTDH), as a prerequisite. Alternatively, additional time-dependent sparse-grid approximations can be used together with MCTDH methods. Furthermore, the surfaces and couplings should preferentially be in a diabatic representation to avoid numerical issues arising from singularities at conical intersections in the adiabatic representation.

Relaxing the constraint of having a fixed basis has led to dynamical wavepacket methods such as full multiple spawning (FMS)<sup>142</sup> and ab initio multiple spawning approaches (AIMS),<sup>7,143</sup> as well as the recent variants of AIMS that have been developed to include external fields,<sup>144</sup> spin—orbit coupling,<sup>145</sup> and to optimize the computational efficiency.<sup>146,147</sup> In this family of methods, nuclear trajectory-basis functions represented by frozen Gaussians evolve classically on adiabatic PESs. In addition, there is the closely related range of techniques stemming from multiconfigurational ansätze, such as the

coupled-coherent states approach (CCS),<sup>148</sup> the multiconfigurational Ehrenfest method (MCE),<sup>149</sup> and the ab initio multiple-cloning algorithm (AIMC),<sup>150</sup> that in general use different PESs than the adiabatic ones to evolve the trajectory-basis functions

Using a fully variational framework with Gaussian wave-packets leads to the variational Gaussian-based approaches, namely the variational multiconfigurational Gaussian (vMCG) formulation and Gaussian-based MCTDH (G-MCTDH). More recently, direct-dynamics extensions of vMCG (DD-vMCG) have been developed enabling implementations with on-the-fly electronic structures, forgoing the need to precompute a global PES.

While the above trajectory-guided methods have been developed to directly tackle the time-dependent molecular Schrödinger equation, quantum-classical methods simplify the coupled electron—nuclear quantum problem by decomposing it into a quantum electronic system coupled to a classical-like nuclear system. Quantum-classical approaches can capture some of the quantum aspects of nuclear dynamics by using an ensemble of trajectories to represent the nuclear density, and they are extremely appealing due to their tractable computational cost.

Surface-hopping methods, in their original formulation  $^{40,155,156}$  and further developments  $^{157-164}$  have become an important class of algorithms for simulating mixed quantumclassical dynamics. Of these, the fewest switches surface hopping (FSSH) approach of Tully 40 is perhaps the most popular choice in current practice. Alternative hopping formalisms have been introduced and gained popularity to circumvent the direct calculation of nonadiabatic or overlap couplings, such as Landau-Zener surface hopping (LZSH) or Zhu-Nakamura theory. 157,165-167 Decoherence corrections (dFSSH), which are intended to cure the overcoherence problem with FSSH and ensure consistent numerical propagation of classical and quantum populations by enforcing population alignment during decoherence events, 168,169 have been developed from numerous different approaches, 170–175 as well as alternative hopping algorithms. 165,176-179 While surface-hopping methods are a popular choice in applications, there remain many open questions in terms of conceptual grounds 169 and formulation of an optimal algorithm, particularly, pertaining to how velocity rescaling and frustrated hop protocols are implemented, 180,181 or concerning the treatment of trivial crossings. 182,183 As such, a

range of alternative surface-hopping approaches have also been developed, including approximate methods based on the exact factorization of the full molecular wave function, <sup>184</sup>,185 which can involve coupled <sup>177</sup>,186–188 or auxiliary <sup>189–192</sup> trajectories (SH-XF). Other FSSH-based variants that offer improved accuracy have also been developed. <sup>175</sup>,179,192–196 For example, while the standard implementations of surface-hopping methods conserve the energy of each classical nuclear trajectory in the ensemble, it has been pointed out that energy should be conserved over the trajectory ensemble as a whole, as quantum-trajectory surface-hopping methods do, <sup>195</sup>,196 which eliminates the need for velocity rescaling and special treatments for forbidden hops. Surface hopping has also been generalized beyond internal conversion <sup>160</sup>,197,198 and beyond the usual quantum-electron/classical-nuclei partitions. <sup>199</sup> Recently, using the semiclassical mapping formalism, a mapping approach to surface hopping (MASH) has also been introduced. <sup>200</sup>–202

Mean-field type approaches are another major category of trajectory-based dynamics methods. While Ehrenfest dynamics<sup>203</sup> belongs to the family of quantum-classical methods and is perhaps the most well-known method of this type, a number of notable improvements have been developed. Quantum-Ehrenfest (Qu-Eh) combines the idea of evolution on an average potential with quantum dynamics and has been related to a particular formulation of vMCG.<sup>204</sup> The ab initio multiple cloning (AIMC) has been proposed as an alternative to address the coherence issues inherent in Ehrenfest trajectories, naturally incorporating decoherence through cloning events. 150,205 A valuable improvement of semiclassical Ehrenfest was the inclusion of coherence and decoherence effects in the coherent switching decay of mixing (CSDM) method.<sup>206–208</sup> One important branch of these developments stems from the semiclassical initial value representation. <sup>209–213</sup> More recently, fully linearized, <sup>214–218</sup> and partially linearized approaches based on the mapping formalism (linearized spin mapping, LSM) have been put forward, <sup>221</sup> which have also proven to offer improved accuracy over the Ehrenfest limit. More generally, it is worth noting that mapping Hamiltonian approaches, such as the Meyer-Miller model, provide an effective framework for investigating nonadiabatic dynamics by transforming discrete quantum states into continuous physical variables. 221-228 In this way, electronic and nuclear degrees of freedom can be treated on an equal footing in the phase space. 229-231 The exact factorization of the full molecular wave function can also be used as a starting point to derive coupled-trajectory mixed quantum-classical (CTMQC) dynamics, <sup>232–235</sup> such that decoherence effects naturally emerge as correction terms to the mean-field Ehrenfest equations. Additional variants of meanfield Ehrenfest have been developed to include external fields and simulate transient absorption spectroscopy. 236,237

The mixed quantum-classical Liouville (MQCL) equation represents another class of NAMD methods, which adopts the density matrix formalism and rigorously introduces the classical limit starting from the quantum-mechanical Liouville-von Neumann equation. MQCL is exact in various conditions, for instance in the case of linear coupling between the quantum and the classical subsystems, and has been shown accurate for proton transfer and proton-coupled electron transfer reactions. It is important to mention here that by introducing approximations in MQCL, as shown in ref 162, the surface-hopping scheme can be derived, hence, putting such a phenomenological approach on a firmer ground. The MQCL has also been used to derive mean-field<sup>242</sup> and improved mean-

field algorithms using full<sup>231,243</sup> and partial linearization techniques,<sup>244,245</sup> introducing the groups of linearized semiclassical methods (LSC) and partially linearized methods (PLDM). A closely related range of techniques have been developed using a path integral formulation,<sup>246</sup> which also permits full<sup>247</sup> and partial linearization<sup>248</sup> approximations.

Still in the density matrix representation, a further range of numerically exact approaches have been developed to solve the electron—nuclear problem. Real-time path integral methods such as the quasi-adiabatic path integral (QuAPI) methods, <sup>249,250</sup> and recent extensions such as the quantum-classical path integral approach and the small matrix path integral approach, use the Feynman path integral method to propagate quantum degrees of freedom. Nonequilibrium Green's functions (NEGF), <sup>253–255</sup> often applied to mesoscopic systems and transport problems, can also be of interest to study proton tunneling reactions. Ring polymer molecular dynamics (RPMD) methods, that extend the imaginary-time path-integral formalism to the real-time domain, have been originally developed for ground-state calculations to account for nuclear quantum effects, <sup>257</sup> but have been also generalized in various flavours to treat nonadiabatic problems.

Other related quantum dynamics methods, which employ either a density-matrix or a wave function formalism, are also worth mentioning here, such as nuclear-electronic orbital (NEO) methods, \$^{118,262,263}\$ the hierarchical equations of motion (HEOM) method, \$^{264,265}\$ TTNS approximations \$^{266,267}\$ and tensor-network-based time-evolving block-decimation techniques (TEBD), among others.

A careful comparison between quantum dynamics and trajectory-based NAMD should address the potential for zero-point energy (ZPE) leakage in the latter, especially in long-time-scale processes such as intersystem crossings. Recently developed Hessian-free ZPE correction methods provide a promising solution to improve the consistency of simulations across these approaches. <sup>270,271</sup>

Recent, provably efficient quantum-computer (QC) algorithms for NAMD simulations present additional opportunities for benchmarking. QC NAMD algorithms use the exponentially large Hilbert space of the QC to represent the Hilbert space of the nuclei and electrons of molecules. This representation allows them to prepare states, simulate dynamics, and measure observables using time and memory polynomial in system size. QC algorithms have been developed for both analog quantum simulators and fully programmable digital quantum computers. Most of the analog approaches are simulations of vibronic-coupling models, <sup>272–275</sup> and have been implemented on quantum hardware to simulate dynamics around conical intersections, <sup>273</sup> charge transfer, <sup>274</sup> and photoinduced dynamics in molecules such as pyrazine. <sup>275</sup> Digital algorithms require large-scale, fault-tolerant quantum computers, but they could simulate the time-dependent Schrödinger equation of all nuclei and electrons on a grid exactly, up to a known and controllable error. 276-280 Other digital algorithms for near-term QCs use variational principles, but lack provable error bounds. 281,282 QC approaches both require new benchmarks to allow fair comparisons with heuristic classical methods and deliver new tools for error-analysis which will allow developers of classicalcomputer algorithms to more accurately bound the errors of their simulations.

Figure 2 provides an overview of the classes of methods presented in this section. However, NAMD is a rapidly evolving field, with a wide variety of methods being constantly developed

and improved, thus, it is challenging to provide an exhaustive list of all the methodologies and variations that have been introduced. Our goal is to offer an overview of the most common and widely used approaches. We also recognize that some methods on the list have primarily been used with low-dimensional model systems so far, but in principle, they could be adapted for realistic molecular systems. Figure 2 also gives an additional categorization of the methods by organizing them in "categories" highlighted by the boxes.

2.3. Electronic Structure and Representation of Potential Energy Surfaces. The ingredient of an NAMD simulation that arguably plays a critical role on its outcome is the underlying electronic structure method, i.e., the level of theory at which the electronic energies, gradients, and couplings between electronic states are calculated - as highlighted in numerous studies. 106,283-287 The impact of the electronic structure on the result of NAMD remains, however, challenging to predict. While very different PESs calculated from two different electronicstructure methods often lead to different excited-state dynamics, <sup>288</sup> examples in the literature show that this correlation does not always hold: vastly different PESs can lead to similar dynamics, and similar PESs can lead to different results in NAMD. 286,289-291 In any case, it is critical to ensure that the electronic-structure quantities for any benchmark system are obtained consistently to fairly compare the outcome of the NAMD simulations.

For the current standard practice of benchmarking on low-dimensional analytical models, ensuring consistency in electronic structure between different NAMD methods is a minor issue. A model Hamiltonian usually provides analytical expressions for energies and (diabatic) couplings, and perhaps even for gradients and for nonadiabatic couplings, making it simpler to ensure that different NAMD simulations are performed using the same electronic information. <sup>292</sup>

In more realistic scenarios, NAMD is often carried out with electronic structure calculated on the fly (also called direct-dynamics) using trajectory-basis functions or quantum-classical techniques. This terminology means that any electronic-structure quantity for the dynamics is calculated locally, i.e., at the current nuclear configuration at that time step, rather than being precomputed or predefined over the full configuration space. In these cases, resolving the electronic structure problem becomes a critical step before establishing benchmark systems. To meaningfully compare different NAMD methodologies and software, it is essential to define the level of electronic-structure theory, ensuring that the underlying electronic-structure quantities remain consistent for all NAMD methods being compared.

An ideal electronic structure method should fulfill several criteria: (1) provide electronic energies, nuclear gradients, and any required couplings (e.g., nonadiabatic couplings, spin—orbit couplings, transition dipole moments), (2) describe all electronic states involved in the dynamics with equal accuracy across the entire configuration space encountered during the dynamics, (3) be numerically robust, (4) capture the potential multiconfigurational character of electronic wave functions, and finally, (5) be computationally affordable. 7,293

Multiconfigurational methods<sup>294</sup> like multiconfigurational self-consistent field (MCSCF), (state-averaged) complete active space self-consistent field (CASSCF), or complete active space configuration interaction (CASCI) are computationally expensive but include static correlation, often providing a qualitative correct picture of the PES. These methods allow

the user to select the active space orbitals (occupied and unoccupied) that dominate the excited-state characters of the molecule of interest.<sup>295</sup> Making an informed choice of active space, that is, making it as compact as possible while still remaining sufficiently stable throughout the dynamics, can offer a good compromise between cost and accuracy. However, in many cases a CASSCF or CASCI approach may not be accurate enough, due to the lack of dynamical correlation. This can be incorporated through the application of perturbation theory (e.g., via multistate or single-state CASPT2)<sup>296</sup> or with multireference methods (e.g., MRCIS or MRCISD).<sup>294</sup> Such methods bring an improved description of the PESs, in particular when excited electronic states of different characters interact, but also increase substantially the cost of the calculation. 296 Alternatively, scaled CASSCF methods (e.g.,  $\alpha$ -CASSCF, <sup>297,298</sup>) introduce empirical corrections to stateaveraged CASSCF, improving the description of PESs while maintaining computational efficiency, and have been successfully applied to study photochemical ring-opening and isomerization reactions. 298-300 If structural rearrangements during the dynamics drive the molecule to regions of the PESs far from the Franck-Condon region, a single computationally affordable active space might not provide enough flexibility to describe the photoproducts with the same accuracy as the initial molecule often leading to instabilities in the electronic structure. As a computationally efficient alternative, floating occupation molecular orbital complete active space configuration interaction (FOMO-CASCI)<sup>301</sup> was also employed in combination with NAMD.<sup>302</sup>

For large molecular systems, linear-response (LR) timedependent (TD) density functional theory (DFT) is a practical alternative due to its excellent balance between cost and accuracy. However, LR-TDDFT often suffers from limitations due to its approximations necessary for practical applications. 303 One of them is its reliance on the *adiabatic approximation*, which hinders describing conical intersections with the electronic ground state, electronic states with double-excitation character, and charge-transfer transitions and Rydberg transitions; rangeseparated hybrids may help with these last two problems. 304-314 These shortcomings may hamper the applicability of LR-TDDFT in NAMD simulations for systems exhibiting such features. In general, for any application to a molecular system, the choice of an adequate density functional may be challenging and requires careful benchmarking. 315-317 Spin-flip variants of these methods exist, 318,319 which can address some of these issues but often introduce spin contamination, except for spin-adapted spin-flip methods.  $^{320-323}$  Some of the aforementioned limitations of LR-TDDFT can be overcome using the ensemble-DFT-based approach which combines multireference methods within a density functional theory framework.<sup>324</sup> In a related approach, the mixed-reference spin-flip TDDFT (MRSF-TDDFT) technique<sup>325</sup> has been proposed recently. At variance with LR-TDDFT, MRSF-TDDFT was shown to predict the correct topology of conical intersections with the ground state and to describe excited states with significant double excitation character. 326,327 Hole-hole Tamm-Dancoff approximated (hh-TDA) density functional theory 228 constitutes another variant of LR-TDDFT adequately describing conical intersections and combined with NAMD. 329 Relatedly, particleparticle RPA can describe double excitations well, <sup>330</sup> and, along with their oscillator strengths, related to their couplings, so can dressed frequency-dependent TDDFT.331,332

We note that, in addition to conventional LR-TDDFT, real-time TDDFT (RT-TDDFT)<sup>303</sup> has also been used. In RT-TDDFT the electron density is propagated by integrating the time-dependent Kohn—Sham equations. RT-TDDFT (or more broadly, real-time electronic structure methods)<sup>333</sup> can be naturally coupled with Ehrenfest dynamics<sup>334</sup> to propagate nuclei classically with forces derived from a weighted average of all electronic states. However, in this approach there is no need for the explicit determination of individual electronic states and their couplings.

The algebraic diagrammatic correction to second order, ADC(2), is a wave function-based single-reference method that has been exploited for NAMD. 335,336 This method, in its original implementation, possesses some limitations — it cannot describe conical intersections with the ground electronic state 283 and suffers from a systematic flaw for carbonyl-containing molecules. However, its overall accuracy and efficiency in describing excited PESs and their coupling regions, 312 as well as its reliability, makes it a key contender for the NAMD of medium-sized molecular systems. ADC methods are closely related to coupled cluster (CC) methods, 338 which were historically not a popular choice for NAMD due to their intrinsic instabilities. 336,339 However, recent CC implementations managed to resolve some of these problems, and have opened the door for CC-based NAMD simulations. 340,341

Semiempirical multireference methods based on multiconfigurational configuration interaction wave functions built from FOMO-CI, <sup>22,178,342,343</sup> particularly those reparameterized based on high level calculations, or the multireference configuration interaction based on the orthogonalization-corrected model Hamiltonian (MRCI/OMx), <sup>22,344</sup> may offer an affordable alternative for describing conical intersections and complex electronic densities. If reparameterization has already been performed for the molecule of interest, these methods can be a suitable choice for benchmarking. They offer electronic structure quantities at a low cost, enabling long propagation times and large numbers of trajectories to be evolved. <sup>186,286,345–348</sup>

The use of a given electronic-structure method to benchmark on-the-fly NAMD techniques is challenging, even if all the input parameters (and initial orbitals) are provided. Ideally, the same quantum-chemical code should be used to ensure a one-to-one comparison, as minor implementation details, such as convergence criteria or algorithmic differences, can impact the final results. To promote accessibility and broader participation of community members, benchmarks should preferably employ freely available or open-source quantum-chemical codes that are widely used within the NAMD community (e.g., Open-Molcas, 349 Bagel, 350 Orca, 351 NWChem, 352 GAMESS, 353 MNDO, 354 MOPAC-PI<sup>21</sup> or PySCF<sup>355</sup>). For many quantumchemical methods, ensuring consistency between two calculations is relatively straightforward if one uses the same version of a given quantum-chemical code and the same input parameters. The case is harder for multireference and multiconfigurational methods, for which it is crucial to ensure that the very same initial molecular orbitals are included in the active space. This can be achieved by making sure that the starting orbitals are provided as a wave function file.

Grid-based methods for quantum dynamics require integrals to be performed over the entire nuclear configuration space. Onthe-fly dynamics is hard to perform for such methods (even though recent forays in this direction have been made 356,357), therefore they often rely on precomputed electronic structure

quantities to fit or build analytical models. A very common approach for obtaining high-dimensional model potentials is to parametrize the PESs with vibronic coupling (VC) models, where the simplest form is the linear VC (LVC). 358 An LVC model proposes to build a harmonic expansion of the diabatic states around the Franck-Condon region, using information from electronic-structure calculations, along with the linear coupling among these diabatic states. While VC models can accurately capture the ultrafast decay in NAMD, in their simplest LVC form, they are limited by their underlying harmonic approximation for describing the PESs and can only be applied to relatively rigid systems. Despite these shortcomings and when used on suitable systems, the LVC approach has recently gained popularity as a cost-efficient mean for comparing different trajectory-based approaches with accurate quantum dynamics results in high-dimensional systems. 51,54,55,92,181,359,360 Here it is worth noting that recent advances in artificial intelligence and machine learning have significantly enhanced the accessibility of high-dimensional and anharmonic analytical potentials, reducing the computational cost of electronic structure and improving the fitting procedures, <sup>361</sup> thus pushing NAMD simulations to longer time scales. <sup>362–364</sup> In this context, benchmarking efforts will become even more critical in the future, particularly as machine learning based interatomic potentials (MLPs) evolve into widely adopted tools for NAMD. Well-defined benchmarks will be crucial not only for testing traditional electronic structure methods but also for providing a structured framework to assess how well MLPs reproduce reference electronic structure results within the same NAMD framework. Moreover, stable and reliable MLPs have the potential to revolutionize how NAMD methods are evaluated by enabling rapid and extensive testing, and facilitating the efficient exploration of the parameter space in existing NAMD techniques.

Finally, the use of fitted, analytical potentials versus on-the-fly dynamics for benchmarking needs to be addressed further. There is a clear and obvious advantage in developing models based on analytical potentials, as they directly allow quantum dynamics simulations to be performed and (near) numerically exact solutions to be used as a reference. However, most common applications of NAMD focus on molecules for which a parametrization in full dimensionality is often inaccessible and that are therefore more easily described by on-the-fly simulations. Hence, NAMD benchmarks should be best conducted based on both approaches: fitted/analytical potentials and on-the-fly dynamics. One should stress that in general, a NAMD simulation carried out on precomputed, fitted potentials in reduced dimensionality cannot be compared with NAMD conducted with direct dynamics in full dimensionality (see for instance a quantum dynamics study on a 2D model of retinal, 42 followed by fully dimensional direct dynamics 365 and experimental evidence<sup>366</sup> demonstrating the necessity of additional degrees of freedom). This is because the configuration space that can be explored is predefined in a precomputed model, constraining the dynamics to a certain region of the nuclear configuration space. It might be useful, however, to conduct simulations on model potentials using onthe-fly NAMD simulation methodologies to provide a strict comparison of their performance against accurate grid-based

A plausible solution to such an issue is to fit directly a global PES into analytical separable (sum of products or tree) form. In this way, it could be used by the whole range of NAMD techniques. From a purely algorithmic perspective, one can distinguish two classes of such fitting procedures: (i) those based on machine learning (ML) or neural networks (NN) and (ii) those relying on a functional ansatz related to tensor decomposition algorithms.

The first category includes methods based on machine learning or neural networks, such as single-layered Neural Networks with specific activation functions<sup>367</sup> and Gaussian Process Regression with separable multidimensional kernels.<sup>368</sup> The second category involves methods exploiting PES smoothness under separable form constraints, including Smolyak interpolation scheme with nondirect product basis<sup>369</sup> and the Finite Basis Representation (FBR) family of PES representations.<sup>370–372</sup> FBR models can be optimized from scattered reference data and have been applied to various physico/chemical processes, including vibrational problems (6D/9D),<sup>370,371</sup> reactive scattering processes (13D/15D/72D),<sup>371,373</sup> and nonadiabatic dynamical problems (12D).

**2.4.** Initial Conditions for the Dynamics. Any NAMD simulation requires a definition of the initial state of the molecule before being excited by light or before the dynamics is started. Therefore, a critical aspect to discuss is the nature of this initial molecular state for the molecule of interest, be that the ground state of the molecule or the state directly generated by the photoexcitation process.<sup>374</sup>

Following the time-dependent perturbation theory to first order for a system with two electronic states,  $^4$  one can show that the first-order contribution to the molecular state immediately after excitation by an infinitely short pulse (a  $\delta$ -pulse) is simply the initial ground-state nuclear wave function (multiplied by the transition dipole moment between the ground and the excited electronic state). In other words, if the molecule is excited by a very short pulse, a commonly accepted approximation is to simply project the ground-state nuclear wave function onto the desired excited electronic state. This approximation, often referred to as the sudden, or vertical, excitation, dramatically simplifies the preparation of initial conditions for NAMD, as it neglects the time duration of the excitation process (e.g., an experimental laser pulse) and the precise nature of the molecular state formed upon photoexcitation.

Within this sudden excitation, the initialization of a quantum dynamics simulation only requires the nuclear wave function associated with the ground electronic state for the system of interest, often taken as the ground vibrational state for all modes considered. This nuclear wave function can be obtained by imaginary-time propagation or, for potential energy surfaces invoking a harmonic approximation, simply from a Gaussian nuclear wave function. Similarly, the most commonly employed strategy for trajectory-based methods consists first of sampling an approximate ground-state distribution. The harmonic Wigner distribution, constructed from the molecular equilibrium geometry and its harmonic normal modes, is often used to sample representative initial conditions (nuclear momenta and positions). 6,374 Once the initial ground-state nuclear wave function (quantum dynamics methods) or ground-state nuclear momenta + positions (trajectory-based methods) are acquired, they can be projected onto the desired excited electronic state to begin the NAMD.

While the protocol described above is the most commonly employed strategy to initialize a NAMD simulation, it relies on a series of approximations, <sup>376</sup> namely that (i) the molecule is in its electronic and vibrational ground state before photoexcitation and (ii) that the laser pulse employed is infinitely short (or at

least short enough for its bandwidth to overlap with all necessary vibrational states in the excited electronic state for a projection of the ground-state nuclear wave function), meaning that a perfect nuclear wavepacket is generated in the excited electronic state(s) of interest. We note that the initialization of quantum dynamics simulations also often relies on the Condon approximation, that is, the transition dipole moment does not depend significantly on the nuclear geometries under the initial wavepacket. Nevertheless, care must be taken since cases of strong violation of Condon approximation have been reported.<sup>377</sup>

For floppy molecules with multiple dihedral angles and low rotational barriers, harmonic Wigner distributions are not suitable for sampling initial conditions. Improvements in the generation of the ground-state probability density can be obtained for trajectory-based methods by using ab initio molecular dynamics (AIMD). Initial positions and momenta can be obtained from long, equilibrated ground-state molecular dynamics simulations, providing a more accurate representation of the nuclear phase space. Incorporating ZPE in the dynamics requires the use of a quantum thermostat (QT), 378-380 as a regular 300 K AIMD would lead to molecular distributions that are too narrow in comparison to their ZPE equivalent.<sup>381</sup> QT-AIMD can overcome some limitations of the harmonic Wigner sampling, in particular for flexible molecules with low-frequency (anharmonic) vibrational modes. Using the harmonic Wigner sampling for molecules with photoactive low-energy modes can lead to severe artifacts in the ensuing excited-state dynamics an issue fixed with the QT-AIMD.<sup>38</sup>

Moving beyond the sudden excitation requires a more careful inclusion of the external electric field in the simulation, aiming for more robust comparisons with experiments. Most methods for NAMD have been extended to incorporate photoexcitation triggered by an explicit laser pulse (e.g., refs 31,160,236,237,383-385). This strategy, though, does appear to stretch the approximations of methods like surface hopping for longer laser pulses, 144,386,387 and modifications of surface hopping based on Floquet theory were presented in the literature. 388,389 Different works have discussed photoexcitation beyond laser pulses, including incoherent sunlight 375,390,391 or a periodic drive, <sup>392</sup> in NAMD. Building the effect of a laser pulse within the initial conditions was also suggested. 84,393,394 Furthermore, upon initial photoexcitation by a laser pulse, a group of electronic states may be excited and the subsequent dynamics can differ depending on whether the system evolves from a superposition of states (pure) or a mixed ensemble.<sup>395</sup>

Another issue that needs to be addressed in the context of benchmarking different families of methods for NAMD is the representation of the electronic states. In conventional trajectory-based methods, the nuclear dynamics is usually performed by invoking electronic properties in the adiabatic representation. On the other hand, quantum dynamics methods often rely on the - more convenient - diabatic representation to avoid encountering singularities of the nonadiabatic couplings at conical intersections. Therefore, in the initialization of a quantum dynamics simulation, the ground-state nuclear wave function needs to be projected onto a given diabatic electronic state. For a proper assessment of trajectory-based methods against quantum dynamics results, the initial electronic diabatic state needs to be translated appropriately into an adiabatic state or a linear combination of adiabatic states when the trajectorybased simulation is performed with methods employing the adiabatic representation.

**2.5. Observables and Properties.** Benchmarking NAMD methods faces the challenge of identifying a unique, clearly defined, and quantifiable "result". In contrast, electronic structure benchmarks are based on well-defined numerical values such as electronic energies, or optimized geometries. The outcome of a NAMD simulation involves a time-dependent molecular wave function, with the desired results and properties depending on the specific system and phenomenon under study. Nevertheless, we aim to identify key properties and observables that can facilitate both qualitative and quantitative comparisons across different methods for NAMD.

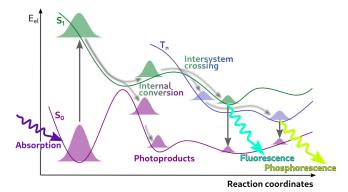
In this section, we use the term observable in the physical sense, namely a quantity that is directly determinable from an experiment and is, therefore, independent of the theoretical representation used in the calculations as it corresponds to the expectation value of an operator. It is worth mentioning here that, as it will become clear from the discussions of the next sections, in this preliminary stage of our work on NAMD benchmarks, we are not considering using experimental signals as a reference for evaluating the performance of the simulation methods. However, it is indeed likely that we will calculate experimental observables, and, in order to provide fair and unbiased grounds for comparisons, we will adopt - as far as it is possible, given the different nature of various NAMD techniques - the same methodologies to extract the experimental observables from the available simulated data. By contrast, we refer to a property as a quantity that may be used to interpret the simulated dynamics or an experimental measurement, but that cannot be directly measured. Below, we discuss how observables and properties can be selected for benchmarks.

For the purpose of benchmarking, observables and properties need to be selected such that different methods can be compared fairly, following several criteria. First, it is desirable that the considered observables or properties can be computed by every NAMD method under investigation. For instance, the operators involved in the calculation of expectation values should ideally have a relatively simple form to allow for the computation of high-dimensional integrals required for the quantum dynamics approaches. Similarly, it should be possible to calculate the observables directly as expectation values by reconstructing the nuclear wave functions. For trajectory-based methods, the observables and the properties are often calculated as trajectory averages.

Second, it is also necessary to choose a set of observables and properties that describe all aspects of the dynamical processes at play. For NAMD, this normally requires the consideration of both electronic and nuclear degrees of freedom. Different methods are unlikely to reproduce each type of observable or property equally well, so having the most diverse observable set is important for a comprehensive comparison between methods.

Finally, NAMD methods employ different electronic representations. Some electronic properties, such as electronic populations may only be accessible in or dependent on a given representation and shall be used "with care" for comparisons of methods. One way to avoid this issue is to consider representation-independent electronic properties and observables, such as optical spectra.

To make a tangible example of the observables and properties that can be of interest for understanding the processes taking place during a photochemical reaction, let us discuss Figure 3. The *absorption* of light by an organic molecule in its vibrational and electronic ground state,  $S_0$  (violet Gaussian on the left) produces a photoexcited nuclear wavepacket in a singlet excited



**Figure 3.** Processes that can occur upon photoexcitation of a molecular system.

electronic state, here  $S_1$  (green Gaussian on the left). The photoexcited molecule relaxes nonradiatively via *internal conversion* from  $S_1$  to  $S_0$ , transferring the population to the electronic ground state and accessing the configurations of the various *photoproducts* (violet Gaussians in the center). The remaining contribution to the nuclear wavepacket in  $S_1$  can be transferred nonradiatively to a triplet state (blue Gaussians in the center), here  $T_n$ , by *intersystem crossing*. Finally, the  $S_1$  and the  $T_n$  wavepackets can ultimately relax radiatively to the ground state (violet Gaussians on the right) via *fluorescence* and *phosphorescence*.

Based on this schematic representation of a photochemical reaction, the following properties could provide a useful way of tracking the important aspects of the dynamics. The relaxation of the photoexcited system to a lower energy electronic state can be followed via the electronic (adiabatic and diabatic) populations. While easily accessible, electronic populations are a representation-dependent quantity and therefore, excited state lifetimes in different spin multiplicities should additionally be linked to an observable that is sensitive to them. Calculating the time-dependence of the energy gap distribution between two appropriate electronic PESs would additionally quantify the motion of the nuclear wavepacket away from the conical intersection seams toward a stable minimum energy geometry on the lower-energy surface and give a quantitative picture of the electronic relaxation, in particular for NRR. For molecular systems consisting of donor and acceptor moieties, transient exciton localization can be tracked, enabling the study of intramolecular energy transfer between different chromophoric units. 396,397 Finally, an important aspect of photochemical processes is the formation of photoproducts. This is particularly important for characterizing ISO, DIS, and ESIPT phenomena, and can be probed via the associated quantum yields, preferably computed for different excitation wavelengths. For ESIPTrelated processes, it would be particularly interesting to study the mechanistic details of the proton transfer, i.e., whether it is stepwise or concerted. This can be deduced from the timeevolved nuclear probability distribution of the transferring proton or the kinetic isotope effect, <sup>398</sup> for example.

To properly compare with experiments, it is essential to consider various spectroscopic observables that can be used to interrogate photochemical and photophysical phenomena. Optical transient absorption, 405–408 time-resolved X-ray absorption, 409 2D electronic spectroscopy 404,410 and time-resolved photoelectron spectroscopy 411,412 are several complementary techniques that directly probe the dynamical changes in electronic structure associated with a particular

process. All of these techniques can, in principle, distinguish between states of different spin multiplicity, 413-415 and the method of choice may depend on whether the associated valence or core excitation spectra or the photoionization cross sections provide the greatest contrast between the molecular species and states of interest. In particular, 2D electronic spectroscopy is an ultrafast optical technique capable of providing critical insights into coherence, which signifies the simultaneous evolution of electronic and vibrational dynamics in complex natural and synthetic systems 416 Coherence refers to the in-phase evolution of specific degrees of freedom and, in quantum mechanics, is formally described by the off-diagonal elements of the density matrix, encompassing both electronic and vibrational components. Capturing such coherent phenomena in NAMD simulations 117,418 remains a significant challenge due to the need for consistent and accurate propagation of both electronic and nuclear degrees of freedom at the surface crossings.

One advantage offered by time-resolved photoelectron spectroscopy is that processes like electronic population transfer involving an optically dark electronic state can be directly observed. 411 Recently, attosecond transient absorption spectroscopy 419 and multiphoton ionization 420 have been used to measure and distinguish adiabatic and nonadiabatic effects in the evolution of electronic coherences. Finally, time-resolved X-ray diffraction 421-423 and ultrafast electron diffraction 424,425 spectroscopies provide a useful way of directly probing the nuclear rearrangements of molecules in real-time and can be highlighted as effective experimental tools for investigating ISO, DIS and ESIPT phenomena. In particular, ultrafast electron diffraction has shown sufficient sensitivity to monitor the motion of light atoms like hydrogen in the context of photodissociation. 426 In general, scattering experiments are beginning to be employed to detect information beyond structural dynamics, such as electronic populations 427 or indeed the rearrangement of electrons during a reaction. 428,429 This indicates that such experiments stand to provide comprehensive and complete information about the evolution of the molecular wavepacket.

2.6. The Role of Experiments in Benchmarking Nonadiabatic Molecular Dynamics. Experimental observables are often regarded as the "ultimate" data for providing a reference for results obtained from quantum chemical methods. Spectroscopic techniques seem especially well-suited for providing this due to their ability to reveal quantum state information on the target system. However, there are a number of challenges when drawing comparisons between experiment and theory that need to be considered, particularly when benchmarking NAMD simulations.

Ultrafast spectroscopies are reasonably young in comparison to their static counterparts, with the earliest time-resolved optical absorption measurements being performed in the 1970s. Anny ultrafast techniques, such as time-resolved X-ray absorption, are even newer, Mich poses a number of further challenges for using this experimental data as a reference in the benchmark of NAMD. The first of these is simply the quantity of experimental data available. While ultrafast optical techniques have seen significant hardware developments, such that "all-in-one" laser and spectrometer systems are now commercially available, ultrafast optical techniques are nevertheless nowhere near as ubiquitous as standard UV—vis absorption, which is now even being performed with smartphones.

A more serious issue for benchmarking is the reproducibility and reliability of the experimental data, coupled with the quality of the data reporting. Although chemists and physicists are generally among the least concerned about a "reproducibility crisis" in science, 437 there have been recent reviews highlighting how, for X-ray photoelectron spectroscopy (XPS), there is a nontrivial number of papers reporting experimental data with minor errors in the collection process and a much more significant number with major issues associated with the subsequent peak fitting and data analysis procedures. 438 Growing concerns about the reproducibility problem in XPS have prompted journals 439 and the community 440,441 to produce documents on best practices for data collection, reporting, and analysis in order to try and ensure consistent standards are maintained.

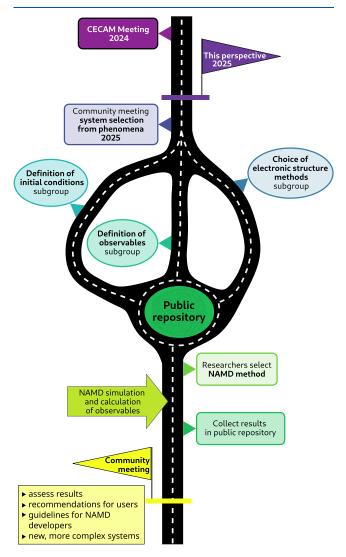
No such systematic analysis exists for the ultrafast literature, and many techniques are still sufficiently novel and challenging to perform. Hence, the research focus is still far from prioritizing systematic characterization studies. Even a brief survey of the literature, though, will reveal many inconsistencies and inadequacies in what experimental parameters are reported. For example, many papers do not report how time-zero (where the pump and probe pulses are temporally overlapping) is established or whether any wavelength calibrations for detectors have been performed and how. Often, only representative pulse parameters for the pump and probe pulses, such as pulse energies, temporal duration and central wavelengths, are reported, and no spectral information provided. While not all measurements are particularly sensitive to the excitation conditions, without this information, it becomes difficult to simulate the exact experimental conditions in excited-state dynamics simulations, particularly when an explicit pulse is included. While there are often reasons for not reporting all of this information, it is clear that it would be highly beneficial to specifically design experiments for use in theoretical benchmarking studies, where a different approach to data collection is required than for a standard photophysical experiment.<sup>442</sup>

It is also very important to make a clear distinction between what is the true experimental signal of measurement and what are parameters extracted from a fitting or modeling of the experimental data. For example, ultrafast spectroscopies are used to extract "lifetime" information, but the reported lifetimes are normally extracted from some kind of kinetic model with an inherent number of assumptions, 443 although there are a few notable exceptions. 444,445 As explored more extensively in a recent review, 401 the same change in an experimental observable can arise from different physical mechanisms, and it is important to note that most spectroscopies are not directly sensitive to the population dynamics, but rather to the population dynamics convoluted with a transition probability. Evaluating the trustworthiness of models and fits can be as challenging as assessing the quality of experimental data and a difficult task without direct engagement with experts.

# 3. OUTLOOK – A ROADMAP FOR MOLECULAR BENCHMARKS IN NAMD

The multifaceted nature of NAMD has, to date, hindered systematic efforts toward designing molecular benchmarks, with only a few notable studies making headway. The intention behind this Perspective is to narrow down the multitude of available choices of "benchmarkable phenomena" and encourage collaborative efforts within the NAMD community toward these goals. This Section summarizes key considerations

for developing molecular benchmarks and presents an executive outline for their implementation. The steps discussed in this Perspective form the *roadmap* toward a community-driven development of benchmarks for NAMD methods (Figure 4).



**Figure 4.** Schematic representation of the steps discussed in this *roadmap* toward the creation of a benchmark set for NAMD methods and the future steps planned by the community.

First, we briefly overview key insights from the workshop in Paris,<sup>39</sup> which established foundational ideas for this initiative. One challenge identified by the community of NAMD users and developers is the breadth and complexity of NAMD simulations, demanding careful selection criteria to balance feasibility with scientific relevance. To ensure meaningful assessments, molecular benchmarks are meant to capture realistic nonadiabatic phenomena while minimizing reliance on model potentials with reduced dimensionality. The emphasis on realistic processes – those measurable in experiments – reflects the goal of creating benchmarks that will increase confidence in the predictive power of current theoretical developments. We have identified four relevant, although not exhaustive, groups of molecular phenomena for detailed exploration: ISO, DIS, NRR and ESIPT. They are connected to a range of observables, which will be defined early on but whose calculation represents almost the final step of the roadmap (Figure 4). Prioritizing direct

calculations of molecular observables reduces the influence of different PES representations, ensuring that benchmarks maintain scientific relevance by predicting measurable quantities.

As discussed above, this relates to the question about the role of experimental data in benchmarking theoretical methods. While reproducing experimental measurements remains a key objective for the community, the direct prediction of experimental observables should currently be viewed as a goal rather than a strategy for benchmarking. Confidently bridging the gap between experiment and theory requires active collaborations from both sides in order to drive the development of all aspects and ingredients of NAMD, and as such, remains an ongoing area of research. However, this should not impede the evaluation of NAMD methods in the context of benchmarking. Therefore, we currently do not recommend the systematic assessment of theoretical results by direct comparison with experimental measurements unless the same experimental observable is calculated. Even then, caution is required. In trajectory-based NAMD methods, observables such as photoelectron spectra may be reproduced with comparatively few trajectories, 446,447 while branching ratios require more. 106 As a consequence, it may be misleading to judge convergence and overall accuracy on the basis of a single observable. In addition, in Section 2.6, we focused our attention on the role of ultrafast spectroscopy in the context of benchmarking NAMD. Alternative and complementary experimental techniques, such as time-resolved mass spectrometry, can provide insights into ultrafast structural dynamics with femtosecond time resolution 448-452 (thus, having the potential to serve as a highthroughput data source for nonadiabatic simulation benchmarks), but accurate simulations of ultrafast processes in gasphase ion (as compared to neutral) chemistry remain relatively underexplored.453

Molecular benchmarking should rather focus on comparing the theoretical approximations directly with exact or nearly exact solutions from theory, an approach that allows full control over external parameters and ensures a fair comparison. Recognizing that nearly exact solutions may not always be available or feasible to estimate, we refer to the concept of benchmarking by comparison. This involves comparing different methods without an absolute reference point. Even in such cases, we can establish a theoretical best estimate (TBE): a prediction from a method that provides the highest level of accuracy in treating nonadiabatic effects in that system. In this context, it is crucial that NAMD calculations are properly converged to the limit of their nuclear basis set or number of trajectories to ensure reliable comparisons. It is worth noting that TBEs have also been used in electronic structure benchmarks and have been updated progressively over time. 34,456,457

Using consistent electronic structure methods and equivalent initial conditions for comparing NAMD methods is generally less contentious as an idea, but the practical implementation poses challenges. We have thoroughly discussed these complexities to address all underlying nuances. The systems of interest should avoid prohibitively expensive electronic structure, so as to allow the sufficient convergence of dynamics results, especially for the more computationally demanding approaches. Full dimensional LVC models, which require modest computational resources, may serve as a suitable testing ground for a wide range of methods, particularly in cases like internal conversion and intersystem crossing in NRR, which do not necessarily involve large-amplitude motions (as in ISO) or bond breaking

(as in DIS and ESIPT). The exploration of ISO, DIS, and ESIPT phenomena requires more efforts on the accurate electronic structure evaluation. This would involve selecting electronic structure methods that are affordable, numerically stable, and widely accessible to the community through preferably software packages that are free of charge for the scientific community. Alternatively, one can take advantage of analytical potentials that have been previously obtained and used in NAMD calculations, keeping in mind that it is sometimes not straightforward to transfer a given analytical expressions into the specific form, as for instance a sum-of-products form.

In the generation of initial conditions, using simple approximations like the sudden approximation and the use of a harmonic approximation to describe the ground-state potential could mitigate the complications with initiating different NAMD methods. Nonetheless, translation between the adiabatic and diabatic representations of electronic states requires more meticulous considerations.

Research activities that are currently prioritized involve testing preliminary molecular systems and phenomena selected from a short list with strong potential as effective benchmarks. In this context, "system" refers not only to the molecule itself but also to its electronic structure representation and the possibility of calculating relevant observables. Some of the molecular systems under investigation leverage the advantages of vibronic coupling potentials. At the same time, others already have available preconstructed PESs that would also be suitable for efficient on-the-fly simulations. Following initial scrutiny, the most promising systems will be selected for benchmarking.

Another ongoing effort involves the creation of a common online repository. Making research data openly available encourages wide participation by researchers from the field, promoting transparency, accessibility, and collaboration. An accessible online repository will allow storage of essential data such as input files, all information relevant for reproducibility and the collection of the results of the benchmarking. Here, the utilization of data science and machine learning techniques, which are rapidly advancing and increasingly permeating chemical and materials sciences, can play a critical role in supporting and maintaining data repositories. These approaches enable efficient data curation, analysis, and debugging, and are especially valuable for integrating data of varying fidelity and origin, thereby enhancing the robustness and usability of complex data sets. 458

Once the initial set of benchmark systems is finalized and agreed upon by community members, a common set of initial conditions will be established and made available in the repository. Hereby, we recommend entrusting the preparation of initial conditions to a single dedicated research team, making sure that all types of NAMD methods are covered comprehensively. At this stage, establishing standardized input and output data formats is also anticipated to enhance the broader usability of the benchmark set. An appropriate electronic structure method, along with freely available software, will be selected for on-the-fly dynamics. All necessary quantities, input data, and (if required) initial wave function files will be incorporated into the repository. For methods that require analytical potentials, these will either be sourced from existing literature or parametrized and shared in the repository. Additionally, a set of relevant observables will be identified for each system, chosen to capture and represent the key aspects of nuclear and electronic dynamics. Comprehensive instructions and materials detailing the calculation of these observables will

be provided to ensure consistent evaluation across all NAMD simulations. Additionally, it could be useful to standardize the tools used for postprocessing and analysis of NAMD data. Selecting a dedicated Python framework (or equivalent) would ensure consistency in analyzing observables, trajectory-based statistics, and error quantification, streamlining testing workflows, and promoting transparency across different benchmarking studies. The selection of initial conditions, of the electronic structure method and of the relevant observables will be performed in parallel, as indicated in the roadmap of Figure 4, ultimately converging in the creation of a repository.

Using the system information gathered in the repository, all researchers interested in participating in the benchmarking effort can test their NAMD methodologies and software on the designated test-set. This benchmarking initiative aims to engage researchers with diverse expertise, encompassing the full range of NAMD methods, from trajectory-based approaches to quantum wavepacket-propagation techniques and quantumcomputing approaches. This diversity is particularly desired in the realm of benchmarking by comparison, as each method should ideally be leveraged to its utmost potential, using the optimal choice of parameters associated with best practices for each NAMD approach. The calculated results, along with the best practice procedures, are expected to be published in conventional research articles as well as the data shared through the repository - ensuring that benchmarks remain valuable longterm resources. The benchmarking results will be evaluated by the community members during a collective meeting. Based on the data, the goal is to assess the quality of different NAMD approaches for various molecular groups. Additionally, guidelines will be introduced for future NAMD method development, defining standardized tests and expected results to evaluate the performance of new methods.

In the long run, we foresee a continuous refinement of molecular benchmarks aligned with the ongoing advancements in the field that invariably present new challenges. More complex features will be gradually introduced, and likewise, benchmarks will be expanded to include complex systems and phenomena. This covers, for example, molecules in realistic environments (such as solvents, surfaces and materials), 460–464 an explicit treatment of light-matter interactions, 376 high density of states, and long dynamics. The utilization of machine learning approaches in these efforts has shown great promise in significantly reducing computational cost without compromising numerical accuracy, as clearly demonstrated by early studies in the field. 364,465,466 Finally, a synergistic approach that integrates theory and experiment (within the context of benchmarking) will inevitably emerge as a key task for the broader NAMD community.

Alongside this *roadmap*, which serves as an initial effort to disseminate our thoughts about benchmarking methods for NAMD, we aim at promoting the broader participation from community members beyond the present core group of contributors, as well as organizing regular meetings and progress reports to ensure the successful accomplishment of the plan.

#### AUTHOR INFORMATION

# **Corresponding Authors**

Federica Agostini — CNRS, Institut de Chimie Physique UMR 8000, Université Paris-Saclay, 91405 Orsay, France; o orcid.org/0000-0003-2951-4964;

Email: federica.agostini@universite-paris-saclay.fr

- Sandra Gómez Departamento de Química, Módulo 13, Universidad Autónoma de Madrid, 28049 Madrid, Spain; orcid.org/0000-0002-1874-6578; Email: sandra.gomezr@uam.es
- Lea M. Ibele CNRS, ICR, Aix Marseille University, 13397 Marseille, France; CNRS, Institut de Chimie Physique UMR 8000, Université Paris-Saclay, 91405 Orsay, France; orcid.org/0000-0002-1434-3843; Email: leamaria.ibele@univ-amu.fr
- Antonio Prlj Department of Physical Chemistry, Rudjer Bošković Institute, 10000 Zagreb, Croatia; o orcid.org/ 0000-0002-5589-9776; Email: antonio.prlj@irb.hr

#### **Authors**

- Léon L. E. Cigrang Department of Chemistry, University College London, WC1H 0AJ London, United Kingdom; orcid.org/0009-0004-8118-5699
- Basile F. E. Curchod Centre for Computational Chemistry, School of Chemistry, University of Bristol, Bristol BS8 1TS, United Kingdom
- Rebecca A. Ingle Department of Chemistry, University College London, WC1H 0AJ London, United Kingdom; orcid.org/0000-0002-0566-3407
- Aaron Kelly Hamburg Center for Ultrafast Imaging, Universität Hamburg and Max Planck Institute for the Structure and Dynamics of Matter, 22761 Hamburg, Germany
- Jonathan R. Mannouch Hamburg Center for Ultrafast Imaging, Universität Hamburg and Max Planck Institute for the Structure and Dynamics of Matter, 22761 Hamburg, Germany; orcid.org/0000-0003-3090-8987
- Davide Accomasso Faculty of Chemistry, University of Warsaw, Warsaw 00-927, Poland; Department of Industrial Chemistry, University of Bologna, Bologna 40126, Italy; orcid.org/0000-0002-4100-4679
- Alexander Alijah Groupe de Spectrométrie Moléculaire et Atmosphérique, GSMA, UMR CNRS 7331, Université de Reims Champagne-Ardenne, U.F.R. Sciences Exactes et Naturelles, 51687 Reims Cedex 2, France; orcid.org/0000-0002-4915-0558
- Mario Barbatti CNRS, ICR, Aix Marseille University, 13397 Marseille, France; Institut Universitaire de France, 75231 Paris, France; oorcid.org/0000-0001-9336-6607
- Wiem Chebbi Laboratoire de Spectroscopie Atomique, Moléculaire et Applications (LSAMA), University of Tunis El Manar, 1060 Tunis, Tunisia
- Nadja Došlić Department of Physical Chemistry, Rudjer Bošković Institute, 10000 Zagreb, Croatia; orcid.org/ 0000-0001-6535-9020
- Elliot C. Eklund School of Chemistry, University of Sydney, Sydney, NSW 2006, Australia
- Antonia Freibert Department of Physics, University of Hamburg, 22761 Hamburg, Germany; orcid.org/0000-0002-6197-2597
- Leticia González Institute of Theoretical Chemistry, Faculty of Chemistry, University of Vienna, A-1090 Vienna, Austria; orcid.org/0000-0001-5112-794X
- Giovanni Granucci Department of Chemistry and Industrial Chemistry, University of Pisa, 56124 Pisa, Italy; ocid.org/0000-0002-4753-6318

- Federico J. Hernández Centre for Computational Chemistry, School of Chemistry, University of Bristol, Bristol BS8 1TS, United Kingdom; ocid.org/0000-0001-7497-9424
- Javier Hernández-Rodríguez Departamento de Química Física, Universidad de Salamanca, Salamanca 37008, Spain
- Amber Jain − Department of Chemistry, Indian Institute of Technology Bombay, Mumbai 400076, India; ocid.org/0000-0003-4108-9112
- Jiří Janoš Department of Physical Chemistry, University of Chemistry and Technology, 16628 Prague, Czech Republic; Centre for Computational Chemistry, School of Chemistry, University of Bristol, Bristol BS8 1TS, United Kingdom; orcid.org/0000-0001-5903-8538
- Ivan Kassal School of Chemistry, University of Sydney, Sydney, NSW 2006, Australia; orcid.org/0000-0002-8376-0819
- Adam Kirrander Physical and Theoretical Chemistry Laboratory, Department of Chemistry, University of Oxford, OX1 3QZ Oxford, United Kingdom; orcid.org/0000-0002-3347-8137
- Zhenggang Lan MOE Key Laboratory of Environmental Theoretical Chemistry, School of Environment, South China Normal University, Guangzhou 510006, China; SCNU Environmental Research Institute, Guangdong Provincial Key Laboratory of Chemical Pollution and Environmental Safety, Guangzhou 510631, China; orcid.org/0000-0002-8509-0388
- Henrik R. Larsson Department of Chemistry and Biochemistry, University of California, Merced, California 95343, United States; Occid.org/0000-0002-9417-1518
- David Lauvergnat CNRS, Institut de Chimie Physique UMR 8000, Université Paris-Saclay, 91405 Orsay, France; orcid.org/0000-0002-8258-3531
- Brieuc Le Dé CNRS, Institut des Nanosciences de Paris, Sorbonne Université, 75005 Paris, France; ocid.org/0000-0001-6004-0758
- Yeha Lee Laboratory of Theoretical Physical Chemistry, Institut des Sciences et Ingénierie Chimiques, Ecole Polytechnique Fédérale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland
- Neepa T. Maitra Department of Physics, Rutgers University, Newark, New Jersey 07102, United States; orcid.org/ 0000-0002-1840-8827
- Seung Kyu Min Department of Chemistry, Ulsan National Institute of Science and Technology (UNIST), Ulsan 44919, South Korea; orcid.org/0000-0001-5636-3407
- Daniel Peláez CNRS, Institut des Sciences Moléculaires d'Orsay, Université Paris-Saclay, 91405 Orsay, France; orcid.org/0000-0003-3924-7804
- David Picconi Institute of Theoretical and Computational Chemistry, Heinrich-Heine-Universität Düsseldorf, 40225 Düsseldorf, Germany; orcid.org/0000-0001-6468-1595
- Zixing Qiu CNRS, Institut des Sciences Moléculaires d'Orsay, Université Paris-Saclay, 91405 Orsay, France; MICS, CentraleSupélec, Paris-Saclay University, Gif-sur-Yvette 91190, France
- Umberto Raucci Italian Institute of Technology, Genoa 16153, Italy; o orcid.org/0000-0002-8219-224X
- Patrick Robertson School of Chemistry, University of Nottingham, Nottingham NG72RD, United Kingdom; orcid.org/0000-0003-0935-3331
- Eduarda Sangiogo Gil Institute of Theoretical Chemistry, Faculty of Chemistry, University of Vienna, 1090 Vienna, Austria; orcid.org/0000-0002-0945-2906

Marin Sapunar — Department of Physical Chemistry, Rudjer Bošković Institute, 10000 Zagreb, Croatia; ⊚ orcid.org/ 0000-0002-5717-1930

**Peter Schürger** – CNRS, Institut de Chimie Physique UMR 8000, Université Paris-Saclay, 91405 Orsay, France

Patrick Sinnott — School of Chemistry, University of Sydney, Sydney, NSW 2006, Australia

Sergei Tretiak — Theoretical Division and Center for Integrated Nanotechnologies, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, United States; Ocid.org/0000-0001-5547-3647

Arkin Tikku – School of Chemistry, University of Sydney, Sydney, NSW 2006, Australia

Patricia Vindel-Zandbergen — Department of Chemistry, New York University, New York, New York 10003, United States; Simons Center for Computational Physical Chemistry at New York University, New York, New York 10003, United States; orcid.org/0000-0003-3719-8199

Graham A. Worth — Department of Chemistry, University College London, WC1H 0AJ London, United Kingdom; orcid.org/0000-0002-2044-4499

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.jpca.5c02171

#### **Author Contributions**

<sup>†</sup>L.L.E.C., B.F.E.C., R.A.I., A.K., and J.R.M. contributed equally to this work.

#### Notes

The authors declare no competing financial interest.

#### **Biographies**



Federica Agostini received her Dr. rer. nat. in Physics from the University Sapienza in Rome (Italy) and the University Pierre et Marie Curie in Paris (France) in 2010 under the supervision of Prof. Giovanni Ciccotti and Prof. Rodolphe Vuilleumier. After two postdoctoral experiences, at the École Normale Supérieure in Paris with Prof. Rodolphe Vuilleumier and at the Max-Planck Institute of Microstructure Physics with Prof. E. K. U. Gross, she was appointed Associate Professor at the Chemistry Department of the University Paris-Saclay (France) in 2016. Her expertise is the development of theory and algorithms for nonadiabatic dynamics based on trajectories employing the exact factorization of the electron—nuclear wavefunction. She was awarded in 2022 the Young Researcher Prize of the Physical Chemistry Division of the French Chemical Society and she serves in the Editorial Board of Physical Review A for her expertise in chemical physics.



Sandra Gómez received her Dr. rer. nat. in Chemistry from the Universität Wien in 2019 under the supervision of Prof. Leticia González. She was a postdoctoral researcher at University College London with Prof. Graham A. Worth (2019–2022), followed by an independent research fellowship at the University of Salamanca (2022–2024). In 2024, she joined the Universidad Autónoma de Madrid as an Assistant Professor for the Chemistry Department. Her research focuses on nonadiabatic dynamics in photochemistry and photophysics, with applications ranging from femtochemistry and optoelectronics to bioimaging. She is a member of the JACS Au Early Career Advisory Board and is involved in the organization of the Virtual Winter School for Computational Chemistry.



Lea M. Ibele received her doctoral degree in Chemistry in 2022 from the University of Durham in the United Kingdom, under the supervision of Prof. Basile Curchod. Until 2024, she pursued a postdoctoral position at the University Paris-Saclay in France, working with Dr. Federica Agostini. Since January 2025, she holds a position as a CNRS researcher at the Institute of Radical Chemistry at Aix Marseille University. Her research focus lies on benchmarks for nonadiabatic dynamics, computational time-resolved spectroscopy and the simulation of radiative processes. She also actively contributes to scientific outreach and is part of the Calliope. Join the Dots. program, an initiative of the Austrian Ministry for European and International Affairs.



Antonio Prlj received his doctoral degree in Chemistry in 2017 from the École Polytechnique Fédérale de Lausanne (EPFL) in Switzerland, under the supervision of Prof. Clémence Corminboeuf. His research focused on noncovalent interactions, organic electronics, and nonadiabatic molecular dynamics. After completing his PhD, he pursued a postdoctoral position with Prof. Jiří Vaniček at EPFL, working with semiclassical methods, followed by a second postdoctoral stay with Prof. Basile Curchod at Durham and Bristol Universities (UK), where he investigated in silico photochemistry of atmospheric molecules and challenges related to initial conditions in nonadiabatic dynamics. Since 2022, he has been employed as a research associate at the Rudjer Bošković Institute in Zagreb, where he continues to explore nonadiabatic phenomena and excited-state processes. He has coorganized several international conferences, including two CECAM workshops.

## ACKNOWLEDGMENTS

We are grateful to the Centre Européen de Calcul Atomique et Moléculaire (CECAM) for funding for the workshop which inspired this Perspective. We also thank the staff at the CECAM Headquarters at EPF-Lausanne, Switzerland, and at the CECAM node based in Île-de-France (CECAM-FR-MOSER), for their support in developing and advertising the program, and for their assistance in the organization of the workshop. We acknowledge fruitful discussions and contributions from Jorge Alonso De La Fuente, Liudmil Antonov, Davide Barbiero, Lou Barreau, Julien Eng, Dario Frassi, Scott Habershon, John Herbert, Christine Isborn, Yorick Lassmann, Ben Levine, Hiroki Nakamura, Igor Schapiro, Burkhard Schmidt, Jiří Vaníček and Sergei Yurchenko. B.F.E.C. and G.A.W. acknowledge support from the EPSRC under grants EP/V026690/1 and EP/ X026973/1. B.F.E.C. also acknowledges funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (Grant agreement No. 803718, project SINDAM) and EPSRC grant EP/Y01930X/1. R.I. was supported by the Engineering and Physical Sciences Research Council (Grant No. EP/ X031519/1). A.K. and A.F. were supported by the Cluster of Excellence "CUI: Advanced Imaging of Matter" of the Deutsche Forschungsgemeinschaft (DFG) (EXC 2056, Project 390715994). J.R.M. acknowledges support from the Alexander von Humboldt Foundation. D.A. acknowledges funding from the National Science Centre (Poland) under the project No. 2022/47/P/ST4/01418, and the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No. 945339. M.B. received support from the French government under the France 2030 investment plan as part of the Initiative d'Excellence d'AixMarseille Université (AMX-22-IN1-48) and from the European Research Council (ERC) Advanced Grant SubNano (Grant agreement 832237). E.C.E., P.S., A.T., and I.K. acknowledge support by Google, by the Australian Research Council (FT230100653), and by the United States Office of Naval Research Global (N62909-24-1-2083). N.D. acknowledges the support by the Croatian Science Foundation under the project numbers [HRZZ-IP-2020-02-9932 and HRZZ-IP-2022-10-4658]. J.J. thanks the Czech Science Foundation for the support via grant number 23-07066S. A.K. acknowledges funding from the Engineering and Physical Sciences Research Council grants EP/V006819/2, EP/V049240/2, EP/X026698/1, EP/ X026973/1, the U.S. Department of Energy, Office of Science, Basic Energy Sciences, under award number DE-SC0020276, and the Leverhulme Trust via grant RPG-2020-208. H.R.L. was supported by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences, CPIMS program, under Award DE-SC0024267 (ML-MCTDH and PES representations), by the U.S. National Science Foundation under grant no. CHE-2312005 (connecting ML-MCTDH to TD-DMRG), and by the American Chemical Society Petroleum Research Fund via grant no. 67511-DNI6 (electronic structure). D.P. and Z.Q. gratefully acknowledge the project UDOPIA and the French National Research Agency (ANR), as well as Institut DATAIA Paris-Saclay, the AI institute of the University Paris-Saclay for his Ph.D. funding (https://www.dataia.eu/). D.P. also acknowledges ANR-DFG financial support for the QD4ICEC project Grant number ANR-22-CE92-0071-02. N.M. acknowledges the National Science Foundation (NSF) under Award No. CHE-2154829. P.R. would like to acknowledge the School of Chemistry at the University of Nottingham, and the Hobday Fund for their start-up funding. S.T. and S.F.A. acknowledge the Center for Integrated Nanotechnology (CINT) at Los Alamos National Laboratory (LANL), a U.S. DOE and Office of Basic Energy Sciences user facility. F.A. and P.S. acknowledge financial support from the French Agence Nationale de la Recherche via the project STROM (Grant No. ANR-23-ERCC-0002). F.A. and L.M.I. acknowledge financial support from a public grant from the Laboratoire d'Excellence Physics Atoms Light Matter (LabEx PALM) overseen by the French National Research Agency (ANR) as part of the "Investissements d'Avenir" program (reference: ANR-10-LABX-0039-PALM). F.A. also acknowledges financial support from the French Agence Nationale de la Recherche via the project Q-DeLight (Grant No. ANR-20-CE29-0014). A.P. acknowledges the support by the Croatian Science Foundation under the project number HRZZ-IP-2020-02-7262.

## REFERENCES

- (1) Born, M.; Oppenheimer, R. Zur Quantentheorie der Molekeln. Ann. Phys. 1927, 84, 457–484.
- (2) Domcke, W.; Yarkony, D. R.; Köppel, H. Conical Intersections: Electronic Structure, Dynamics & Spectroscopy; World Scientific: 2004; Vol. 15.
- (3) Baer, M.Beyond Born-Oppenheimer: Electronic Nonadiabatic Coupling Terms and Conical Intersections; Wiley Interscience: 2006.
- (4) Tannor, D. J.Introduction to Quantum Mechanics: A Time-Dependent Perspective; University Science Books: 2007.
- (5) Tully, J. C. Perspective: Nonadiabatic dynamics theory. *J. Chem. Phys.* **2012**, 137, 22A301.
- (6) Crespo-Otero, R.; Barbatti, M. Recent Advances and Perspectives on Nonadiabatic Mixed Quantum-Classical Dynamics. *Chem. Rev.* **2018**, *118*, 7026–7068.

- (7) Curchod, B. F. E.; Martínez, T. J. Ab Initio Nonadiabatic Quantum Molecular Dynamics. *Chem. Rev.* **2018**, *118*, 3305–3336.
- (8) Ibele, L.-M.; Sangiogo Gil, E.; Villaseco Arribas, E.; Agostini, F. Simulations of photoinduced processes with the exact factorization: state of the art and perspectives. *Phys. Chem. Chem. Phys.* **2024**, *26*, 26693–26718.
- (9) Nelson, T. R.; White, A. J.; Bjorgaard, J. A.; Sifain, A. E.; Zhang, Y.; Nebgen, B.; Fernandez-Alberti, S.; Mozyrsky, D.; Roitberg, A. E.; Tretiak, S. Non-adiabatic Excited-State Molecular Dynamics: Theory and Applications for Modeling Photophysics in Extended Molecular Materials. *Chem. Rev.* **2020**, *120*, 2215–2287.
- (10) Zewail, A. H. Laser Femtochemistry. Science 1988, 242, 1645–
- (11) Zewail, A. H. Femtochemistry: Atomic-Scale Dynamics of the Chemical Bond. *J. Phys. Chem. A* **2000**, *104*, 5660–5694.
- (12) Stolow, A.; Bragg, A. E.; Neumark, D. M. Femtosecond Time-Resolved Photoelectron Spectroscopy. *Chem. Rev.* **2004**, *104*, 1719–1758.
- (13) Kowalewski, M.; Fingerhut, B. P.; Dorfman, K. E.; Bennett, K.; Mukamel, S. Simulating Coherent Multidimensional Spectroscopy of Nonadiabatic Molecular Processes: From the Infrared to the X-ray Regime. *Chem. Rev.* **2017**, *117*, 12165–12226.
- (14) Maiuri, M.; Garavelli, M.; Cerullo, G. Ultrafast Spectroscopy: State of the Art and Open Challenges. *J. Am. Chem. Soc.* **2020**, *142*, 3–15.
- (15) Kraus, P. M.; Zürch, M.; Cushing, S. K.; Neumark, D. M.; Leone, S. R. The ultrafast X-ray spectroscopic revolution in chemical dynamics. *Nat. Rev. Chem.* **2018**, *2*, 82–94.
- (16) Worth, G. A.; Beck, M. H.; Jäckle, A.; Meyer, H.-D. The MCTDH Package, Version 8.2, (2000). H.-D. Meyer, Version 8.3 (2002), Version 8.4 (2007). O. Vendrell and H.-D. Meyer, Version 8.5 (2013). http://mctdh.uni-hd.de (accessed Jun 2, 2025).
- (17) Barbatti, M.; Bondanza, M.; Crespo-Otero, R.; Demoulin, B.; Dral, P. O.; Granucci, G.; Kossoski, F.; Lischka, H.; Mennucci, B.; Mukherjee.; et al. Newton-X Platform: New Software Developments for Surface Hopping and Nuclear Ensembles. *J. Chem. Theory Comput.* 2022, 18, 6851–6865.
- (18) Mai, S.; Marquetand, P.; González, L. Nonadiabatic dynamics: The SHARC approach. *Wiley Interdiscip. Rev.: Comput. Mol. Sci.* **2018**, 8, No. e1370.
- (19) Shakiba, M.; Smith, B.; Li, W.; Dutra, M.; Jain, A.; Sun, X.; Garashchuk, S.; Akimov, A. Libra: A modular software library for quantum nonadiabatic dynamics. *Softw. Impacts* **2022**, *14*, No. 100445.
- (20) Worth, G. A. QUANTICS: A general purpose package for quantum molecular dynamics simulations. *Comput. Phys. Commun.* **2020**, 248, No. 107040.
- (21) Granucci, G.; Persico, M.; Accomasso, D.; Sangiogo Gil, E.; Corni, S.; Fregoni, J.; Laino, T.; Tesi, M.; Toniolo, A.MOPAC-PI: a program for excited state dynamics simulations based on nonadiabatic trajectories and semiempirical electronic structure calculations, 2024. https://gitlab.com/granucci/mopacpi.git (accessed Jun 2, 2025).
- (22) Thiel, W. Semiempirical quantum—chemical methods. WIREs Comput. Mol. Sci. 2014, 4, 145—157.
- (23) CPMD. Copyright IBM Corp 1990–2019, Copyright MPI für Festkörperforschung Stuttgart 1997–2001, 2024. http://www.cpmd.org/.
- (24) Pereira, A.; Knapik, J.; Chen, A.; Lauvergnat, D.; Agostini, F. Quantum molecular dynamics simulations of the effect of secondary modes on the photoisomerization of a retinal chromophore model. *Eur. Phys. J. Spec. Top.* **2023**, 232, 1917–1933.
- (25) Lee, I. S.; Ha, J. K.; Han, D.; Kim, T. I.; Moon, S. W.; Min, S. K. PyUNIxMD: A Python-based excited state molecular dynamics package. *J. Comput. Chem.* **2021**, *42*, 1755–1766.
- (26) Akimov, A. V.; Prezhdo, O. V. The PYXAID Program for Non-Adiabatic Molecular Dynamics in Condensed Matter Systems. *J. Chem. Theory Comput.* **2013**, *9*, 4959–4972.
- (27) Weingart, O.; Nenov, A.; Altoè, P.; Rivalta, I.; Segarra-Martí, J.; Dokukina, I.; Garavelli, M. COBRAMM 2.0—A software interface for

- tailoring molecular electronic structure calculations and running nanoscale (QM/MM) simulations. J. Mol. Model. 2018, 24, 271.
- (28) Fedorov, D. A.; Seritan, S.; Fales, B. S.; Martínez, T. J.; Levine, B. G. PySpawn: Software for Nonadiabatic Quantum Molecular Dynamics. *J. Chem. Theory Comput.* **2020**, *16*, 5485–5498.
- (29) Du, L.; Lan, Z. An On-the-Fly Surface-Hopping Program JADE for Nonadiabatic Molecular Dynamics of Polyatomic Systems: Implementation and Applications. *J. Chem. Theory Comput.* **2015**, *11*, 1360–1374.
- (30) Malone, W.; Nebgen, B.; White, A.; Zhang, Y.; Song, H.; Bjorgaard, J. A.; Sifain, A. E.; Rodriguez-Hernandez, B.; Freixas, V. M.; Fernandez-Alberti, S.; et al. NEXMD Software Package for Nonadiabatic Excited State Molecular Dynamics Simulations. *J. Chem. Theory Comput.* **2020**, *16*, 5771–5783.
- (31) Mitrić, R.; Petersen, J.; Bonačić-Kouteckỳ, V. Laser-field-induced surface-hopping method for the simulation and control of ultrafast photodynamics. *Phys. Rev. A* **2009**, 79, No. 053416.
- (32) Prediction Challenge: Cyclobutanone Photochemistry. https://pubs.aip.org/collection/16531/Prediction-Challenge-Cyclobutanone-Photochemistry (accessed Jun 2, 2025).
- (33) Delta project. https://molmod.ugent.be/deltacodesdft (accessed Jun 2, 2025).
- (34) Schreiber, M.; Silva-Junior, M. R.; Sauer, S. P. A.; Thiel, W. Benchmarks for electronically excited states: CASPT2, CC2, CCSD, and CC3. *J. Chem. Phys.* **2008**, *128*, 134110.
- (35) Lejaeghere, K.; Bihlmayer, G.; Björkman, T.; Blaha, P.; Blügel, S.; Blum, V.; Caliste, D.; Castelli, I. E.; Clark, S. J.; Dal Corso, A.; et al. Reproducibility in density functional theory calculations of solids. *Science* **2016**, *351*, aad3000.
- (36) Adamo, C.; Jacquemin, D. The calculations of excited-state properties with Time-Dependent Density Functional Theory. *Chem. Soc. Rev.* **2013**, *42*, 845–856.
- (37) HyDRA Challenge. https://qmbench.net/challenges/hydra/hydra. (accessed Jun 2, 2025).
- (38) Fe-MAN challenge. https://qmbench.net/challenges/feman/feman (accessed Jun 2, 2025).
- (39) CECAM workshop: Standardizing nonadiabatic dynamics: towards common benchmarks. https://www.cecam.org/workshop-details/standardizing-nonadiabatic-dynamics-towards-common-benchmarks-1304, May 2024.
- (40) Tully, J. C. Molecular dynamics with electronic transitions. *J. Chem. Phys.* **1990**, 93, 1061–1071.
- (41) Shin, S.; Metiu, H. Nonadiabatic effects on the charge transfer rate constant: A numerical study of a simple model system. *J. Chem. Phys.* **1995**, *102*, 9285–9295.
- (42) Hahn, S.; Stock, G. Quantum-Mechanical Modeling of the Femtosecond Isomerization in Rhodopsin. *J. Phys. Chem. B* **2000**, *104*, 1146–1149.
- (43) Engel, V.; Metiu, H. A quantum mechanical study of predissociation dynamics of NaI excited by a femtosecond laser pulse. *J. Chem. Phys.* **1989**, *90*, 6116–6128.
- (44) Schneider, R.; Domcke, W.  $S_1$ - $S_2$  conical intersection and ultrafast  $S_1 \rightarrow S_2$  internal conversion in pyrazine. *Chem. Phys. Lett.* **1988**, 150, 235–242.
- (45) Hack, M. D.; Wensmann, A. M.; Truhlar, D. G.; Ben-Nun, M.; Martínez, T. J. Comparison of full multiple spawning, trajectory surface hopping, and converged quantum mechanics for electronically nonadiabatic dynamics. *J. Chem. Phys.* **2001**, *115*, 1172–1186.
- (46) Choi, S.; Vaníček, J. How important are the residual nonadiabatic couplings for an accurate simulation of nonadiabatic quantum dynamics in a quasidiabatic representation? *J. Chem. Phys.* **2021**, *154*, 124119.
- (47) Limbu, D. K.; Shakib, F. A. SHARP pack: A modular software for incorporating nuclear quantum effects into non-adiabatic dynamics simulations. *Softw. Impacts* **2024**, *19*, No. 100604.
- (48) Kundu, S.; Makri, N. PathSum: A C++ and Fortran suite of fully quantum mechanical real-time path integral methods for (multi-) system+bath dynamics. *J. Chem. Phys.* **2023**, *158*, 224801.

- (49) Xie, W.; Sapunar, M.; Došlić, N.; Sala, M.; Domcke, W. Assessing the performance of trajectory surface hopping methods: Ultrafast internal conversion in pyrazine. *J. Chem. Phys.* **2019**, *150*, 154119.
- (50) Coonjobeeharry, J.; Spinlove, K. E.; Sanz Sanz, C.; Sapunar, M.; Došlić, N.; Worth, G. A. Mixed-quantum-classical or fully-quantized dynamics? A unified code to compare methods. *Philos. Trans. R. Soc. A* **2022**, 380, 20200386.
- (51) Plasser, F.; Gómez, S.; Menger, M. F. S. J.; Mai, S.; González, L. Highly efficient surface hopping dynamics using a linear vibronic coupling model. *Phys. Chem. Chem. Phys.* **2019**, *21*, 57–69.
- (52) Nelson, T.; Naumov, A.; Fernandez-Alberti, S.; Tretiak, S. Nonadiabatic excited-state molecular dynamics: On-the-fly limiting of essential excited states. *Chem. Phys.* **2016**, *481*, 84–90.
- (53) Ibele, L. M.; Curchod, B. F. E. A molecular perspective on Tully models for nonadiabatic dynamics. *Phys. Chem. Chem. Phys.* **2020**, 22, 15183–15196.
- (54) Gómez, S.; Spinlove, E.; Worth, G. Benchmarking non-adiabatic quantum dynamics using the molecular Tully models. *Phys. Chem. Chem. Phys.* **2024**, 26, 1829–1844.
- (55) Mannouch, J. R.; Kelly, A. Quantum Quality with Classical Cost: Ab Initio Nonadiabatic Dynamics Simulations Using the Mapping Approach to Surface Hopping. *J. Phys. Chem. Lett.* **2024**, *15*, 5814–5823.
- (56) Ibele, L. M.; Lassmann, Y.; Martínez, T. J.; Curchod, B. F. E. Comparing (stochastic-selection) ab initio multiple spawning with trajectory surface hopping for the photodynamics of cyclopropanone, fulvene, and dithiane. *J. Chem. Phys.* **2021**, *154*, 104110.
- (57) Weight, B. M.; Mandal, A.; Huo, P. Ab initio symmetric quasiclassical approach to investigate molecular Tully models. *J. Chem. Phys.* **2021**, *155*, No. 084106.
- (58) Weight, B. M.; Mandal, A.; Hu, D.; Huo, P. Ab initio spin-mapping non-adiabatic dynamics simulations of photochemistry. *J. Chem. Phys.* **2025**, *162*, No. 084105.
- (59) Avagliano, D.; Lorini, E.; González, L. Sampling effects in quantum mechanical/molecular mechanics trajectory surface hopping non-adiabatic dynamics. *Philos. Trans. R. Soc. A* **2022**, *380*, 20200381.
- (60) Vindel-Zandbergen, P.; Ibele, L. M.; Ha, J.-K.; Min, S. K.; Curchod, B. F. E.; Maitra, N. T. Study of the Decoherence Correction Derived from the Exact Factorization Approach for Nonadiabatic Dynamics. *J. Chem. Theory Comput.* **2021**, *17*, 3852–3862.
- (61) Tokić, N.; Piteša, T.; Prlj, A.; Sapunar, M.; Došlić, N. Advantages and Limitations of Landau-Zener Surface Hopping Dynamics. *Croat. Chem. Acta* **2024**, *97*, 205.
- (62) Michl, J.; Bonačić-Koutecký, V. Electronic Aspects of Organic Photochemistry; Wiley: 1990.
- (63) Turro, N. J. Modern Molecular Photochemistry; University Science Books: 1991.
- (64) Persico, M.; Granucci, G.Photochemistry: A Modern Theoretical Perspective; Springer: 2018.
- (65) May, V.; Kühn, O.Charge and Energy Transfer Dynamics in Molecular Systems; John Wiley & Sons: 2011.
- (66) Wade, A. D.The Semantic Scholar Academic Graph (S2AG). In WWW'22: Companion Proceedings of the Web Conference 2022; Association for Computing Machinery: 2022.
- (67) Wald, G. Molecular Basis of Visual Excitation. *Science* **1968**, *162*, 230–239.
- (68) Warshel, A. Bicycle-pedal model for the first step in the vision process. *Nature* **1976**, *260*, *679*–*683*.
- (69) Bandara, H. D.; Burdette, S. C. Photoisomerization in different classes of azobenzene. *Chem. Soc. Rev.* **2012**, *41*, 1809–1825.
- (70) Waldeck, D. H. Photoisomerization dynamics of stilbenes. *Chem. Rev.* **1991**, *91*, 415–436.
- (71) Kortekaas, L.; Browne, W. R. The evolution of spiropyran: fundamentals and progress of an extraordinarily versatile photochrome. *Chem. Soc. Rev.* **2019**, *48*, 3406–3424.
- (72) Levine, B. G.; Martínez, T. J. Isomerization Through Conical Intersections. *Annu. Rev. Phys. Chem.* **2007**, *58*, 613–634.

- (73) Schinke, R.Photodissociation Dynamics: Spectroscopy and Fragmentation of Small Polyatomic Molecules; Cambridge University Press: 1995.
- (74) Scherer, N. F.; Knee, J. L.; Smith, D. D.; Zewail, A. H. Femtosecond Photofragment Spectroscopy: The Reaction ICN  $\rightarrow$  CN + I. *J. Phys. Chem.* **1985**, 89, 5141–5143.
- (75) Rose, T. S.; Rosker, M. J.; Zewail, A. H. Femtosecond real-time observation of wave packet oscillations (resonance) in dissociation reactions. *J. Chem. Phys.* **1988**, *88*, 6672–6673.
- (76) Foth, H. J.; Polanyi, J. C.; Telle, H. H. Emission from molecules and reaction intermediates in the process of falling apart. *J. Phys. Chem.* **1982**, *86*, 5027–5041.
- (77) Engel, V.; Metiu, H. The study of NaI predissociation with pumpprobe femtosecond laser pulses: The use of an ionizing probe pulse to obtain more detailed dynamic information. *Chem. Phys. Lett.* **1989**, *155*, 77–82.
- (78) Williams, S. O.; Imre, D. G. Determination of real time dynamics in molecules by femtosecond laser excitation. *J. Phys. Chem.* **1988**, 92, 6648–6654.
- (79) Engel, V.; Metiu, H.; Almeida, R.; Marcus, R. A.; Zewail, A. H. Molecular state evolution after excitation with an ultra-short laser pulse: A quantum analysis of NaI and NaBr dissociation. *Chem. Phys. Lett.* **1988**, *152*, 1–7.
- (80) Choi, S. E.; Light, J. C. Use of the discrete variable representation in the quantum dynamics by a wave packet propagation: Predissociation of  $NaI(^{1}\Sigma_{0}^{+}) \rightarrow NaI(0^{+}) \rightarrow Na(^{2}S) + I(^{2}P)$ . J. Chem. Phys. 1989, 90, 2593–2604.
- (81) Chapman, S.; Child, M. S. A semiclassical study of long time recurrences in the femtosecond predissociation dynamics of NaI. *J. Phys. Chem.* **1991**, *95*, 578–584.
- (82) Liane, E. M.; Simmermacher, M.; Kirrander, A. Ultrafast X-ray scattering and electronic coherence at avoided crossings: complete isotropic signals. *J. Phys. B: At. Mol. Opt. Phys.* **2024**, *57*, 145602.
- (83) Betz, V.; Goddard, B. D.; Manthe, U. Wave packet dynamics in the optimal superadiabatic approximation. *J. Chem. Phys.* **2016**, *144*, 224109
- (84) Janoš, J.; Slavíček, P.; Curchod, B. F. E. Including Photoexcitation Explicitly in Trajectory-Based Nonadiabatic Dynamics at No Cost. *J. Phys. Chem. Lett.* **2024**, *15*, 10614–10622.
- (85) Blank, D. A.; North, S. W.; Lee, Y. T. The ultraviolet photodissociation dynamics of pyrrole. *Chem. Phys.* **1994**, *187*, 35–47.
- (86) Tseng, C.-M.; Lee, Y. T.; Lin, M.-F.; Ni, C.-K.; Liu, S.-Y.; Lee, Y.-P.; Xu, Z.; Lin, M.-C. Photodissociation Dynamics of Phenol. *J. Phys. Chem. A* **2007**, *111*, 9463–9470.
- (87) Satyapal, S.; Park, J.; Bersohn, R.; Katz, B. Dissociation of methanol and ethanol activated by a chemical reaction or by light. *J. Chem. Phys.* **1989**, *91*, 6873–6879.
- (88) Loreti, A.; Freixas, V. M.; Avagliano, D.; Segatta, F.; Song, H.; Tretiak, S.; Mukamel, S.; Garavelli, M.; Govind, N.; Nenov, A. WFOT: A Wave Function Overlap Tool between Single-and Multi-Reference Electronic Structure Methods for Spectroscopy Simulation. *J. Chem. Theory Comput.* **2024**, *20*, 4804–4819.
- (89) Curchod, B. F. E.; Sisto, A.; Martínez, T. J. Ab Initio Multiple Spawning Photochemical Dynamics of DMABN Using GPUs. *J. Phys. Chem. A* **2017**, *121*, 265–276.
- (90) Matsika, S.; Yarkony, D. R. Beyond Two-State Conical Intersections. Three-State Conical Intersections in Low Symmetry Molecules: the Allyl Radical. *J. Am. Chem. Soc.* **2003**, *125*, 10672–10676.
- (91) Rankine, C. D.; Nunes, J. P. F.; Robinson, M. S.; Lane, P. D.; Wann, D. A. A theoretical investigation of internal conversion in 1,2-dithiane using non-adiabatic multiconfigurational molecular dynamics. *Phys. Chem. Chem. Phys.* **2016**, *18*, 27170–27174.
- (92) Zobel, J. P.; Heindl, M.; Plasser, F.; Mai, S.; González, L. Surface Hopping Dynamics on Vibronic Coupling Models. *Acc. Chem. Res.* **2021**, *54*, 3760–3771.
- (93) Richter, M.; Marquetand, P.; González-Vázquez, J.; Sola, I.; González, L. Femtosecond Intersystem Crossing in the DNA Nucleobase Cytosine. *J. Phys. Chem. Lett.* **2012**, *3*, 3090–3095.

- (94) Mai, S.; Richter, M.; Marquetand, P.; González, L. Excitation of Nucleobases from a Computational Perspective II: Dynamics. In *Photoinduced Phenomena in Nucleic Acids I: Nucleobases in the Gas Phase and in Solvents*; Barbatti, M.; Borin, A. C.; Ullrich, S., Eds.; Springer International Publishing: 2015; pp 99–153.
- (95) Fu, B.; Han, Y. C.; Bowman, J. M.; Angelucci, L.; Balucani, N.; Leonori, F.; Casavecchia, P. Intersystem crossing and dynamics in  $O(^3P) + C_2H_4$  multichannel reaction: experiment validates theory. *Proc. Natl. Acad. Sci. U.S.A.* **2012**, *109*, 9733–9738.
- (96) Schnappinger, T.; Kölle, P.; Marazzi, M.; Monari, A.; González, L.; de Vivie-Riedle, R. Ab initio molecular dynamics of thiophene: the interplay of internal conversion and intersystem crossing. *Phys. Chem. Chem. Phys.* **2017**, *19*, 25662–25670.
- (97) Schnappinger, T.; Marazzi, M.; Mai, S.; Monari, A.; González, L.; de Vivie-Riedle, R. Intersystem Crossing as a Key Component of the Nonadiabatic Relaxation Dynamics of Bithiophene and Terthiophene. *J. Chem. Theory Comput.* **2018**, *14*, 4530–4540.
- (98) Minns, R. S.; Parker, D. S. N.; Penfold, T. J.; Worth, G. A.; Fielding, H. H. Competing ultrafast intersystem crossing and internal conversion in the "channel 3" region of benzene. *Phys. Chem. Chem. Phys.* **2010**, *12*, 15607–15615.
- (99) Reichardt, C.; Vogt, R. A.; Crespo-Hernández, C. E. On the origin of ultrafast nonradiative transitions in nitro-polycyclic aromatic hydrocarbons: Excited-state dynamics in 1-nitronaphthalene. *J. Chem. Phys.* **2009**, *131*, 224518.
- (100) Mai, S.; Pollum, M.; Martínez-Fernández, L.; Dunn, N.; Marquetand, P.; Corral, I.; Crespo-Hernández, C. E.; González, L. The origin of efficient triplet state population in sulfur-substituted nucleobases. *Nat. Commun.* **2016**, *7*, 13077.
- (101) Valverde, D.; Mai, S.; Canuto, S.; Borin, A. C.; González, L. Ultrafast Intersystem Crossing Dynamics of 6-Selenoguanine in Water. *JACS Au* **2022**, *2*, 1699–1711.
- (102) Zobel, J. P.; González, L. Nonadiabatic Dynamics Simulation Predict Intersystem Crossing in Nitroaromatic Molecules on a Picosecond Time Scale. *ChemPhotoChem.* **2019**, *3*, 833–845.
- (103) Greene, H. J. M.; Ghosh, D.; Sazanovich, I. V.; Phelps, R.; Curchod, B. F. E.; Orr-Ewing, A. J. Competing Nonadiabatic Relaxation Pathways for Near-UV Excited ortho-Nitrophenol in Aqueous Solution. *J. Phys. Chem. Lett.* **2024**, *15*, 9153–9159.
- (104) Marian, C. M. Understanding and Controlling Intersystem Crossing in Molecules. *Annu. Rev. Phys. Chem.* **2021**, 72, 617–640.
- (105) Smith, A. D.; Warne, E. M.; Bellshaw, D.; Horke, D. A.; Tudorovskya, M.; Springate, E.; Jones, A. J. H.; Cacho, C.; Chapman, R. T.; Kirrander, A.; Minns, R. S. Mapping the complete reaction path of a complex photochemical reaction. *Phys. Rev. Lett.* **2018**, *120*, No. 183003.
- (106) Bellshaw, D.; Minns, R. S.; Kirrander, A. Correspondence between electronic structure calculations and simulations: nonadiabatic dynamics in CS<sub>2</sub>. *Phys. Chem. Chem. Phys.* **2019**, 21, 14226–14237.
- (107) Cao, J.; Chen, D.-C. Disulfide bond photochemistry: the effects of higher excited states and different molecular geometries on disulfide bond cleavage. *Phys. Chem. Chem. Phys.* **2019**, 21, 4176–4183.
- (108) Mukherjee, S.; Fedorov, D. A.; Varganov, S. A. Modeling spin-crossover dynamics. *Annu. Rev. Phys. Chem.* **2021**, 72, 515–540.
- (109) Zhou, P.; Han, K. Unraveling the Detailed Mechanism of Excited-State Proton Transfer. Acc. Chem. Res. 2018, 51, 1681–1690.
- (110) Chen, C.-L.; Chen, Y.-T.; Demchenko, A. P.; Chou, P.-T. Amino proton donors in excited-state intramolecular proton-transfer reactions. *Nat. Rev. Chem.* **2018**, *2*, 131–143.
- (111) Demchenko, A. P. Proton transfer reactions: From photochemistry to biochemistry and bioenergetics. *BBA Adv.* **2023**, 3, No. 100085.
- (112) Holt, E. L.; Stavros, V. G. Applications of ultrafast spectroscopy to sunscreen development, from first principles to complex mixtures. *Int. Rev. Phys. Chem.* **2019**, *38*, 243–285.
- (113) Sedgwick, A. C.; Wu, L.; Han, H.-H.; Bull, S. D.; He, X.-P.; James, T. D.; Sessler, J. L.; Tang, B. Z.; Tian, H.; Yoon, J. Excited-state intramolecular proton-transfer (ESIPT) based fluorescence sensors and imaging agents. *Chem. Soc. Rev.* **2018**, *47*, 8842–8880.

- (114) Wu, C.-H.; Karas, L. J.; Ottosson, H.; Wu, J. I.-C. Excited-state proton transfer relieves antiaromaticity in molecules. *Proc. Natl. Acad. Sci. U.S.A.* **2019**, *116*, 20303–20308.
- (115) Joshi, H. C.; Antonov, L. Excited-State Intramolecular Proton Transfer: A Short Introductory Review. *Molecules* **2021**, *26*, 1475.
- (116) Hammes-Schiffer, S.; Stuchebrukhov, A. A. Theory of Coupled Electron and Proton Transfer Reactions. *Chem. Rev.* **2010**, *110*, 6939–6960.
- (117) Yu, Q.; Roy, S.; Hammes-Schiffer, S. Nonadiabatic Dynamics of Hydrogen Tunneling with Nuclear-Electronic Orbital Multistate Density Functional Theory. *J. Chem. Theory Comput.* **2022**, *18*, 7132–7141.
- (118) Hammes-Schiffer, S. Nuclear-electronic orbital methods: Foundations and prospects. *J. Chem. Phys.* **2021**, *155*, No. 030901.
- (119) Shushkov, P.; Li, R.; Tully, J. C. Ring polymer molecular dynamics with surface hopping. *J. Chem. Phys.* **2012**, *137*, 22A549.
- (120) Shakib, F. A.; Huo, P. Ring polymer surface hopping: Incorporating nuclear quantum effects into nonadiabatic molecular dynamics simulations. *J. Phys. Chem. Lett.* **2017**, *8*, 3073–3080.
- (121) González, L.; Lindh, R.Quantum Chemistry and Dynamics of Excited States: Methods and Applications; Wiley: 2021.
- (122) Light, J. C.; Hamilton, I. P.; Lill, J. V. Generalized discrete variable approximation in quantum mechanics. *J. Chem. Phys.* **1985**, *82*, 1400–1409.
- (123) Light, J. C.; Carrington, T., Jr. Discrete-Variable Representations and their Utilization. *Adv. Chem. Phys.* **2000**, *114*, 263–310.
- (124) Avila, G.; Carrington, T., Jr. Nonproduct quadrature grids for solving the vibrational Schrödinger equation. *J. Chem. Phys.* **2009**, *131*, 174103.
- (125) Meyer, H.-D.; Manthe, U.; Cederbaum, L. S. The multiconfigurational time-dependent Hartree approach. *Chem. Phys. Lett.* **1990**, *165*, 73–78.
- (126) Beck, M. H.; Jäckle, A.; Worth, G. A.; Meyer, H.-D. The multiconfiguration time-dependent Hartree (MCTDH) method: a highly efficient algorithm for propagating wavepackets. *Phys. Rep.* **2000**, 324, 1–105.
- (127) Wang, H.; Thoss, M. Multilayer formulation of the multiconfiguration time-dependent Hartree theory. *J. Chem. Phys.* **2003**, *119*, 1289–1299.
- (128) Manthe, U. A multilayer multiconfigurational time-dependent Hartree approach for quantum dynamics on general potential energy surfaces. *J. Chem. Phys.* **2008**, *128*, 164116.
- (129) Lode, A. U. J.; Lévêque, C.; Madsen, L. B.; Streltsov, A. I.; Alon, O. E. Colloquium: Multiconfigurational time-dependent Hartree approaches for indistinguishable particles. *Rev. Mod. Phys.* **2020**, 92, No. 011001.
- (130) Raab, A.; Burghardt, I.; Meyer, H.-D. The multiconfiguration time-dependent Hartree method generalized to the propagation of density operators. *J. Chem. Phys.* **1999**, *111*, 8759–8772.
- (131) Picconi, D.; Burghardt, I. Open system dynamics using Gaussian-based multiconfigurational time-dependent Hartree wavefunctions: Application to environment-modulated tunneling. *J. Chem. Phys.* **2019**, *150*, 224106.
- (132) Picconi, D. Dynamics of high-dimensional quantum systems coupled to a harmonic bath. General theory and implementation via multiconfigurational wave packets and truncated hierarchical equations for the mean-fields. *J. Chem. Phys.* **2024**, *161*, 164108.
- (133) Van Haeften, A.; Ash, C.; Worth, G. Propagating multi-dimensional density operators using the multi-layer- $\rho$  multi-configurational time-dependent Hartree method. *J. Chem. Phys.* **2023**, *159*, 194114.
- (134) Haegeman, J.; Lubich, C.; Oseledets, I.; Vandereycken, B.; Verstraete, F. Unifying time evolution and optimization with matrix product states. *Phys. Rev. B* **2016**, *94*, No. 165116.
- (135) Paeckel, S.; Köhler, T.; Swoboda, A.; Manmana, S. R.; Schollwöck, U.; Hubig, C. Time-evolution methods for matrix-product states. *Ann. Phys.* **2019**, *411*, No. 167998.

- (136) Larsson, H. R. A tensor network view of multilayer multiconfiguration time-dependent Hartree methods. *Mol. Phys.* **2024**, *122*, No. e2306881.
- (137) Ren, J.; Li, W.; Jiang, T.; Wang, Y.; Shuai, Z. Time-dependent density matrix renormalization group method for quantum dynamics in complex systems. *Wiley Interdiscip. Rev.: Comput. Mol. Sci.* **2022**, *12*, No. e1614.
- (138) Han, S.; Schröder, M.; Gatti, F.; Meyer, H.-D.; Lauvergnat, D.; Yarkony, D. R.; Guo, H. Representation of Diabatic Potential Energy Matrices for Multiconfiguration Time-Dependent Hartree Treatments of High-Dimensional Nonadiabatic Photodissociation Dynamics. *J. Chem. Theory Comput.* **2022**, *18*, 4627–4638.
- (139) Larsson, H. R.; Viel, A. 2500 vibronic eigenstates of the NO<sub>3</sub> radical. *Phys. Chem. Chem. Phys.* **2024**, *26*, 24506–24523.
- (140) Viel, A.; Eisfeld, W.; Neumann, S.; Domcke, W.; Manthe, U. Photoionization-induced dynamics of ammonia: Ab initio potential energy surfaces and time-dependent wave packet calculations for the ammonia cation. *J. Chem. Phys.* **2006**, *124*, 214306.
- (141) Ellerbrock, R.; Hoppe, H.; Manthe, U. A non-hierarchical multi-layer multi-configurational time-dependent hartree approach for quantum dynamics on general potential energy surfaces. *J. Chem. Phys.* **2024**, *160*, 224108.
- (142) Martínez, T. J.; Ben-Nun, M.; Levine, R. D. Multi-Electronic-State Molecular Dynamics: A Wave Function Approach with Applications. J. Phys. Chem. 1996, 100, 7884–7895.
- (143) Ben-Nun, M.; Quenneville, J.; Martínez, T. J. Ab Initio Multiple Spawning: Photochemistry from First Principles Quantum Molecular Dynamics. *J. Phys. Chem. A* **2000**, *104*, 5161–5175.
- (144) Mignolet, B.; Curchod, B. F. E. Excited-State Molecular Dynamics Triggered by Light Pulses—Ab Initio Multiple Spawning vs Trajectory Surface Hopping. *J. Phys. Chem. A* **2019**, *123*, 3582–3591.
- (145) Curchod, B. F. E.; Rauer, C.; Marquetand, P.; González, L.; Martínez, T. J. Communication: GAIMS—Generalized Ab Initio Multiple Spawning for both internal conversion and intersystem crossing processes. *J. Chem. Phys.* **2016**, *144*, 101102.
- (146) Curchod, B. F. E.; Glover, W. J.; Martínez, T. J. SSAIMS—Stochastic-Selection Ab Initio Multiple Spawning for Efficient Non-adiabatic Molecular Dynamics. *J. Phys. Chem. A* **2020**, *124*, 6133–6143.
- (147) Lassmann, Y.; Curchod, B. F. E. AIMSWISS—Ab initio multiple spawning with informed stochastic selections. *J. Chem. Phys.* **2021**, *154*, 211106.
- (148) Shalashilin, D. V.; Child, M. S. Multidimensional quantum propagation with the help of coupled coherent states. *J. Chem. Phys.* **2001**, *115*, 5367–5375.
- (149) Shalashilin, D. V. Quantum mechanics with the basis set guided by Ehrenfest trajectories: Theory and application to spin-boson model. *J. Chem. Phys.* **2009**, *130*, 244101.
- (150) Makhov, D. V.; Glover, W. J.; Martínez, T. J.; Shalashilin, D. V. Ab initio multiple cloning algorithm for quantum nonadiabatic molecular dynamics. *J. Chem. Phys.* **2014**, *141*, No. 054110.
- (151) Burghardt, I.; Meyer, H.-D.; Cederbaum, L. S. Approaches to the approximate treatment of complex molecular systems by the multiconfiguration time-dependent Hartree method. *J. Chem. Phys.* **1999**, *111*, 2927–2939.
- (152) Worth, G. A.; Burghardt, I. Full quantum mechanical molecular dynamics using Gaussian wavepackets. *Chem. Phys. Lett.* **2003**, 368, 502–508.
- (153) Burghardt, I.; Giri, K.; Worth, G. A. Multimode quantum dynamics using Gaussian wavepackets: The Gaussian-based multiconfiguration time-dependent Hartree (G-MCTDH) method applied to the absorption spectrum of pyrazine. *J. Chem. Phys.* **2008**, *129*, 174104.
- (154) Richings, G. W.; Worth, G. A. Multi-state non-adiabatic direct-dynamics on propagated diabatic potential energy surfaces. *Chem. Phys. Lett.* **2017**, *6*83, 606–612.
- (155) Tully, J. C.; Preston, R. K. Trajectory Surface Hopping Approach to Nonadiabatic Molecular Collisions: The Reaction of H<sup>+</sup> with D<sub>2</sub>. J. Chem. Phys. **1971**, 55, 562–572.

- (156) Hammes-Schiffer, S.; Tully, J. C. Proton transfer in solution: Molecular dynamics with quantum transitions. *J. Chem. Phys.* **1994**, 101, 4657–4667.
- (157) Zhu, C.; Nobusada, K.; Nakamura, H. New implementation of the trajectory surface hopping method with use of the Zhu–Nakamura theory. *J. Chem. Phys.* **2001**, *115*, 3031–3044.
- (158) Coker, D. F.; Xiao, L. Methods for molecular dynamics with nonadiabatic transitions. *J. Chem. Phys.* **1995**, *102*, 496–510.
- (159) Nielsen, S.; Kapral, R.; Ciccotti, G. Mixed quantum-classical surface hopping dynamics. *J. Chem. Phys.* **2000**, *112*, 6543–6553.
- (160) Richter, M.; Marquetand, P.; González-Vázquez, J.; Sola, I.; González, L. SHARC: ab Initio Molecular Dynamics with Surface Hopping in the Adiabatic Representation Including Arbitrary Couplings. J. Chem. Theory Comput. 2011, 7, 1253–1258.
- (161) Kelly, A.; Markland, T. E. Efficient and accurate surface hopping for long time nonadiabatic quantum dynamics. *J. Chem. Phys.* **2013**, 139, No. 014104.
- (162) Kapral, R. Surface hopping from the perspective of quantum–classical Liouville dynamics. *Chem. Phys.* **2016**, *481*, 77–83.
- (163) Belyaev, A. K.; Domcke, W.; Lasser, C.; Trigila, G. Nonadiabatic nuclear dynamics of the ammonia cation studied by surface hopping classical trajectory calculations. *J. Chem. Phys.* **2015**, *142*, 104307.
- (164) Araujo, L.; Lasser, C.; Schmidt, B. FSSH-2: fewest switches surface hopping with robust switching probability. *J. Chem. Theory Comput.* **2024**, 20, 3413–3419.
- (165) Belyaev, A. K.; Lasser, C.; Trigila, G. Landau–Zener type surface hopping algorithms. *J. Chem. Phys.* **2014**, *140*, 224108.
- (166) Hsiao, I.-Y.; Teranishi, Y.; Nakamura, H. Classically forbidden nonadiabatic transitions in multidimensional chemical dynamics. *Phys. Chem. Chem. Phys.* **2024**, *26*, 3795–3799.
- (167) Ishida, T.; Nanbu, S.; Nakamura, H. Clarification of nonadiabatic chemical dynamics by the Zhu-Nakamura theory of nonadiabatic transition: from tri-atomic systems to reactions in solutions. *Int. Rev. Phys. Chem.* **2017**, *36*, 229–285.
- (168) Bittner, E. R.; Rossky, P. J. Quantum decoherence in mixed quantum-classical systems: Nonadiabatic processes. *J. Chem. Phys.* **1995**, *103*, 8130–8143.
- (169) Subotnik, J. E.; Jain, A.; Landry, B.; Petit, A.; Ouyang, W.; Bellonzi, N. Understanding the Surface Hopping View of Electronic Transitions and Decoherence. *Annu. Rev. Phys. Chem.* **2016**, *67*, 387–417.
- (170) Granucci, G.; Persico, M. Critical appraisal of the fewest switches algorithm for surface hopping. *J. Chem. Phys.* **2007**, *126*, 134114.
- (171) Granucci, G.; Persico, M.; Zoccante, A. Including quantum decoherence in surface hopping. *J. Chem. Phys.* **2010**, *133*, 134111.
- (172) Persico, M.; Granucci, G.; Accomasso, D.The Quantum Decoherence Problem in Nonadiabatic Trajectory Methods. In *Comprehensive Computational Chemistry*, 1st ed.; Yáñez, M.; Boyd, R. J., Eds., Elsevier: Oxford, 2024; Vol. 4, pp 273–292.
- (173) Subotnik, J. E.; Shenvi, N. A new approach to decoherence and momentum rescaling in the surface hopping algorithm. *J. Chem. Phys.* **2011**, *134*, No. 024105.
- (174) Jain, A.; Alguire, E.; Subotnik, J. E. An Efficient, Augmented Surface Hopping Algorithm That Includes Decoherence for Use in Large-Scale Simulations. *J. Chem. Theory Comput.* **2016**, *12*, 5256–5268.
- (175) Jaeger, H. M.; Fischer, S.; Prezhdo, O. V. Decoherence-induced surface hopping. *J. Chem. Phys.* **2012**, *137*, 22A545.
- (176) Suchan, J.; Janoš, J.; Slavíček, P. Pragmatic Approach to Photodynamics: Mixed Landau—Zener Surface Hopping with Intersystem Crossing. *J. Chem. Theory Comput.* **2020**, *16*, 5809—5820.
- (177) Pieroni, C.; Agostini, F. Nonadiabatic Dynamics with Coupled Trajectories. *J. Chem. Theory Comput.* **2021**, *17*, 5969–5991.
- (178) Granucci, G.; Persico, M.; Toniolo, A. Direct semiclassical simulation of photochemical processes with semiempirical wave functions. *J. Chem. Phys.* **2001**, *114*, 10608–10615.
- (179) Wang, L.; Akimov, A.; Prezhdo, O. V. Recent Progress in Surface Hopping: 2011–2015. *J. Phys. Chem. Lett.* **2016**, *7*, 2100–2112.

- (180) Toldo, J. M.; Mattos, R. S.; Pinheiro, M., Jr.; Mukherjee, S.; Barbatti, M. Recommendations for Velocity Adjustment in Surface Hopping. *J. Chem. Theory Comput.* **2024**, *20*, 614–624.
- (181) Plasser, F.; Mai, S.; Fumanal, M.; Gindensperger, E.; Daniel, C.; González, L. Strong influence of decoherence corrections and momentum rescaling in surface hopping dynamics of transition metal complexes. *J. Chem. Theory Comput.* **2019**, *15*, 5031–5045.
- (182) Nelson, T.; Fernandez-Alberti, S.; Roitberg, A. E.; Tretiak, S. Artifacts due to trivial unavoided crossings in the modeling of photoinduced energy transfer dynamics in extended conjugated molecules. *Chem. Phys. Lett.* **2013**, *590*, 208–213.
- (183) Wang, L.; Prezhdo, O. V. A Simple Solution to the Trivial Crossing Problem in Surface Hopping. *J. Phys. Chem. Lett.* **2014**, *5*, 713–719
- (184) Abedi, A.; Maitra, N. T.; Gross, E. K. U. Exact Factorization of the Time-Dependent Electron-Nuclear Wave Function. *Phys. Rev. Lett.* **2010**, *105*, No. 123002.
- (185) Ibele, L. M.; Pieroni, C.; Talotta, F.; Curchod, B. F. E.; Lauvergnat, D.; Agostini, F.Exact Factorization of the Electron-Nuclear Wavefunction: Fundamentals and Algorithms. In *Comprehensive Computational Chemistry*, 1st ed.; Yáñez, M.; Boyd, R. J., Eds.; Elsevier: Oxford, 2024; Vol. 4, pp 188–211.
- (186) Pieroni, C.; Sangiogo Gil, E.; Ibele, L. M.; Persico, M.; Granucci, G.; Agostini, F. Investigating the Photodynamics of trans-Azobenzene with Coupled Trajectories. *J. Chem. Theory Comput.* **2024**, 20, 580–596
- (187) Xie, R.; Shi, Z.; Wang, L. Coupled Trajectory Surface Hopping with Sign Consistency. *J. Chem. Phys.* **2025**, *162*, 164103.
- (188) Ibele, L. M.; Sangiogo Gil, E.; Schürger, P.; Agostini, F.A coupled-trajectory approach for decoherence, frustrated hops and internal consistency in surface hopping. 2024, DOI: 10.48550/arXiv.2412.04958 (accessed Jun 2, 2025).
- (189) Ha, J.-K.; Lee, I. S.; Min, S. K. Surface Hopping Dynamics beyond Nonadiabatic Couplings for Quantum Coherence. *J. Phys. Chem. Lett.* **2018**, *9*, 1097–1104.
- (190) Ha, J.-K.; Min, S. K. Independent trajectory mixed quantum-classical approaches based on the exact factorization. *J. Chem. Phys.* **2022**, *156*, 174109.
- (191) Han, D.; Akimov, A. V. Nonadiabatic Dynamics with Exact Factorization: Implementation and Assessment. *J. Chem. Theory Comput.* **2024**, 20, 5022–5042.
- (192) Dupuy, L.; Rikus, A.; Maitra, N. T. Exact-Factorization-Based Surface Hopping without Velocity Adjustment. *J. Phys. Chem. Lett.* **2024**, *15*, 2643–2649.
- (193) Craig, C. F.; Duncan, W. R.; Prezhdo, O. V. Trajectory Surface Hopping in the Time-Dependent Kohn-Sham Approach for Electron-Nuclear Dynamics. *Phys. Rev. Lett.* **2005**, *95*, No. 163001.
- (194) Tempelaar, R.; Reichman, D. R. Generalization of fewest-switches surface hopping for coherences. *J. Chem. Phys.* **2018**, *148*, 102309.
- (195) Martens, C. C. Surface Hopping without Momentum Jumps: A Quantum-Trajectory-Based Approach to Nonadiabatic Dynamics. *J. Phys. Chem. A* **2019**, *123*, 1110–1128.
- (196) Martens, C. C. Surface Hopping by Consensus. J. Phys. Chem. Lett. 2016, 7, 2610–2615.
- (197) Spencer, J.; Gajdos, F.; Blumberger, J. FOB-SH: Fragment orbital-based surface hopping for charge carrier transport in organic and biological molecules and materials. *J. Chem. Phys.* **2016**, *145*, No. 064102.
- (198) Kossoski, F.; Barbatti, M. Nonadiabatic dynamics in multidimensional complex potential energy surfaces. *Chem. Sci.* **2020**, *11*, 9827–9835
- (199) Tao, Z.; Yu, Q.; Roy, S.; Hammes-Schiffer, S. Direct Dynamics with Nuclear–Electronic Orbital Density Functional Theory. *Acc. Chem. Res.* **2021**, *54*, 4131–4141.
- (200) Mannouch, J. R.; Richardson, J. O. A mapping approach to surface hopping. *J. Chem. Phys.* **2023**, *158*, 104111.
- (201) Runeson, J. E.; Manolopoulos, D. E. A multi-state mapping approach to surface hopping. *J. Chem. Phys.* **2023**, *159*, No. 094115.

- (202) Lawrence, J. E.; Mannouch, J. R.; Richardson, J. O. A size-consistent multi-state mapping approach to surface hopping. *J. Chem. Phys.* **2024**, *160*, 244112.
- (203) McLachlan, A. D. A variational solution of the time-dependent schrodinger equation. *Mol. Phys.* **1964**, *8*, 39–44.
- (204) Jenkins, A. J.; Spinlove, K. E.; Vacher, M.; Worth, G. A.; Robb, M. A. The Ehrenfest method with fully quantum nuclear motion (QuEh): Application to charge migration in radical cations. *J. Chem. Phys.* **2018**, *149*, No. 094108.
- (205) Freixas, V. M.; Fernandez-Alberti, S.; Makhov, D. V.; Tretiak, S.; Shalashilin, D. An ab initio multiple cloning approach for the simulation of photoinduced dynamics in conjugated molecules. *Phys. Chem. Chem. Phys.* **2018**, 20, 17762–17772.
- (206) Cheng, S. C.; Zhu, C.; Liang, K. K.; Lin, S. H.; Truhlar, D. G. Algorithmic decoherence time for decay-of-mixing non—Born—Oppenheimer dynamics. *J. Chem. Phys.* **2008**, *129*, No. 024112.
- (207) Zhu, C.; Nangia, S.; Jasper, A. W.; Truhlar, D. G. Coherent switching with decay of mixing: an improved treatment of electronic coherence for non-Born—Oppenheimer trajectories. *J. Chem. Phys.* **2004**, *121*, 7658—7670.
- (208) Zhu, C.; Jasper, A. W.; Truhlar, D. G. Non-Born-Oppenheimer Liouville-von Neumann Dynamics. Evolution of a Subsystem Controlled by Linear and Population-Driven Decay of Mixing with Decoherent and Coherent Switching. *J. Chem. Theory Comput.* **2005**, *1*, 527–540.
- (209) Miller, W. H. The Semiclassical Initial Value Representation: A Potentially Practical Way for Adding Quantum Effects to Classical Molecular Dynamics Simulations. *J. Phys. Chem. A* **2001**, *105*, 2942–2955
- (210) Sun, X.; Miller, W. H. Semiclassical initial value representation for electronically nonadiabatic molecular dynamics. *J. Chem. Phys.* **1997**, *106*, 6346–6353.
- (211) Sun, X.; Wang, H.; Miller, W. H. Semiclassical theory of electronically nonadiabatic dynamics: Results of a linearized approximation to the initial value representation. *J. Chem. Phys.* **1998**, *109*, 7064–7074.
- (212) Cotton, S. J.; Miller, W. H. Symmetrical windowing for quantum states in quasi-classical trajectory simulations: Application to electronically non-adiabatic processes. *J. Chem. Phys.* **2013**, *139*, 234112.
- (213) Cotton, S. J.; Miller, W. H. Symmetrical windowing for quantum states in quasi-classical trajectory simulations. *J. Phys. Chem. A* **2013**, *117*, 7190–7194.
- (214) Runeson, J. E.; Richardson, J. O. Spin-mapping approach for nonadiabatic molecular dynamics. *J. Chem. Phys.* **2019**, *151*, No. 044119.
- (215) Runeson, J. E.; Richardson, J. O. Generalized spin mapping for quantum-classical dynamics. *J. Chem. Phys.* **2020**, *152*, No. 084110.
- (216) Saller, M. A. C.; Kelly, A.; Richardson, J. O. On the identity of the identity operator in nonadiabatic linearized semiclassical dynamics. *J. Chem. Phys.* **2019**, *150*, No. 071101.
- (217) Saller, M. A. C.; Kelly, A.; Richardson, J. O. Improved population operators for multi-state nonadiabatic dynamics with the mixed quantum-classical mapping approach. *Faraday Discuss.* **2020**, 221, 150–167.
- (218) Amati, G.; Saller, M. A. C.; Kelly, A.; Richardson, J. O. Quasiclassical approaches to the generalized quantum master equation. *J. Chem. Phys.* **2022**, *157*, 234103.
- (219) Mannouch, J. R.; Richardson, J. O. A partially linearized spin-mapping approach for nonadiabatic dynamics. I. Derivation of the theory. *J. Chem. Phys.* **2020**, *153*, 194109.
- (220) Mannouch, J. R.; Richardson, J. O. A partially linearized spin-mapping approach for nonadiabatic dynamics. II. Analysis and comparison with related approaches. *J. Chem. Phys.* **2020**, *153*, 194110. (221) Hu, D.; Xie, Y.; Peng, J.; Lan, Z. On-the-Fly Symmetrical Quasi-Classical Dynamics with Meyer—Miller Mapping Hamiltonian for the Treatment of Nonadiabatic Dynamics at Conical Intersections. *J. Chem. Theory Comput.* **2021**, *17*, 3267—3279.

- (222) Meyer, H.; Miller, W. H. A classical analog for electronic degrees of freedom in nonadiabatic collision processes. *J. Chem. Phys.* **1979**, *70*, 3214–3223.
- (223) Stock, G.; Thoss, M. Classical description of nonadiabatic quantum dynamics. *Adv. Chem. Phys.* **2005**, *131*, 243–375.
- (224) Liu, J.; He, X.; Wu, B. Unified formulation of phase space mapping approaches for nonadiabatic quantum dynamics. *Acc. Chem. Res.* **2021**, 23, 4215–4228.
- (225) Xie, Y.; Zheng, J.; Lan, Z. Performance evaluation of the symmetrical quasi-classical dynamics method based on Meyer-Miller mapping Hamiltonian in the treatment of site-exciton models. *J. Chem. Phys.* **2018**, *149*, 174105.
- (226) Gao, X.; Saller, M. A. C.; Liu, Y.; Kelly, A.; Richardson, J. O.; Geva, E. Benchmarking Quasiclassical Mapping Hamiltonian Methods for Simulating Electronically Nonadiabatic Molecular Dynamics. *J. Chem. Theory Comput.* **2020**, *16*, 2883–2895.
- (227) Zhou, W.; Mandal, A.; Huo, P. Quasi-diabatic scheme for nonadiabatic on-the-fly simulations. *J. Phys. Chem. Lett.* **2019**, *10*, 7062–7070.
- (228) Tang, D.; Fang, W.-H.; Shen, L.; Cui, G. Combining Meyer-Miller Hamiltonian with electronic structure methods for on-the-fly nonadiabatic dynamics simulations: Implementation and application. *Phys. Chem. Phys.* **2019**, *21*, 17109–17117.
- (229) Miller, W. H. Electronically Nonadiabatic Dynamics via Semiclassical Initial Value Methods. *J. Phys. Chem. A* **2009**, *113*, 1405–1415.
- (230) Huo, P. F.; Coker, D. F. Consistent schemes for non-adiabatic dynamics derived from partial linearized density matrix propagation. *J. Chem. Phys.* **2012**, *137*, 22A535.
- (231) Kim, H.; Nassimi, A.; Kapral, R. Quantum-classical Liouville dynamics in the mapping basis. *J. Chem. Phys.* **2008**, *129*, No. 084102.
- (232) Min, S. K.; Agostini, F.; Gross, E. K. U. Coupled-Trajectory Quantum-Classical Approach to Electronic Decoherence in Non-adiabatic Processes. *Phys. Rev. Lett.* **2015**, *115*, No. 073001.
- (233) Villaseco Arribas, E.; Maitra, N. T. Energy-conserving coupled trajectory mixed quantum-classical dynamics. *J. Chem. Phys.* **2023**, *158*, 161105.
- (234) Dines, A.; Ellis, M.; Blumberger, J. Stabilized coupled trajectory mixed quantum-classical algorithm with improved energy conservation: CTMQC-EDI. *J. Chem. Phys.* **2023**, *159*, 234118.
- (235) Villaseco Arribas, E.; Ibele, L. M.; Lauvergnat, D.; Maitra, N. T.; Agostini, F. Significance of Energy Conservation in Coupled-Trajectory Approaches to Nonadiabatic Dynamics. *J. Chem. Theory Comput.* **2023**, 19, 7787–7800.
- (236) Bonafé, F. P.; Aradi, B.; Hourahine, B.; Medrano, C. R.; Hernández, F. J.; Frauenheim, T.; Sánchez, C. G. A Real-Time Time-Dependent Density Functional Tight-Binding Implementation for Semiclassical Excited State Electron—Nuclear Dynamics and Pump—Probe Spectroscopy Simulations. *J. Chem. Theory Comput.* **2020**, *16*, 4454—4469.
- (237) Hernández, F. J.; Bonafé, F. P.; Aradi, B.; Frauenheim, T.; Sánchez, C. G. Simulation of Impulsive Vibrational Spectroscopy. *J. Phys. Chem. A* **2019**, *123*, 2065–2072.
- (238) Kapral, R.; Ciccotti, G. Mixed quantum-classical dynamics. *J. Chem. Phys.* **1999**, *110*, 8919–8929.
- (239) Kapral, R. Progress in the Theory of Mixed Quantum-Classical Dynamics. *Annu. Rev. Phys. Chem.* **2006**, *57*, 129–157.
- (240) Hanna, G.; Kapral, R. Quantum-classical Liouville dynamics of nonadiabatic proton transfer. *J. Chem. Phys.* **2005**, *122*, 244505.
- (241) Shakib, F.; Hanna, G. Mixed quantum-classical Liouville approach for calculating proton-coupled electron-transfer rate constants. *J. Chem. Theory Comput.* **2016**, *12*, 3020.
- (242) Grunwald, R.; Kelly, A.; Kapral, R.Quantum Dynamics in Almost Classical Environments. In *Energy Transfer Dynamics in Biomaterial Systems*; Burghardt, I.; May, V.; Micha, D. A.; Bittner, E. R., Eds.; Springer: 2009; pp 383–413.
- (243) Kelly, A.; Van Zon, R.; Schofield, J.; Kapral, R. Mapping quantum-classical Liouville equation: Projectors and trajectories. *J. Chem. Phys.* **2012**, *136*, No. 084101.

- (244) Hsieh, C.-Y.; Kapral, R. Nonadiabatic dynamics in open quantum-classical systems: Forward-backward trajectory solution. *J. Chem. Phys.* **2012**, *137*, 22A507.
- (245) Kelly, A.; Montoya-Castillo, A.; Wang, L.; Markland, T. E. Generalized quantum master equations in and out of equilibrium: When can one win? *J. Chem. Phys.* **2016**, *144*, 184105.
- (246) Dunkel, E. R.; Bonella, S.; Coker, D. F. Iterative linearized approach to nonadiabatic dynamics. *J. Chem. Phys.* **2008**, *129*, 114106.
- (247) Bonella, S.; Coker, D. F. LAND-map, a linearized approach to nonadiabatic dynamics using the mapping formalism. *J. Chem. Phys.* **2005**, *122*, 194102.
- (248) Huo, P.; Coker, D. F. Communication: Partial linearized density matrix dynamics for dissipative, non-adiabatic quantum evolution. *J. Chem. Phys.* **2011**, *135*, 201101.
- (249) Makri, N.; Makarov, D. E. Tensor propagator for iterative quantum time evolution of reduced density matrices. I. Theory. *J. Chem. Phys.* **1995**, *102*, 4600–4610.
- (250) Makri, N.; Thompson, K. Semiclassical influence functionals for quantum systems in anharmonic environments. *Chem. Phys. Lett.* **1998**, 291, 101–109.
- (251) Lambert, R.; Makri, N. Quantum-classical path integral. I. Classical memory and weak quantum nonlocality. *J. Chem. Phys.* **2012**, 137, 22A552.
- (252) Makri, N. Small Matrix Path Integral with Extended Memory. *J. Chem. Theory Comput.* **2021**, *17*, 1–6.
- (253) Keldysh, L. V.Diagram technique for nonequilibrium processes. In *Selected Papers of Leonid V Keldysh*; Sadovskii, M. V., Ed.; World Scientific: 2024; pp 47–55.
- (254) Kadanoff, L. P.; Baym, G. Quantum Statistical Mechanics: Green's Function Methods in Equilibrium and Nonequilibrium Problems; CRC Press: 2018.
- (255) Cohen, G.; Galperin, M. Green's function methods for single molecule junctions. *J. Chem. Phys.* **2020**, *152*, No. 090901.
- (256) Nanni, L. Dynamics of proton tunneling in Hydrogen-Bonded systems through Green's function formalism. *J. Nat. Scien. & Math. Res.* **2024**, *10*, 22–34.
- (257) Craig, I. R.; Manolopoulos, D. E. Quantum statistics and classical mechanics: Real time correlation functions from ring polymer molecular dynamics. *J. Chem. Phys.* **2004**, *121*, 3368.
- (258) London, N.; Bu, S.; Johnson, B.; Ananth, N. Mean-field ring polymer rates using a population dividing surface. *J. Phys. Chem. A* **2024**, 128, 5730–5739.
- (259) Ananth, N. Mapping variable ring polymer molecular dynamics: A path-integral based method for nonadiabatic processes. *J. Chem. Phys.* **2013**, *139*, 124102.
- (260) Menzeleev, A. R.; Ananth, N.; Miller, T. F., III Direct simulation of electron transfer using ring polymer molecular dynamics: Comparison with semiclassical instanton theory and exact quantum method. *J. Chem. Phys.* **2011**, *135*, No. 074106.
- (261) Chowdhury, S. N.; Huo, P. Coherent state mapping ring polymer molecular dynamics for non-adiabatic quantum propagations. *J. Chem. Phys.* **2017**, *147*, 214109.
- (262) Xu, J.; Zhou, R.; Blum, V.; Li, T. E.; Hammes-Schiffer, S.; Kanai, Y. First-Principles Approach for Coupled Quantum Dynamics of Electrons and Protons in Heterogeneous Systems. *Phys. Rev. Lett.* **2023**, 131, No. 238002.
- (263) Xu, J.; Zhou, R.; Li, T. E.; Hammes-Schiffer, S.; Kanai, Y. Lagrangian formulation of nuclear—electronic orbital Ehrenfest dynamics with real-time TDDFT for extended periodic systems. *J. Chem. Phys.* **2024**, *161*, 194109.
- (264) Tanimura, Y.; Kubo, R. Time Evolution of a Quantum System in Contact with a Nearly Gaussian-Markoffian Noise Bath. *J. Phys. Soc. Jpn.* **1989**, *58*, 101–114.
- (265) Tanimura, Y. Numerically "exact" approach to open quantum dynamics: The hierarchical equations of motion (HEOM). *J. Chem. Phys.* **2020**, *153*, No. 020901.
- (266) Ke, Y. Tree tensor network state approach for solving hierarchical equations of motion. *J. Chem. Phys.* **2023**, 158, 211102.

- (267) Mangaud, E.; Jaouadi, A.; Chin, A.; Desouter-Lecomte, M. Survey of the hierarchical equations of motion in tensor-train format for non-Markovian quantum dynamics. *Eur. Phys. J.: Spec. Top.* **2023**, 232, 1847–1869.
- (268) Prior, J.; Chin, A. W.; Huelga, S. F.; Plenio, M. B. Efficient Simulation of Strong System-Environment Interactions. *Phys. Rev. Lett.* **2010**, *105*, No. 050404.
- (269) Tamascelli, D.; Smirne, A.; Lim, J.; Huelga, S. F.; Plenio, M. B. Efficient Simulation of Finite-Temperature Open Quantum Systems. *Phys. Rev. Lett.* **2019**, *123*, No. 090402.
- (270) Mukherjee, S.; Barbatti, M. A Hessian-Free Method to Prevent Zero-Point Energy Leakage in Classical Trajectories. *J. Chem. Theory Comput.* **2022**, *18*, 4109–4116.
- (271) Shu, Y.; Truhlar, D. G. Improved Local-Mode Zero-Point-Energy Conservation Scheme for Quasiclassical Trajectories. *J. Phys. Chem. A* **2024**, *128*, 3625–3634.
- (272) MacDonell, R. J.; Dickerson, C. E.; Birch, C. J. T.; Kumar, A.; Edmunds, C. L.; Biercuk, M. J.; Hempel, C.; Kassal, I. Analog quantum simulation of chemical dynamics. *Chem. Sci.* **2021**, *12*, 9794–9805.
- (273) Valahu, C. H.; Olaya-Agudelo, V. C.; MacDonell, R. J.; Navickas, T.; Rao, A. D.; Millican, M. J.; Pérez-Sánchez, J. B.; Yuen-Zhou, J.; Biercuk, M. J.; Hempel, C.; et al. Direct observation of geometric-phase interference in dynamics around a conical intersection. *Nat. Chem.* **2023**, *15*, 1503–1508.
- (274) Sun, K.; Kang, M.; Nuomin, H.; Schwartz, G.; Beratan, D. N.; Brown, K. R.; Kim, J. Quantum simulation of spin-boson models with structured bath. *Nat. Commun.* **2025**, *16*, No. 4042.
- (275) Navickas, T.; MacDonell, R. J.; Valahu, C. H.; Olaya-Agudelo, V. C.; Scuccimarra, F.; Millican, M. J.; Matsos, V. G.; Nourse, H. L.; Rao, A. D. Experimental Quantum Simulation of Chemical Dynamics. *J. Am. Chem. Soc.* **2025**, 147 (27), 23566–23573.
- (276) Kassal, I.; Jordan, S. P.; Love, P. J.; Mohseni, M.; Aspuru-Guzik, A. Polynomial-time quantum algorithm for the simulation of chemical dynamics. *Proc. Natl. Acad. Sci. U.S.A.* **2008**, *105*, 18681–18686.
- (277) Childs, A. M.; Leng, J.; Li, T.; Liu, J.-P.; Zhang, C. Quantum simulation of real-space dynamics. *Quantum* **2022**, *6*, 860.
- (278) Rubin, N. C.; Berry, D. W.; Kononov, A.; Malone, F. D.; Khattar, T.; White, A.; Lee, J.; Neven, H.; Babbush, R.; Baczewski, A. D. Quantum computation of stopping power for inertial fusion target design. *Proc. Natl. Acad. Sci. U. S. A.* **2024**, *121*, No. e2317772121.
- (279) Motlagh, D.; Lang, R. A.; Campos-Gonzalez-Angulo, J. A.; Zeng, T.; Aspuru-Guzik, A.; Arrazola, J. M.Quantum Algorithm for Vibronic Dynamics: Case Study on Singlet Fission Solar Cell Design. 2024. DOI: 10.48550/arXiv.2411.13669 (accessed Jun 2, 2025).
- (280) Kovyrshin, A.; Skogh, M.; Tornberg, L.; Broo, A.; Mensa, S.; Sahin, E.; Symons, B. C. B.; Crain, J.; Tavernelli, I. Nonadiabatic Nuclear–Electron Dynamics: A Quantum Computing Approach. *J. Phys. Chem. Lett.* **2023**, *14*, 7065–7072.
- (281) Ollitrault, P. J.; Mazzola, G.; Tavernelli, I. Nonadiabatic molecular quantum dynamics with quantum computers. *Phys. Rev. Lett.* **2020**, *125*, No. 260511.
- (282) Gandon, A.; Baiardi, A.; Ollitrault, P.; Tavernelli, I. Non-adiabatic Molecular Dynamics with Fermionic Subspace-Expansion Algorithms on Quantum Computers. *J. Chem. Theory Comput.* **2024**, 20, 5951–5963.
- (283) Tuna, D.; Lefrancois, D.; Wolański, Ł.; Gozem, S.; Schapiro, I.; Andruniów, T.; Dreuw, A.; Olivucci, M. Assessment of Approximate Coupled-Cluster and Algebraic-Diagrammatic-Construction Methods for Ground- and Excited-State Reaction Paths and the Conical-Intersection Seam of a Retinal-Chromophore Model. J. Chem. Theory Comput. 2015, 11, 5758–5781.
- (284) Papineau, T. V.; Jacquemin, D.; Vacher, M. Which Electronic Structure Method to Choose in Trajectory Surface Hopping Dynamics Simulations? Azomethane as a Case Study. *J. Phys. Chem. Lett.* **2024**, *15*, 636–643.
- (285) Ibele, L.; Memhood, A.; Levine, B. G.; Avagliano, D. Ab Initio Multiple Spawning Nonadiabatic Dynamics with Different CASPT2 Flavors: A Fully Open-Source PySpawn/OpenMolcas Interface. *J. Chem. Theory Comput.* **2024**, 20, 8140–8151.

- (286) Janoš, J.; Slavíček, P. What Controls the Quality of Photodynamical Simulations? Electronic Structure Versus Nonadiabatic Algorithm. *J. Chem. Theory Comput.* **2023**, *19*, 8273–8284.
- (287) Mukherjee, S.; Mattos, R. S.; Toldo, J. M.; Lischka, H.; Barbatti, M. Prediction challenge: Simulating Rydberg photoexcited cyclobutanone with surface hopping dynamics based on different electronic structure methods. *J. Chem. Phys.* **2024**, *160*, 154306.
- (288) Zobel, J. P.; Kruse, A.; Baig, O.; Lochbrunner, S.; Bokarev, S. I.; Kühn, O.; González, L.; Bokareva, O. S. Can range-separated functionals be optimally tuned to predict spectra and excited state dynamics in photoactive iron complexes? *Chem. Sci.* **2023**, *14*, 1491–1502.
- (289) Gozem, S.; Melaccio, F.; Valentini, A.; Filatov, M.; Huix-Rotllant, M.; Ferré, N.; Frutos, L. M.; Angeli, C.; Krylov, A. I.; Granovsky, A. A.; et al. Shape of Multireference, Equation-of-Motion Coupled-Cluster, and Density Functional Theory Potential Energy Surfaces at a Conical Intersection. *J. Chem. Theory Comput.* **2014**, *10*, 3074–3084.
- (290) Cooper, J. C.; Brown, C. Y. Z.; Kára, J.; Kirrander, A. Photoexcited dynamics of the valence states of norbornadiene. *J. Chem. Phys.* **2025**, *162*, No. 094102.
- (291) Cooper, J. C.; Kirrander, A. Electronic structure of norbornadiene and quadricyclane. *Phys. Chem. Chem. Phys.* **2025**, 27, 3089–3101.
- (292) Brady, R. P.; Drury, C.; Yurchenko, S. N.; Tennyson, J. Numerical Equivalence of Diabatic and Adiabatic Representations in Diatomic Molecules. *J. Chem. Theory Comput.* **2024**, *20*, 2127–2139.
- (293) Matsika, S. Electronic Structure Methods for the Description of Nonadiabatic Effects and Conical Intersections. *Chem. Rev.* **2021**, *121*, 9407–9449.
- (294) Szalay, P. G.; Müller, T.; Gidofalvi, G.; Lischka, H.; Shepard, R. Multiconfiguration Self-Consistent Field and Multireference Configuration Interaction Methods and Applications. *Chem. Rev.* **2012**, *112*, 108–181.
- (295) González, L.; Escudero, D.; Serrano-Andrés, L. Progress and Challenges in the Calculation of Electronic Excited States. *ChemPhysChem* **2012**, *13*, 28–51.
- (296) Park, J. W.; Al-Saadon, R.; MacLeod, M. K.; Shiozaki, T.; Vlaisavljevich, B. Multireference Electron Correlation Methods: Journeys along Potential Energy Surfaces. *Chem. Rev.* **2020**, *120*, 5878–5909.
- (297) Snyder, J. W., Jr.; Parrish, R. M.; Martínez, T. J. α-CASSCF: An Efficient, Empirical Correction for SA-CASSCF To Closely Approximate MS-CASPT2 Potential Energy Surfaces. J. Phys. Chem. Lett. 2017, 8. 2432–2437.
- (298) Frutos, L. M.; Andruniów, T.; Santoro, F.; Ferré, N.; Olivucci, M. Tracking the excited-state time evolution of the visual pigment with multiconfigurational quantum chemistry. *Proc. Natl. Acad. Sci. U.S.A.* **2007**, *104*, 7764–7769.
- (299) Wolf, T. J. A.; Sanchez, D. M.; Yang, J.; Parrish, R. M.; Nunes, J. P. F.; Centurion, M.; Coffee, R.; Cryan, J. P.; Gühr, M.; Hegazy, K.; et al. The photochemical ring-opening of 1,3-cyclohexadiene imaged by ultrafast electron diffraction. *Nat. Chem.* **2019**, *11*, 504–509.
- (300) List, N. H.; Jones, C. M.; Martínez, T. J. Internal conversion of the anionic GFP chromophore: in and out of the I-twisted  $S_1/S_0$  conical intersection seam. *Chem. Sci.* **2022**, *13*, 373–385.
- (301) Slavíček, P.; Martínez, T. J. Ab initio floating occupation molecular orbital-complete active space configuration interaction: An efficient approximation to CASSCF. J. Chem. Phys. 2010, 132, 234102.
- (302) Hollas, D.; Šištík, L.; Hohenstein, E. G.; Martínez, T. J.; Slavíček, P. Nonadiabatic Ab Initio Molecular Dynamics with the Floating Occupation Molecular Orbital-Complete Active Space Configuration Interaction Method. *J. Chem. Theory Comput.* **2018**, 14, 339–350.
- (303) Ullrich, C. A. Time-Dependent Density-Functional Theory: Concepts and Applications; Oxford University Press: 2011.
- (304) Tozer, D. J.; Handy, N. C. On the determination of excitation energies using density functional theory. *Phys. Chem. Chem. Phys.* **2000**, 2, 2117–2121.

- (305) Levine, B. G.; Ko, C.; Quenneville, J.; Martínez, T. J. Conical intersections and double excitations in time-dependent density functional theory. *Mol. Phys.* **2006**, *104*, 1039–1051.
- (306) Maitra, N. T.; Zhang, F.; Cave, R. J.; Burke, K. Double excitations within time-dependent density functional theory linear response. *J. Chem. Phys.* **2004**, *120*, 5932–5937.
- (307) Dreuw, A.; Head-Gordon, M. Failure of Time-Dependent Density Functional Theory for Long-Range Charge-Transfer Excited States: The Zincbacteriochlorin-Bacteriochlorin and Bacteriochlorophyll-Spheroidene Complexes. J. Am. Chem. Soc. 2004, 126, 4007—4016
- (308) Hellgren, M.; Gross, E. K. U. Discontinuities of the exchange-correlation kernel and charge-transfer excitations in time-dependent density-functional theory. *Phys. Rev. A* **2012**, *85*, No. 022514.
- (309) Thiele, M.; Kümmel, S. Frequency Dependence of the Exact Exchange-Correlation Kernel of Time-Dependent Density-Functional Theory. *Phys. Rev. Lett.* **2014**, *112*, No. 083001.
- (310) Cave, R. J.; Zhang, F.; Maitra, N. T.; Burke, K. A dressed TDDFT treatment of the 2<sup>1</sup>A<sub>g</sub> states of butadiene and hexatriene. *Chem. Phys. Lett.* **2004**, 389, 39–42.
- (311) Elliott, P.; Goldson, S.; Canahui, C.; Maitra, N. T. Perspectives on double-excitations in TDDFT. *Chem. Phys.* **2011**, *391*, 110–119.
- (312) Taylor, J. T.; Tozer, D. J.; Curchod, B. F. E. On the description of conical intersections between excited electronic states with LR-TDDFT and ADC(2). *J. Chem. Phys.* **2023**, *159*, 214115.
- (313) Taylor, J. T.; Tozer, D. J.; Curchod, B. F. E. On the Topological Phase around Conical Intersections with Tamm—Dancoff Linear-Response Time-Dependent Density Functional Theory. *J. Phys. Chem.* A **2024**, *128*, 5314—5320.
- (314) Maitra, N. T. Perspective: Fundamental aspects of time-dependent density functional theory. J. Chem. Phys. 2016, 144, 220901.
- (315) Wiggins, P.; Williams, J. A. G.; Tozer, D. J. Excited state surfaces in density functional theory: a new twist on an old problem. *J. Chem. Phys.* **2009**, *131*, No. 091101.
- (316) Ferchichi, O.; Derbel, N.; Cours, T.; Alijah, A. Dichlorine peroxide (ClOOCl), chloryl chloride (ClCl(O)O) and chlorine chlorite (ClOClO): very accurate ab initio structures and actinic degradation. *Phys. Chem. Chem. Phys.* **2020**, 22, 4059–4071.
- (317) Chebbi, W.; Derbel, N.; Alijah, A.; Cours, T. UV-spectrum and photodecomposition of peroxynitrous acid in the troposphere. *Phys. Chem. Chem. Phys.* **2023**, *26*, 123–129.
- (318) Lefrancois, D.; Tuna, D.; Martínez, T. J.; Dreuw, A. The Spin-Flip Variant of the Algebraic-Diagrammatic Construction Yields the Correct Topology of  $S_1/S_0$  Conical Intersections. *J. Chem. Theory Comput.* **2017**, *13*, 4436–4441.
- (319) Shao, Y.; Head-Gordon, M.; Krylov, A. I. The spin—flip approach within time-dependent density functional theory: Theory and applications to diradicals. *J. Chem. Phys.* **2003**, *118*, 4807–4818.
- (320) Zhang, X.; Herbert, J. M. Spin-flip, tensor equation-of-motion configuration interaction with a density-functional correction: a spin-complete method for exploring excited-state potential energy surfaces. *J. Chem. Phys.* **2015**, *143*, 234107.
- (321) Li, Z.; Liu, W. Spin-adapted open-shell random phase approximation and time-dependent density functional theory. I. Theory. J. Chem. Phys. 2010, 133, No. 064106.
- (322) Li, Z.; Liu, W.; Zhang, Y.; Suo, B. Spin-adapted open-shell time-dependent density functional theory. II. Theory and pilot application. *J. Chem. Phys.* **2011**, *134*, 134101.
- (323) Li, Z.; Liu, W. Spin-adapted open-shell time-dependent density functional theory. III. An even better and simpler formulation. *J. Chem. Phys.* **2011**, 135, 194106.
- (324) Filatov, M. Spin-restricted ensemble-referenced Kohn—Sham method: basic principles and application to strongly correlated ground and excited states of molecules. *WIREs Comput. Mol. Sci.* **2015**, *5*, 146–167.
- (325) Lee, S.; Kim, E. E.; Nakata, H.; Lee, S.; Choi, C. H. Efficient implementations of analytic energy gradient for mixed-reference spin-flip time-dependent density functional theory (MRSF-TDDFT). *J. Chem. Phys.* **2019**, *150*, 184111.

- (326) Lee, S.; Shostak, S.; Filatov, M.; Choi, C. H. Conical Intersections in Organic Molecules: Benchmarking Mixed-Reference Spin–Flip Time-Dependent DFT (MRSF-TD-DFT) vs Spin–Flip TD-DFT. J. Phys. Chem. A 2019, 123, 6455–6462.
- (327) Horbatenko, Y.; Lee, S.; Filatov, M.; Choi, C. H. How Beneficial Is the Explicit Account of Doubly-Excited Configurations in Linear Response Theory? *J. Chem. Theory Comput.* **2021**, *17*, 975–984.
- (328) Bannwarth, C.; Yu, J. K.; Hohenstein, E. G.; Martínez, T. J. Hole—hole Tamm—Dancoff-approximated density functional theory: A highly efficient electronic structure method incorporating dynamic and static correlation. *J. Chem. Phys.* **2020**, *153*, No. 024110.
- (329) Yu, J. K.; Bannwarth, C.; Hohenstein, E. G.; Martínez, T. J. Ab Initio Nonadiabatic Molecular Dynamics with Hole—Hole Tamm—Dancoff Approximated Density Functional Theory. *J. Chem. Theory Comput.* **2020**, *16*, 5499—5511.
- (330) Yu, J.; Li, J.; Zhu, T.; Yang, W. Accurate and efficient prediction of double excitation energies using the particle—particle random phase approximation. *J. Chem. Phys.* **2025**, *162*, No. 094101.
- (331) Dar, D. B.; Maitra, N. T. Oscillator strengths and excited-state couplings for double excitations in time-dependent density functional theory. *J. Chem. Phys.* **2023**, *159*, 211104.
- (332) Dar, D. B.; Maitra, N. T. Capturing the Elusive Curve-Crossing in Low-Lying States of Butadiene with Dressed TDDFT. *J. Phys. Chem. Lett.* **2025**, *16*, 703–709.
- (333) Li, X.; Govind, N.; Isborn, C.; DePrince, A. E., III; Lopata, K. Real-Time Time-Dependent Electronic Structure Theory. *Chem. Rev.* **2020**, *120*, 9951–9993.
- (334) Provorse, M. R.; Isborn, C. M. Electron dynamics with real-time time-dependent density functional theory. *Int. J. Quantum Chem.* **2016**, 116, 739–749.
- (335) Dreuw, A.; Wormit, M. The algebraic diagrammatic construction scheme for the polarization propagator for the calculation of excited states. *WIREs Comput. Mol. Sci.* **2015**, *5*, 82–95.
- (336) Plasser, F.; Crespo-Otero, R.; Pederzoli, M.; Pittner, J.; Lischka, H.; Barbatti, M. Surface Hopping Dynamics with Correlated Single-Reference Methods: 9H-Adenine as a Case Study. *J. Chem. Theory Comput.* **2014**, *10*, 1395–1405.
- (337) Marsili, E.; Prlj, A.; Curchod, B. F. E. Caveat when using ADC(2) for studying the photochemistry of carbonyl-containing molecules. *Phys. Chem. Chem. Phys.* **2021**, 23, 12945–12949.
- (338) Hättig, C. Structure Optimizations for Excited States with Correlated Second-Order Methods: CC2 and ADC(2). *Adv. Quantum Chem.* **2005**, *50*, 37–60.
- (339) Parker, S. M.; Roy, S.; Furche, F. Unphysical divergences in response theory. *J. Chem. Phys.* **2016**, *145*, 134105.
- (340) Kjønstad, E. F.; Fajen, O. J.; Paul, A. C.; Angelico, S.; Mayer, D.; Gühr, M.; Wolf, T. J. A.; Martínez, T. J.; Koch, H. Photoinduced hydrogen dissociation in thymine predicted by coupled cluster theory. *Nat. Commun.* **2024**, *15*, 10128.
- (341) Hait, D.; Lahana, D.; Fajen, O. J.; Paz, A. S.; Unzueta, P. A.; Rana, B.; Lu, L.; Wang, Y.; Kjønstad, E. F.; Koch, H.; Martínez, T. J. Prediction of photodynamics of 200 nm excited cyclobutanone with linear response electronic structure and ab initio multiple spawning. *J. Chem. Phys.* **2024**, *160*, 244101.
- (342) Cusati, T.; Granucci, G.; Persico, M. Photodynamics and Time-Resolved Fluorescence of Azobenzene in Solution: A Mixed Quantum-Classical Simulation. *J. Am. Chem. Soc.* **2011**, *133*, 5109–5123.
- (343) Cusati, T.; Granucci, G.; Martínez-Núñez, E.; Martini, F.; Persico, M.; Vázquez, S. Semiempirical Hamiltonian for Simulation of Azobenzene Photochemistry. *J. Phys. Chem. A* **2012**, *116*, 98–110.
- (344) Fabiano, E.; Keal, T. W.; Thiel, W. Implementation of surface hopping molecular dynamics using semiempirical methods. *Chem. Phys.* **2008**, *349*, 334–347.
- (345) Accomasso, D.; Persico, M.; Granucci, G. Diabatization by Localization in the Framework of Configuration Interaction Based on Floating Occupation Molecular Orbitals (FOMO-CI). *ChemPhoto-Chem.* **2019**, *3*, 933–944.

- (346) Accomasso, D.; Arslancan, S.; Cupellini, L.; Granucci, G.; Mennucci, B. Ultrafast Excited-State Dynamics of Carotenoids and the Role of the  $S_X$  State. *J. Phys. Chem. Lett.* **2022**, *13*, 6762–6769.
- (347) Fabiano, E.; Thiel, W. Nonradiative Deexcitation Dynamics of 9H-Adenine: An OM2 Surface Hopping Study. *J. Phys. Chem. A* **2008**, 112, 6859–6863.
- (348) Weingart, O.; Lan, Z.; Koslowski, A.; Thiel, W. Chiral Pathways and Periodic Decay in cis-Azobenzene Photodynamics. *J. Phys. Chem. Lett.* **2011**, *2*, 1506–1509.
- (349) Li Manni, G.; Fdez Galván, I.; Alavi, A.; Aleotti, F.; Aquilante, F.; Autschbach, J.; Avagliano, D.; Baiardi, A.; Bao, J. J.; Battaglia, S.; et al. The OpenMolcas Web: A Community-Driven Approach to Advancing Computational Chemistry. *J. Chem. Theory Comput.* **2023**, 19, 6933–6991.
- (350) Shiozaki, T. BAGEL: Brilliantly Advanced General Electronic-structure Library. *Wiley Interdiscip. Rev.: Comput. Mol. Sci.* **2018**, 8, No. e1331.
- (351) Neese, F. Software update: the ORCA program system, version 4.0. Wiley Interdiscip. Rev.: Comput. Mol. Sci. 2018, 8, No. e1327.
- (352) Aprà, E.; Bylaska, E. J.; de Jong, W. A.; Govind, N.; Kowalski, K.; Straatsma, T. P.; Valiev, M.; van Dam, H. J. J.; Alexeev, Y.; Anchell, J.; et al. NWChem: Past, present, and future. *J. Chem. Phys.* **2020**, *152*, 184102.
- (353) Barca, G. M. J.; Bertoni, C.; Carrington, L.; Datta, D.; De Silva, N.; Deustua, J. E.; Fedorov, D. G.; Gour, J. R.; Gunina, A. O.; Guidez, E.; et al. Recent developments in the general atomic and molecular electronic structure system. *J. Chem. Phys.* **2020**, *152*, 154102.
- (354) Wu, X.; Koslowski, A.; Thiel, W. Semiempirical Quantum Chemical Calculations Accelerated on a Hybrid Multicore CPU-GPU Computing Platform. *J. Chem. Theory Comput.* **2012**, *8*, 2272–2281.
- (355) Sun, Q.; Berkelbach, T. C.; Blunt, N. S.; Booth, G. H.; Guo, S.; Li, Z.; Liu, J.; McClain, J. D.; Sayfutyarova, E. R.; Sharma, S.; et al. PySCF: the Python-based simulations of chemistry framework. *Wiley Interdiscip. Rev.: Comput. Mol. Sci.* **2018**, 8, No. e1340.
- (356) Richings, G. W.; Habershon, S. MCTDH on-the-fly: Efficient grid-based quantum dynamics without pre-computed potential energy surfaces. *J. Chem. Phys.* **2018**, *148*, 134116.
- (357) Richings, G. W.; Robertson, C.; Habershon, S. Improved onthe-Fly MCTDH Simulations with Many-Body-Potential Tensor Decomposition and Projection Diabatization. *J. Chem. Theory Comput.* **2019**, *15*, 857–870.
- (358) Köppel, H.; Domcke, W.; Cederbaum, L. S.The multi-mode vibronic-coupling approach. In *Conical Intersections*; World Scientific: 2004; pp 323–367.
- (359) Heindl, M.; González, L. Taming Disulfide Bonds with Laser Fields. Nonadiabatic Surface-Hopping Simulations in a Ruthenium Complex. J. Phys. Chem. Lett. 2022, 13, 1894–1900.
- (360) Vindel-Zandbergen, P.; Matsika, S.; Maitra, N. T. Exact-Factorization-Based Surface Hopping for Multistate Dynamics. *J. Phys. Chem. Lett.* **2022**, *13*, 1785–1790.
- (361) Guan, Y.; Xie, C.; Yarkony, D. R.; Guo, H. High-fidelity first principles nonadiabaticity: diabatization, analytic representation of global diabatic potential energy matrices, and quantum dynamics. *Phys. Chem. Chem. Phys.* **2021**, 23, 24962–24983.
- (362) Westermayr, J.; Gastegger, M.; Menger, M. F. S. J.; Mai, S.; González, L.; Marquetand, P. Machine learning enables long time scale molecular photodynamics simulations. *Chem. Sci.* **2019**, *10*, 8100–8107.
- (363) Dral, P. O.; Barbatti, M. Molecular excited states through a machine learning lens. *Nat. Rev. Chem.* **2021**, *5*, 388–405.
- (364) Westermayr, J.; Marquetand, P. Machine Learning for Electronically Excited States of Molecules. *Chem. Rev.* **2021**, *121*, 9873–9926.
- (365) Schapiro, I.; Ryazantsev, M. N.; Frutos, L. M.; Ferré, N.; Lindh, R.; Olivucci, M. The Ultrafast Photoisomerizations of Rhodopsin and Bathorhodopsin Are Modulated by Bond Length Alternation and HOOP Driven Electronic Effects. *J. Am. Chem. Soc.* **2011**, *133*, 3354–3364.

- (366) Schnedermann, C.; Yang, X.; Liebel, M.; Spillane, K.; Lugtenburg, J.; Fernández, I.; Valentini, A.; Schapiro, I.; Olivucci, M.; Kukura, P.; et al. Evidence for a vibrational phase-dependent isotope effect on the photochemistry of vision. *Nat. Chem.* **2018**, *10*, 449–455. (367) Manzhos, S.; Carrington, T., Jr. Using neural networks to
- (367) Manzhos, S.; Carrington, T., Jr. Using neural networks to represent potential surfaces as sum of products. *J. Chem. Phys.* **2006**, 125, No. 084109.
- (368) Song, Q.; Zhang, X.; Peláez, D.; Meng, Q. Direct Canonical-Polyadic-Decomposition of the Potential Energy Surface from Discrete Data by Decoupled Gaussian Process Regression. *J. Phys. Chem. Lett.* **2022**, *13*, 11128–11135.
- (369) Avila, G.; Carrington, T., Jr. Using multi-dimensional Smolyak interpolation to make a sum-of-products potential. *J. Chem. Phys.* **2015**, *143*, No. 044106.
- (370) Panadés-Barrueta, R. L.; Peláez, D. Low-rank sum-of-products finite-basis-representation (SOP-FBR) of potential energy surfaces. *J. Chem. Phys.* **2020**, *153*, 234110.
- (371) Nadoveza, N. S.; Panadés-Barrueta, R. L.; Shi, L.; Gatti, F.; Peláez, D. Analytical high-dimensional operators in canonical polyadic finite basis representation (CP-FBR). *J. Chem. Phys.* **2023**, *158*, 114109.
- (372) Qiu, Z.; Magoulès, F.; Peláez, D. Single-entry computation of analytical hierarchical (binary) tree structures. *Adv. Eng. Softw.* **2025**, 203, No. 103873.
- (373) Shi, L.; Schröder, M.; Meyer, H.-D.; Peláez, D.; Wodtke, A. M.; Golibrzuch, K.; Schönemann, A.-M.; Kandratsenka, A.; Gatti, F. Quantum and classical molecular dynamics for h atom scattering from graphene. *J. Chem. Phys.* **2023**, *159*, 194102.
- (374) Persico, M.; Granucci, G. An overview of nonadiabatic dynamics simulations methods, with focus on the direct approach versus the fitting of potential energy surfaces. *Theor. Chem. Acc.* **2014**, 133, 1526.
- (375) Suchan, J.; Hollas, D.; Curchod, B. F. E.; Slavíček, P. On the importance of initial conditions for excited-state dynamics. *Faraday Discuss.* **2018**, 212, 307–330.
- (376) Janoš, J.; Slavíček, P.; Curchod, B. F. E. Selecting Initial Conditions for Trajectory-Based Nonadiabatic Simulations. *Acc. Chem. Res.* **2025**, *58*, 261–270.
- (377) Adamska, L.; Nayyar, I.; Chen, H.; Swan, A. K.; Oldani, N.; Fernandez-Alberti, S.; Golder, M. R.; Jasti, R.; Doorn, S. K.; Tretiak, S. Self-trapping of excitons, violation of condon approximation, and efficient fluorescence in conjugated cycloparaphenylenes. *Nano Lett.* **2014**, *14*, 6539–6546.
- (378) Ceriotti, M.; Bussi, G.; Parrinello, M. Nuclear Quantum Effects in Solids Using a Colored-Noise Thermostat. *Phys. Rev. Lett.* **2009**, *103*, No. 030603.
- (379) Ceriotti, M.; Bussi, G.; Parrinello, M. Colored-Noise Thermostats à la Carte. *J. Chem. Theory Comput.* **2010**, *6*, 1170–1180.
- (380) Huppert, S.; Plé, T.; Bonella, S.; Depondt, P.; Finocchi, F. Simulation of Nuclear Quantum Effects in Condensed Matter Systems via Quantum Baths. *Appl. Sci.* **2022**, *12*, 4756.
- (381) Barbatti, M.; Sen, K. Effects of different initial condition samplings on photodynamics and spectrum of pyrrole. *Int. J. Quantum Chem.* **2016**, *116*, 762–771.
- (382) Prlj, A.; Hollas, D.; Curchod, B. F. E. Deciphering the Influence of Ground-State Distributions on the Calculation of Photolysis Observables. *J. Phys. Chem. A* **2023**, *127*, 7400–7409.
- (383) Tavernelli, I.; Curchod, B. F. E.; Rothlisberger, U. Mixed quantum-classical dynamics with time-dependent external fields: A time-dependent density-functional-theory approach. *Phys. Rev. A* **2010**, *81*, No. 052508.
- (384) Mignolet, B.; Curchod, B. F. E.; Martínez, T. J. Communication: XFAIMS—eXternal Field Ab Initio Multiple Spawning for electron-nuclear dynamics triggered by short laser pulses. *J. Chem. Phys.* **2016**, *145*, 191104.
- (385) Penfold, T.; Pápai, M.; Møller, K. B.; Worth, G. A. Excited state dynamics initiated by an electromagnetic field within the Variational Multi-Configurational Gaussian (vMCG) method. *Comput. Theor. Chem.* **2019**, *1160*, 24–30.

- (386) Bajo, J. J.; Granucci, G.; Persico, M. Interplay of radiative and nonradiative transitions in surface hopping with radiation-molecule interactions. *J. Chem. Phys.* **2014**, *140*, No. 044113.
- (387) Heindl, M.; González, L. Validating fewest-switches surface hopping in the presence of laser fields. *J. Chem. Phys.* **2021**, *154*, 144102.
- (388) Fiedlschuster, T.; Handt, J.; Schmidt, R. Floquet surface hopping: Laser-driven dissociation and ionization dynamics of H2+. *Phys. Rev. A* **2016**, *93*, No. 053409.
- (389) Fiedlschuster, T.; Handt, J.; Gross, E. K. U.; Schmidt, R. Surface hopping in laser-driven molecular dynamics. *Phys. Rev. A* **2017**, 95, No. 063424.
- (390) Brumer, P. Shedding (Incoherent) Light on Quantum Effects in Light-Induced Biological Processes. *J. Phys. Chem. Lett.* **2018**, *9*, 2946–2955
- (391) Barbatti, M. Simulation of Excitation by Sunlight in Mixed Quantum-Classical Dynamics. J. Chem. Theory Comput. 2020, 16, 4849–4856.
- (392) Schirò, M.; Eich, F. G.; Agostini, F. Quantum-classical nonadiabatic dynamics of Floquet driven systems. *J. Chem. Phys.* **2021**, *154*, 114101.
- (393) Martínez-Mesa, A.; Saalfrank, P. Semiclassical modelling of finite-pulse effects on non-adiabatic photodynamics via initial condition filtering: The predissociation of NaI as a test case. *J. Chem. Phys.* **2015**, 142. 194107.
- (394) Gelin, M. F.; Huang, X.; Xie, W.; Chen, L.; Došlić, N.; Domcke, W. Ab Initio Surface-Hopping Simulation of Femtosecond Transient-Absorption Pump—Probe Signals of Nonadiabatic Excited-State Dynamics Using the Doorway—Window Representation. *J. Chem. Theory Comput.* **2021**, *17*, 2394—2408.
- (395) Villaseco Arribas, E.; Maitra, N. T.; Agostini, F. Nonadiabatic dynamics with classical trajectories: The problem of an initial coherent superposition of electronic states. *J. Chem. Phys.* **2024**, *160*, No. 054102.
- (396) Ondarse-Alvarez, D.; Oldani, N.; Roitberg, A.; Kleiman, V.; Tretiak, S.; Fernandez-Alberti, S. Energy transfer and spatial scrambling of an exciton in a conjugated dendrimer. *Phys. Chem. Chem. Phys.* **2018**, 20, 29648–29660.
- (397) Alfonso-Hernandez, L.; Oldani, N.; Athanasopoulos, S.; Lupton, J.; Tretiak, S.; Fernandez-Alberti, S. Photoinduced energy transfer in linear guest—host chromophores: A computational study. *J. Phys. Chem. A* **2021**, *125*, 5303—5313.
- (398) Schriever, C.; Lochbrunner, S.; Ofial, A. R.; Riedle, E. The origin of ultrafast proton transfer: Multidimensional wave packet motion vs. tunneling. *Chem. Phys. Lett.* **2011**, 503, 61–65.
- (399) Barone, V.; Alessandrini, S.; Biczysko, M.; Cheeseman, J. R.; Clary, D. C.; McCoy, A. B.; DiRisio, R. J.; Neese, F.; Melosso, M.; Puzzarini, C. Computational molecular spectroscopy. *Nat. Rev. Methods Primers* **2021**, *1*, 38.
- (400) Avagliano, D.; Bonfanti, M.; Nenov, A.; Garavelli, M. Automatized protocol and interface to simulate QM/MM timeresolved transient absorption at TD-DFT level with COBRAMM. *J. Comput. Chem.* **2022**, *43*, 1641–1655.
- (401) Puzzarini, C.; Bloino, J.; Tasinato, N.; Barone, V. Accuracy and Interpretability: The Devil and the Holy Grail. New Routes across Old Boundaries in Computational Spectroscopy. *Chem. Rev.* **2019**, *119*, 8131–8191.
- (402) Seidner, L.; Stock, G.; Domcke, W. Nonperturbative approach to femtosecond spectroscopy: General theory and application to multidimensional nonadiabatic photoisomerization processes. *J. Chem. Phys.* **1995**, *103*, 3998–4011.
- (403) Domcke, W.; Stock, G. Theory of ultrafast nonadiabatic excitedstate processes and their spectroscopic detection in real time. *Adv. Chem. Phys.* **1997**, *100*, 1–169.
- (404) Huang, X.; Xie, W.; Došlić, N.; Gelin, M. F.; Domcke, W. Ab Initio Quasiclassical Simulation of Femtosecond Time-Resolved Two-Dimensional Electronic Spectra of Pyrazine. *J. Phys. Chem. Lett.* **2021**, 12, 11736–11744.

- (405) Whittock, A. L.; Abiola, T. T.; Stavros, V. G. A Perspective on Femtosecond Pump-Probe Spectroscopy in the Development of Future Sunscreens. *J. Phys. Chem. A* **2022**, *126*, 2299–2308.
- (406) Hu, D.; Peng, J.; Chen, L.; Gelin, M. F.; Lan, Z. Spectral Fingerprint of Excited-State Energy Transfer in Dendrimers through Polarization-Sensitive Transient-Absorption Pump—Probe Signals: On-the-Fly Nonadiabatic Dynamics Simulations. *J. Phys. Chem. Lett.* **2021**, *12*, 9710—9719.
- (407) Xu, C.; Lin, K.; Hu, D.; Gu, F. L.; Gelin, M. F.; Lan, Z. Ultrafast Internal Conversion Dynamics through the on-the-Fly Simulation of Transient Absorption Pump—Probe Spectra with Different Electronic Structure Methods. *J. Phys. Chem. Lett.* **2022**, *13*, 661–668.
- (408) Perez-Castillo, R.; Freixas, V. M.; Mukamel, S.; Martinez-Mesa, A.; Uranga-Piña, L.; Tretiak, S.; Gelin, M. F.; Fernandez-Alberti, S. Transient-absorption spectroscopy of dendrimers via nonadiabatic excited-state dynamics simulations. *Chem. Sci.* **2024**, *15*, 13250–13261.
- (409) Bhattacherjee, A.; Leone, S. R. Ultrafast X-ray Transient Absorption Spectroscopy of Gas-Phase Photochemical Reactions: A New Universal Probe of Photoinduced Molecular Dynamics. *Acc. Chem. Res.* **2018**, *51*, 3203–3211.
- (410) Zhang, J.; Peng, J.; Hu, D.; Gelin, M. F.; Lan, Z. What Two-Dimensional Electronic Spectroscopy Can Tell Us about Energy Transfer in Dendrimers: Ab Initio Simulations. *J. Phys. Chem. Lett.* **2025**, *16*, 1007–1015.
- (411) Schuurman, M. S.; Blanchet, V. Time-resolved photoelectron spectroscopy: the continuing evolution of a mature technique. *Phys. Chem. Chem. Phys.* **2022**, 24, 20012–20024.
- (412) Pemberton, C. C.; Zhang, Y.; Saita, K.; Kirrander, A.; Weber, P. M. From the (1B) Spectroscopic State to the Photochemical Product of the Ultrafast Ring-Opening of 1,3-Cyclohexadiene: A Spectral Observation of the Complete Reaction Path. *J. Phys. Chem. A* **2015**, 119, 8832–8845.
- (413) Bhattacherjee, A.; Pemmaraju, C. D.; Schnorr, K.; Attar, A. R.; Leone, S. R. Ultrafast Intersystem Crossing in Acetylacetone via Femtosecond X-ray Transient Absorption at the Carbon K-Edge. *J. Am. Chem. Soc.* **2017**, *139*, 16576–16583.
- (414) Wolf, T. J. A.; Parrish, R. M.; Myhre, R. H.; Martínez, T. J.; Koch, H.; Gühr, M. Observation of Ultrafast Intersystem Crossing in Thymine by Extreme Ultraviolet Time-Resolved Photoelectron Spectroscopy. *J. Phys. Chem. A* **2019**, 123, 6897–6903.
- (415) Palmeira, T.; Conceição, D. S.; Ferreira, D. P.; Ferreira, C. C.; Ferreira, L. F. V.; Berberan-Santos, M. N. Obtaining triplet-triplet absorption spectra and triplet lifetimes of long-lived molecules with a UV-Visible spectrophotometer. *J. Photochem. Photobiol.* **2024**, 20, No. 100226.
- (416) Biswas, S.; Kim, J. W.; Zhang, X.; Scholes, G. D. Coherent Two-Dimensional and Broadband Electronic Spectroscopies. *Chem. Rev.* **2022**, *122*, 4257–4321.
- (417) Schultz, J. D.; Yuly, J. L.; Arsenault, E. A.; Parker, K.; Chowdhury, S. N.; Dani, R.; Kundu, S.; Nuomin, H.; Zhang, Z.; Valdiviezo, J.; et al. Coherence in Chemistry: Foundations and Frontiers. *Chem. Rev.* **2024**, *124*, 11641–11766.
- (418) Nelson, T. R.; Ondarse-Alvarez, D.; Oldani, N.; Rodriguez-Hernandez, B.; Alfonso-Hernandez, L.; Galindo, J. F.; Kleiman, V. D.; Fernandez-Alberti, S.; Roitberg, A. E.; Tretiak, S. Coherent exciton-vibrational dynamics and energy transfer in conjugated organics. *Nat. Commun.* **2018**, *9*, 2316.
- (419) Kaufman, B.; Marquetand, P.; Rozgonyi, T.; Weinacht, T. Longlived electronic coherences in molecules. *Phys. Rev. Lett.* **2022**, *131*, No. 263202.
- (420) Matselyukh, D. T.; Despré, V.; Golubev, N. V.; Kuleff, A. I.; Wörner, H. J. Decoherence and revival in attosecond charge migration driven by non-adiabatic dynamics. *Nat. Phys.* **2022**, *18*, 1206–1213.
- (421) Lee, Y.; Oang, K. Y.; Kim, D.; Ihee, H. A comparative review of time-resolved x-ray and electron scattering to probe structural dynamics. *Struct. Dyn.* **2024**, *11*, No. 031301.
- (422) Yong, H.; Kirrander, A.; Weber, P. M.Time-resolved X-ray Scattering of Excited State Structure and Dynamics. In *Structural Dynamics with X-ray and Electron Scattering*, 1st ed.; Amini, K.; Rouzée,

- A.; Vrakking, M. J. J., Eds.; Theoretical and Computational Chemistry Series; Royal Society of Chemistry: United Kingdom, 2024; Vol. 25, pp 344–373.
- (423) Odate, A.; Kirrander, A.; Weber, P. M.; Minitti, M. P. Brighter, faster, stronger: ultrafast scattering of free molecules. *Adv. Phys.: X* **2023**, *8*, No. 2126796.
- (424) Centurion, M.; Wolf, T. J.; Yang, J. Ultrafast Imaging of Molecules with Electron Diffraction. *Annu. Rev. Phys. Chem.* **2022**, 73, 21–42.
- (425) Razmus, W. O.; Acheson, K.; Bucksbaum, P.; Centurion, M.; Champenois, E.; Gabalski, I.; Hoffman, M. C.; Howard, A.; Lin, M.-F.; Liu, Y.; et al. Multichannel photodissociation dynamics in CS<sub>2</sub> studied by ultrafast electron diffraction. *Phys. Chem. Chem. Phys.* **2022**, 24, 15416—15427
- (426) Champenois, E. G.; List, N. H.; Ware, M.; Britton, M.; Bucksbaum, P. H.; Cheng, X.; Centurion, M.; Cryan, J. P.; Forbes, R.; Gabalski, I.; et al. Femtosecond Electronic and Hydrogen Structural Dynamics in Ammonia Imaged with Ultrafast Electron Diffraction. *Phys. Rev. Lett.* **2023**, *131*, No. 143001.
- (427) Yang, J.; Zhu, X.; Nunes, J. P. F.; Yu, J. K.; Parrish, R. M.; Wolf, T. J. A.; Centurion, M.; Gühr, M.; Li, R.; Liu, Y.; et al. Simultaneous observation of nuclear and electronic dynamics by ultrafast electron diffraction. *Science* **2020**, *368*, 885–889.
- (428) Yong, H.; Zotev, N.; Ruddock, J. M.; Stankus, B.; Simmermacher, M.; Carrascosa, A. M.; Du, W.; Goff, N.; Chang, Y.; Bellshaw, D.; et al. Observation of the molecular response to light upon photoexcitation. *Nat. Commun.* **2020**, *11*, 2157.
- (429) Yong, H.; Xu, X.; Ruddock, J. M.; Stankus, B.; Carrascosa, A. M.; Zotev, N.; Bellshaw, D.; Du, W.; Goff, N.; Chang, Y.; et al. Ultrafast X-ray scattering offers a structural view of excited-state charge transfer. *Proc. Natl. Acad. Sci. U. S. A.* **2021**, *118*, No. e2021714118.
- (430) Busch, G. E.; Rentzepis, P. M. Picosecond Chemistry. *Science* **1976**, 194, 276–283.
- (431) Khalil, M.; Marcus, M. A.; Smeigh, A. L.; McCusker, J. K.; Chong, H. H. W.; Schoenlein, R. W. Picosecond X-ray Absorption Spectroscopy of a Photoinduced Iron(II) Spin Crossover Reaction in Solution. *J. Phys. Chem. A* **2006**, *110*, 38–44.
- (432) Gawelda, W.; Pham, V.-T.; Benfatto, M.; Zaushitsyn, Y.; Kaiser, M.; Grolimund, D.; Johnson, S. L.; Abela, R.; Hauser, A.; Bressler, C.; Chergui, M. Structure Determination of a Short-Lived Excited Iron(II) Complex by Picosecond X-Ray Absorption Spectroscopy. *Phys. Rev. Lett.* 2007, 98, No. 057401.
- (433) Mayer, D.; Lever, F.; Picconi, D.; Metje, J.; Alisauskas, S.; Calegari, F.; Düsterer, S.; Ehlert, C.; Feifel, R.; Niebuhr, M.; et al. Following excited-state chemical shifts in molecular ultrafast x-ray photoelectron spectroscopy. *Nat. Commun.* **2022**, *13*, 198.
- (434) Kuhs, C. T.; Luther, B. M.; Krummel, A. T. Recent Advances in 2D IR Spectroscopy Driven by Advances in Ultrafast Technology. *IEEE J. Sel. Top. Quantum Electron.* **2019**, *25*, 3100313.
- (435) de Oliveira, H. J. S.; de Almeida, P. L., Jr; Sampaio, B. A.; Fernandes, J. P. A.; Pessoa-Neto, O. D.; de Lima, E. A.; de Almeida, L. F. A handheld smartphone-controlled spectrophotometer based on hue to wavelength conversion for molecular absorption and emission measurements. Sens. Actuators B: Chem. 2017, 238, 1084–1091.
- (436) Grasse, E. K.; Torcasio, M. H.; Smith, A. W. Teaching UV-Vis Spectroscopy with a 3D-Printable Smartphone Spectrophotometer. *J. Chem. Educ.* **2016**, 93, 146–151.
- (437) Baker, M. Is there a reproducibility crisis? *Nature* **2016**, 533, 452–454.
- (438) Major, G. H.; Avval, T. G.; Moeini, B.; Pinto, G.; Shah, D.; Jain, V.; Carver, V.; Skinner, W.; Gengenbach, T. R.; Easton, C. D.; et al. Assessment of the frequency and nature of erroneous x-ray photoelectron spectroscopy analyses in the scientific literature. *J. Vac. Sci. Technol. A* **2020**, *38*, No. 061204.
- (439) Baer, D. R.; Gilmore, I. S. Responding to the growing issue of research reproducibility. *J. Vac. Sci. Technol. A* **2018**, *36*, No. 068502. (440) Pinder, J. W.; Major, G. H.; Baer, D. R.; Terry, J.; Whitten, J. E.; Čechal, J.; Crossman, J. D.; Lizarbe, A. J.; Jafari, S.; Easton, C. D.; et al.

Avoiding common errors in X-ray photoelectron spectroscopy data

- collection and analysis, and properly reporting instrument parameters. *Appl. Surf. Sci. Adv.* **2024**, *19*, No. 100534.
- (441) Baer, D. R.; Artyushkova, K.; Brundle, C. R.; Castle, J. E.; Engelhard, M. H.; Gaskell, K. J.; Grant, J. T.; Haasch, R. T.; Linford, M. R.; Powell, C. J.; et al. Practical guides for x-ray photoelectron spectroscopy: First steps in planning, conducting, and reporting XPS measurements. *J. Vac. Sci. Technol. A* **2019**, *37*, No. 031401.
- (442) Mata, R. A.; Suhm, M. A. Benchmarking Quantum Chemical Methods: Are We Heading in the Right Direction? *Angew. Chem. Int. Ed* **2017**, *56*, 11011–11018.
- (443) Beckwith, J. S.; Rumble, C. A.; Vauthey, E. Data analysis in transient electronic spectroscopy—an experimentalist's view. *Int. Rev. Phys. Chem.* **2020**, *39*, 135–216.
- (444) Lang, B.; Rosspeintner, A.; Angulo, G.; Vauthey, E. Model-free decomposition of transient absorption spectra into components with time-dependent shape. *EPJ Web Conf.* **2019**, 205, No. 09011.
- (445) Lang, B.; Rosspeintner, A.; Vauthey, E. Model-free Investigation of Ultrafast Bimolecular Chemical Reactions: Bimolecular Photo Induced Electron Transfer. *EPJ. Web Conf.* **2013**, *41*, No. 05041.
- (446) Tudorovskaya, M.; Minns, R. S.; Kirrander, A. Effects of probe energy and competing pathways on time-resolved photoelectron spectroscopy: the ring-opening of 1,3-cyclohexadiene. *Phys. Chem. Phys.* **2018**, *20*, 17714–17726.
- (447) Kirrander, A.; Saita, K.; Shalashilin, D. V. Ultrafast X-ray Scattering from Molecules. *J. Chem. Theory Comput.* **2016**, *12*, 957–967
- (448) Zhong, D.; Zewail, A. H. Femtosecond Real-Time Probing of Reactions. 23. Studies of Temporal, Velocity, Angular, and State Dynamics from Transition States to Final Products by Femtosecond-Resolved Mass Spectrometry. *J. Phys. Chem. A* **1998**, *102*, 4031–4058.
- (449) Dantus, M. Tracking Molecular Fragmentation in Electron—Ionization Mass Spectrometry with Ultrafast Time Resolution. *Acc. Chem. Res.* **2024**, *57*, 845–854.
- (450) Roeding, S.; Brixner, T. Coherent two-dimensional electronic mass spectrometry. *Nat. Commun.* **2018**, *9*, 2519.
- (451) Hervé, M.; Despré, V.; Castellanos Nash, P.; Loriot, V.; Boyer, A.; Scognamiglio, A.; Karras, G.; Brédy, R.; Constant, E.; Tielens, A. G. G. M.; et al. Ultrafast dynamics of correlation bands following XUV molecular photoionization. *Nat. Phys.* **2021**, *17*, 327–331.
- (452) Marciniak, A.; Despré, V.; Barillot, T.; Rouzée, A.; Galbraith, M. C. E.; Klei, J.; Yang, C.-H.; Smeenk, C. T. L.; Loriot, V.; Nagaprasad Reddy, S.; et al. XUV excitation followed by ultrafast non-adiabatic relaxation in PAH molecules as a femto-astrochemistry experiment. *Nat. Commun.* **2015**, *6*, 7909.
- (453) Wang, S.; Kind, T.; Bremer, P. L.; Tantillo, D. J.; Fiehn, O. Beyond the Ground State: Predicting Electron Ionization Mass Spectra Using Excited-State Molecular Dynamics. *J. Chem. Inf. Model.* **2022**, *62*, 4403–4410.
- (454) Gonçalves, C. E. M.; Levine, R. D.; Remacle, F. Ultrafast geometrical reorganization of a methane cation upon sudden ionization: an isotope effect on electronic non-equilibrium quantum dynamics. *Phys. Chem. Chem. Phys.* **2021**, 23 (21), 12051–12059.
- (455) Koopman, J.; Grimme, S. Calculation of Mass Spectra with the QCxMS Method for Negatively and Multiply Charged Molecules. J. Am. Soc. Mass Spectrom. 2022, 33, 2226–2242.
- (456) Silva-Junior, M. R.; Schreiber, M.; Sauer, S. P. A.; Thiel, W. Benchmarks of electronically excited states: Basis set effects on CASPT2 results. *J. Chem. Phys.* **2010**, *133*, 174318.
- (457) Silva-Junior, M. R.; Sauer, S. P. A.; Schreiber, M.; Thiel, W. Basis set effects on coupled cluster benchmarks of electronically excited states: CC3, CCSDR(3) and CC2. *Mol. Phys.* **2010**, *108*, 453–465.
- (458) Kulichenko, M.; Nebgen, B.; Lubbers, N.; Smith, J. S.; Barros, K.; Allen, A. E. A.; Habib, A.; Shinkle, E.; Fedik, N.; Li, Y. W.; et al. Data Generation for Machine Learning Interatomic Potentials and Beyond. *Chem. Rev.* **2024**, *24*, 13681–13714.
- (459) Pinheiro, M.; de Oliveira Bispo, M.; Mattos, R. S.; Telles do Casal, M.; Garain, B. C.; Toldo, J. M.; Mukherjee, S.; Barbatti, M. ULaMDyn: enhancing excited-state dynamics analysis through streamlined unsupervised learning. *Digital Discovery* **2025**, *4*, 666–682.

- (460) Polonius, S.; Zhuravel, O.; Bachmair, B.; Mai, S. LVC/MM: A Hybrid Linear Vibronic Coupling/Molecular Mechanics Model with Distributed Multipole-Based Electrostatic Embedding for Highly Efficient Surface Hopping Dynamics in Solution. *J. Chem. Theory Comput.* **2023**, *19*, 7171–7186.
- (461) Cigrang, L. L. E.; Green, J. A.; Gómez, S.; Cerezo, J.; Improta, R.; Prampolini, G.; Santoro, F.; Worth, G. A. Non-adiabatic direct quantum dynamics using force fields: Toward solvation. *J. Chem. Phys.* **2024**, *160*, 174120.
- (462) Vandaele, E.; Mališ, M.; Luber, S. The  $\Delta$ SCF method for non-adiabatic dynamics of systems in the liquid phase. *J. Chem. Phys.* **2022**, 156, 130901.
- (463) Rivera, M.; Dommett, M.; Crespo-Otero, R. ONIOM-(QM:QM') Electrostatic Embedding Schemes for Photochemistry in Molecular Crystals. *J. Chem. Theory Comput.* **2019**, *15*, 2504–2516.
- (464) Zuehlsdorff, T. J.; Isborn, C. M. Modeling absorption spectra of molecules in solution. *Int. J. Quantum Chem.* **2018**, *119*, No. e25719.
- (465) Dral, P. O.; Barbatti, M.; Thiel, W. Nonadiabatic Excited-State Dynamics with Machine Learning. *J. Phys. Chem. Lett.* **2018**, 9 (19), 5660–5663.
- (466) Dupuy, L.; Maitra, N. T. Exciting DeePMD: Learning excited-state energies, forces, and non-adiabatic couplings. *J. Chem. Phys.* **2024**, *161*, 134103.